

# Thermal Diffusion and Diffusion Thermo Effects on MHD 3D Mixed Upper Convective Flow of Maxwell Nanofluid Flow Past using Nonlinear Radiative Heat Flux

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ARTICLE INFO	ABSTRACT
Article history: Received 17 March 2023 Received in revised form 15 April 2023 Accepted 12 May 2023 Available online 1 September 2023 <i>Keywords:</i> Chemical Reaction; Maxwell Nanofluid; Radiative Heat Flux	This article aims to investigate the effect of nanoparticles and magnetohydrodynamics (MHD) on the transfer of heat and mass using a three-dimensional upper-convected Maxwell (UCM) nanofluid flow across a stretched surface in the presence of diffusion thermo and thermal diffusion. A nonlinear radiative heat flow was included in formulating the equation that describes energy. The nonlinear partial differential equations of the issue are transformed into ordinary differential equations utilizing the similarity transformation. These equations are then solved using the well-known shooting approach in conjunction with the Runge-Kutta integration process of order four. To increase the dependability of our findings, we additionally make use of the bvp4c built-in function that is available in MATLAB. On the velocities, temperatures, and concentrations of the particles, the graphical and numerical representations of the effects of the main parameters, such as the Dufour parameter, the Brownian motion parameter, the Prandtl number, the thermophoresis parameter, and the magnetic parameter, are presented. It has been shown that the flow velocity decreases as a function of both the linear and nonlinear thermal radiation parameters. In addition, increasing values of the Brownian motion parameter have the effect of reducing the nanoparticle corport.

## 1. Introduction

In resent few years, study of the non-Newtonian fluids is curiously expanded because of their extensive dimension, useful technological and industrial applications. Shampoos, blood at low shear rate, soaps, apple sauce, mud, chyme, sugar solution, emulsion, etc are some real-life examples of non-Newtonian fluids. In polymer, chemical and biomedical industries, the importance of non-Newtonian fluids cannot be denied. In almost all the industrial and biological fluids, the relationship between the rate of deformation and the stress is not linear. The sole properties of all non-Newtonian fluids cannot be completely described by any concrete single equation/relation. Due to this, researchers have suggested various mathematical models of non-Newtonian fluids. Amongst these models, Maxwell fluids and viscoelastic fluids have ample range of industrial applications such as glass blowing, extrusion of polymer sheets, manufacturing of plastic films, hot rolling, crystal growing

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etc. The viscoelastic fluid models such as second order and/or Walter-B fluid models are recommended for fluids having small level of elasticity [1]. These fluid models violate some established rules of thermodynamics [2]. For highly viscoelastic polymers, second grade fluid models with high Deborah number do not give the meaningful results [3,4], which reduces their significance in the polymer industry. Consequently, some more realistic fluid models, such as Oldroyd-B or upperconvected Maxwell fluid models have been considered for the application purpose [5]. Indeed, these two models for viscoelastic fluid flow have been studied on stretching and non-stretching sheets. Ali and Ashrafi [6] have investigated the upper convected Maxwell fluid with high Weissenberg number over a linearly stretching sheet. Velocity and heat transfer analysis of the fluid flow is carried out by using the shooting technique. Mushtaq et al., [7] analyzed the Sakiadis flow of upper-convected Maxwell fluid through a stretching sheet using Cattaneo-Christov model. Omowaye and Animasaum [8] studied the MHD UCM (upper convected Maxwell) fluid over a melting surface subject to thermal stratification with variable thermo-physical properties. They concluded that velocity profile is enhanced for the higher values of Deborah number. Krupalakshmi et al., [9] found the numerical solution of UCM fluid in the existence of dust particles over convectively heated stretching sheet. They incorporated the magnetic field and discussed the effects of viscous dissipation, non-linear thermal radiation, and heat source/sink. Waini et al., [10] considered the inclined magnetic field through a continuously stretched sheet for the study of heat and fluid flow of UCM fluid. They concluded that the magnetic field's strength is enhanced when the inclination of the aligned magnetic field is high, and resultantly it increases the temperature and reduces the velocity of the fluid. Bilal et al., [11] have Studied on MHD 3d Upper Convected Maxwell Fluid Flow With thermophoretic effect Using Nonlinear Radiative Heat Flux.

The research on stagnation point flow of nanofluid over stretching surface has different applications in industries and technology. As a result, Raghunath *et al.*, [12] have discussed Influence of MHD mixed convection flow for maxwell nanofluid through a vertical cone with porous material in the existence of variable heat conductivity and diffusion. Raghunath *et al.*, [13] have possessed Radiation absorption on MHD Free Conduction flow through porous medium over an unbounded vertical plate with heat source. Li *et al.*, [14] expressed Effects of activation energy and chemical reaction on unsteady MHD dissipative Darcy–Forchheimer squeezed flow of Casson fluid over horizontal channel. Suresh Kumar *et al.*, [15] have analyzed numerical analysis of magnetohydrodynamics Casson nanofluid flow with activation energy, Hall current and thermal radiation. Raghunath [16] has studied Heat and Mass Transfer of an Unsteady Magnetohydrodynamic Nanofluid Flow Past a Vertical Porous Plate in the Presence of Chemical Reaction, Radiation and Soret Effects. Maatoug *et al.*, [17] have possessed variable chemical species and thermo-diffusion Darcy–Forchheimer squeezed flow of Jeffrey nanofluid in horizontal channel with viscous dissipation effects.

Thermal radiation is the phenomenon of energy or heat transmission in the form of electromagnetic waves. The thermal radiation is significant in the high-temperature variance case among the ambient fluid and boundary surface. In engineering and physics, radiative impacts play an essential role. The effects of radiation heat transfer on various flows are essential in high-temperature and space technology processes. The effects of radiation are important in monitoring heat transmission in the polymer industries, where the final product quality is influenced by heat controlling variables to some extent. Also, the radiative impacts are significant in missiles, aircraft, gas turbines, solar radiations, space vehicles, liquid metal fluids, MHD accelerators, and nuclear power plants. The impact of nonlinear thermal radiation on the Sakiadis flow was analysed by Pantokratoras and Fang [18]. The impact of thermal radiation and MHD flow of a water-based nanofluid in a shrinkable\stretchable divergent\convergent channel was examined by Dogonchi and Ganji [19]. The radiative flow via a porous surface was addressed by Khan *et al.*, [20]. Omar *et al.*,

[21] have studied Hall Current and Soret Effects on Unsteady MHD Rotating Flow of Second-Grade Fluid through Porous Media under the Influences of Thermal Radiation and Chemical Reactions. Deepthi *et al.*, [22] have discussed Recent Development of Heat and Mass Transport in the Presence of Hall, Ion Slip and Thermo Diffusion in Radiative Second Grade Material. Aruna *et al.*, [23] have analyzed an unsteady MHD flow of a second-grade fluid passing through a porous medium in the presence of radiation absorption exhibits Hall and ion slip effects. Raghunath *et al.*, [24] have expressed Hall, Soret, and rotational effects on unsteady MHD rotating flow of a second-grade fluid through a porous medium in the presence of chemical reaction and aligned magnetic field.

The Soret effect is associated with mass flux phenomena induced by heat diffusion, while the Dufour effect is related to the energy flux generated by the solute difference. The Soret impact is used to cope with concentrations of gases having lighter and medium molecular mass. Heat and mass transfer via the Soret and Dufour phenomena are significant in a wide range of industrial and engineering applications, like geosciences multi component melts, groundwater pollutant migration, solidification of binary alloys, chemical reactors, space cooling, isotope separation, oil reservoirs, and mixtures of gases. Shojaei et al., [25] used the second-grade fluid to examine the Dufour and Soret effect in a convective stretchy cylinder. In this work, they noticed that raising the viscoelastic parameter causes a rise in velocity profile, while the temperature and concentration profiles indicate the opposite behaviour. Similarly, The MHD nanofluid flow of two stretchable spinning discs was studied by Zangooee et al., [26]. The consequences of Soret and Dufour on MHD Casson fluid flow generated by a stretching sheet were inspected by Hayat et al., [27]. In the presence of heatgenerating and nonlinear thermal radiation, Pal and Mondal [28] numerically analyzed the thermophoresis, Soret, and Dufour impacts on steady-state flow via a non-isothermal wedge. Hayat et al., [29] explored heat and mass transfer in a porous media filled with a viscoelastic fluid flow across a stretched vertical surface under Soret and Dufour effect. Raghunath and Mohana Ramana [30] have discussed Soret and chemical reaction effects on heat and mass transfer in MHD flow of a Kuvshinski fluid through porous medium with aligned magnetic field and radiation, Nonlinear Dynamics and Applications. Raghunath et al., [31] have studied Chemical reaction with aligned magnetic field effects on unsteady MHD Kuvshinski fluid flow past an inclined porous plate in the presence of radiation and Soret effects.

All the above investigators disregard three-dimensional upper-convected Maxwell (UCM) nanofluid flow over a stretching surface, which has been considered to examine the effects of nanoparticles and magnetohydrodynamics (MHD) on the heat and mass transfer in the presence of soret and Dufour effects. Non-linear radiative heat flux is incorporated in the formulation of the energy equation. Similarity transformation reduces the non-linear partial differential equations of the problem to the ordinary differential equations, which are then solved by the well-known shooting technique through the Runge-Kutta integration procedure of order four. The built-in MATLAB function bvp4c is also used to improve the reliability of our results.

# 2. Formulation of the Problem

A steady incompressible upper convected Maxwell nanofluid over a bilinear stretching surface in the positive xy-plane is considered to investigate the behaviour of temperature and concentration. A uniform magnetic field of strength  $B_0$  is applied normal to the flow i.e., in the z-direction. The induced magnetic field is ignored because of the assumption of the small Reynolds number. Applied magnetic field drags the magnetic field lines in the direction of the flow which interact with the induced current density to give raise a force known as the Lorentz force. Further, a non-linear thermal radiation is taken into account during the formulation of the energy equation. The stretching surface velocities in the x and y plane are considered as  $U_w(x)$ . = ax and  $V_w(y)$ . = by respectively as shown in Figure 1. Under these assumptions, the governing equations of time-independent and incompressible boundary layer flow nanofluid over stretching sheet are given by



Fig. 1. Physical configuration of the problem

$$\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} + \frac{\partial w}{\partial z} = 0$$
(1)

$$u\frac{\partial u}{\partial x} + v\frac{\partial u}{\partial y} + w\frac{\partial u}{\partial z} = v\frac{\partial^2 u}{\partial x^2} - \lambda \left( \begin{aligned} u^2 \frac{\partial^2 u}{\partial x^2} + v^2 \frac{\partial^2 u}{\partial y^2} + w^2 \frac{\partial^2 u}{\partial z^2} + \\ 2uv\frac{\partial^2 u}{\partial x \partial y} + 2uw\frac{\partial^2 u}{\partial x \partial z} + 2vw\frac{\partial^2 u}{\partial y \partial z} \end{aligned} \right) - \left( \frac{\sigma B_0^2}{\rho} \right) \left( u + \lambda w \frac{\partial u}{\partial z} \right)$$
(2)

$$u\frac{\partial v}{\partial x} + v\frac{\partial v}{\partial y} + w\frac{\partial v}{\partial z} = v\frac{\partial^2 v}{\partial z^2} - \lambda \begin{pmatrix} u^2 \frac{\partial^2 v}{\partial x^2} + v^2 \frac{\partial^2 v}{\partial y^2} + w^2 \frac{\partial^2 v}{\partial z^2} + u^2 \frac{\partial^2 v}{\partial z^2$$

$$u\frac{\partial T}{\partial x} + v\frac{\partial T}{\partial y} + w\frac{\partial T}{\partial z} = \alpha \left(\frac{\partial^2 T}{\partial z^2}\right) + \tau \left(D_B \frac{\partial C}{\partial z}\frac{\partial T}{\partial z} + \frac{D_T}{T_{\infty}}\left(\frac{\partial T}{\partial z}\right)^2\right) - \frac{1}{\rho C_p}\frac{\partial q_r}{\partial z} + \frac{D_m k_T}{c_s c_p}\frac{\partial^2 C}{\partial z^2}$$
(4)

$$u\frac{\partial C}{\partial x} + v\frac{\partial C}{\partial y} + w\frac{\partial C}{\partial z} = \frac{D_m k_T}{T_m}\frac{\partial T^2}{\partial y^2} + D_B\left(\frac{\partial^2 C}{\partial z^2}\right) + \frac{D_T}{T_\infty}\frac{\partial^2 T}{\partial z^2} - K_r(C - C_\infty)$$
(5)

For this flow, corresponding boundary conditions are the corresponding boundary conditions for the governing PDEs are

$$u = u_w = ax, \quad v = v_w = b_y, \quad w = 0, \quad T = T_w, \quad C = C_w \quad \text{at } z = 0$$
  
$$u \to 0, \quad v \to 0, \quad w \to 0, \quad T \to T_\infty \quad C \to C_\infty \quad \text{as } z \to \infty$$
 (6)

Dimensionless quantities are introduced to simplify the mathematical analysis of the problem by introducing the following similarity transformation used to transform the PDEs to dimensionless ODEs

$$u = ax f'(\eta), v = ay g'(\eta), w = -\sqrt{av} \left( f(\eta) + g(\eta) \right), \eta = \sqrt{\frac{a}{v}} z, \theta(\eta) = \frac{T - T_{\infty}}{T_{w} - T_{\infty}}, \phi(\eta) = \frac{C - C_{\infty}}{C_{w} - C_{\infty}}$$
(7)

The Rosseland approximation can be used for the radiative heat flux vector qr because there is also self-absorption in addition to emission for an optically thick fluid. Since the absorption coefficient is typically wavelength dependent and significant, we can use the Rosseland approximation. Therefore, the definition of qr is [32, 33].

$$q_r = -\frac{4\sigma^*}{3N}\frac{\partial T^4}{\partial z}$$
(8)

The Eq. (8) can be expressed as [27] since non-linear thermal radiation is being taken into consideration.

$$T = T_{\infty} ((\theta_{w} - 1)\theta + 1).$$
(9)

Using Eq. (8) and Eq. (9)

$$q_r = -\frac{16\sigma^*}{3N}T_{\infty}^3((\theta_w - 1)\theta + 1)^3\frac{\partial T}{\partial z}$$
(10)

Upon converting Eq. (2) through Eq. (5) to ordinary differential equations, Eq. (1) is identically satisfied:

$$f''' - f'^{2} + (M^{2}\Lambda + 1)(f + g)f'' + 2\Lambda f'(f + g)f'' - \Lambda f'(f + g)^{2} f''' - M^{2} f'' = 0$$
(11)

$$g''' - g'^{2} + (M^{2}\Lambda + 1)(f + g)g'' + 2\Lambda g'(f + g)g'' - \Lambda f'(f + g)^{2}g''' - M^{2}g'' = 0$$
(12)

$$\theta'' + R_d \left( \left( \left( \theta_w - 1 \right) \theta + 1 \right)^3 + 3 \left( \theta_w - 1 \right) \left( \left( \theta_w - 1 \right) \theta + 1 \right)^2 \theta'^2 \right) + \Pr\left( f + g \right) \theta' + \Pr N_b \left( \theta' \phi' + \frac{N_T}{N_b} \theta'^2 \right) + \Pr D_u \phi' = 0$$
(13)

$$\phi'' + \Pr L_e \left( f \phi' - K_r \phi \right) + S_r L_e \theta'' + \frac{N_t}{N_b} \theta'' = 0$$
(14)

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The correlated Dimensionless boundary conditions (BCs) are

$$f(0) = 0, \quad f'(0) = 1, \quad g(0) = 0, \quad g'(0) = c, \quad \theta(0) = 0, \quad \phi(0) = 1 \quad at \quad \eta = 0$$
  
$$f'(\eta) \to 0, \quad g'(\eta) \to 0, \quad \theta(\eta) \to 0, \quad \phi(\eta) \to 0 \quad as \quad \eta \to \infty$$
 (15)

In the equations that do not include dimensions, the important parameters are defined as

$$M = \frac{\sigma B_0^2}{\rho a}, \text{ Pr} = \frac{v}{\alpha} = \frac{v \rho C_p}{k}, L_e = \frac{\alpha}{D_B}, c = \frac{b}{a}, N_b = \frac{\tau D_B (C_w - C_w)}{v}, N_t = \frac{\tau D_T (T_w - T_w)}{v},$$
$$Du = \frac{D_M k_T (C_w - C_w)}{C_S C_p v a^2 (T_w - T_w)}, R_d = \frac{4\sigma^* T_w^3}{kN}, \theta_w = \frac{T_w}{T_w} S_r = \frac{D_M k_T (T_w - T_w)}{T_m \alpha_m (C_w - C_w)}, K_r = \frac{K_r}{a}$$
(16)

The local Nusselt number  $Nu_x$ , and the local Sherwood number  $Sh_x$  are the physical quantities of relevance that influence the flow. These numbers have the following definitions:

$$Nu_{x} = \frac{xq_{w}}{k(T_{w} - T_{\infty})}, \quad Sh_{x} = \frac{xj_{w}}{D_{B}(C_{w} - C_{\infty})}$$
(17)

Where wall heat flux and wall mass flux respectively given by

$$q_{w} = -k \left[ \frac{\partial T}{\partial y} \right]_{z=0}, \qquad j_{w} = -D_{B} \left[ \frac{\partial C}{\partial y} \right]_{z=0}$$
(18)

The coefficient of Nusselt number, and the Sherwood number are all expressed in their nondimensional versions in terms of the similarity variable as follows

$$\operatorname{Re}_{z}^{1/2} Nu_{z} = -\left(1 + \frac{4}{3}R_{d}\theta_{w}^{3}\right)\theta'(0), \quad \operatorname{Re}_{z}^{1/2} Sh_{z} = -\phi'(0)$$
(19)

## 3. Solution Methodology

The system of non-linear ODEs (11-14) subject to the boundary conditions 15 has been solved by the shooting method for various values of the involved parameters. We observed through graphs that for  $\eta > 7$ , there is no significant variation in the behaviour of solutions. Therefore, on the basis of such computational experiments, we are pondering (0,7) as the domain of the problem instead of (0,  $\infty$ ). We denote f by  $y_1$ , g by  $y_4$ ,  $\theta$  by  $y_7$  and  $\phi$  by  $y_9$  for converting the boundary value problem (11-14) to the following initial value problem consisting of 10 first order differential equations.

 $y'_1 = y_2,$  $y'_2 = y_3,$ 

$$y'_{3} = \frac{1}{1 - K(y_{1} + y_{4})} (y_{2}^{2} - (M^{2}\Lambda + 1)(y_{1} + y_{4})y_{3} + 2\Lambda y_{2}y_{3}(y_{1} + y_{4}) + M^{2}y_{2}),$$
  

$$y'_{4} = y_{5},$$
  

$$y'_{5} = y_{6},$$
  

$$y'_{6} = \frac{1}{1 - K(y_{1} + y_{4})^{2}} (y_{5}^{2} - (M^{2}\Lambda + 1)(y_{1} + y_{4})y_{6} - 2\Lambda y_{5}y_{6}(y_{1} + y_{4}) + M^{2}y_{5}),$$
  

$$y'_{7} = y_{8},$$
  

$$y'_{7} = \frac{13y_{8}}{3 + 4R_{d}(1 + (\theta_{w} - 1)y_{7})^{3}} (\frac{(4Rd(\theta_{w} - 1)((\theta_{w} - 1)y_{7} + 1)^{2})y_{8} + Pr((y_{1} + y_{4}) + N_{t}y_{8} + N_{b}y_{10} + Duy_{10}))$$
  

$$y'_{9} = y_{10},$$
  

$$y'_{10} = -\Pr L_{e} (y_{1} + y_{4})y_{10} + \Pr L_{e} K_{r} y_{6} - S_{r}L_{e} y'_{5} - \frac{N_{t}}{N_{b}} y'_{8}$$

To solve the above initial value problem arising in the shooting method, Runge Kutta method of order four is used. Classical Newton method is applied for the refinement of initial guesses Q1, Q2, Q3 and Q4 subject to the tolerance of  $\varepsilon = 10^{-7}$ .

## 4. Results and Discussion

We have obtained the solution of Eq. (11) to Eq. (14) Subject to the Eq. (15) with the help of MATLAB software. We have sketched graphs to examine the influence of numerous parameters appearing in equations for dimensionless velocity, temperature, and concentration. The parameter's ranges are taken as Le=1.0, Pr=0.2, M=2.0, c=0.5, Rd=1.0, Nb=0.8, Nt=1.2,  $\Lambda$ =0.3, Du=0.5, Kr=0.2, Sr=0.5.

Figures 2 and 3 depict the typical profiles of velocity and temperature for the magnetic parameter M. By increasing the magnetic parameter M, a drag force known as the Lorentz force also increases which resultantly reduces the velocity of the fluid and hence the rate of heat transfer is reduced and this leads to an increment in the temperature.



Figures 4 and 5 reflect the impact of the Deborah number  $\Lambda$ , which is a ratio of the fluid relaxation time to its characteristic time scale on the velocity profiles. When the shear stress is applied on the fluid, the time in which it gains its equilibrium position is called relaxation time. This time is higher for the fluids having high viscosity. So, an increase in the Deborah number may increase the viscosity

of the fluid and hence the velocity decreases as shown in Figures 4 and 5. The fluid becomes Newtonian if we consider  $\Lambda = 0$  and its viscosity gradually increases with an increase in the Deborah number  $\Lambda$ . From Figure 5, it is also concluded that boundary layer thickness reduces for the upper convected Maxwell fluid. When  $\Lambda$  is increased, the hydrodynamic boundary layer thickness decreases.



In Figures 6 and 7, the effect of the variation in the Deborah number on the temperature  $\theta(\eta)$  and the nanoparticle concentration  $\phi(\eta)$  is displayed respectively. It is observed that the temperature and the concentration increase with an increase in the relaxation time. From this observation, we can conclude that the elastic force promotes the heat and the mass transfer in the upper-convected Maxwell nanofluid.



To see the variation in the temperature profile against the increasing values of the Prandtl number Pr, Figure 8 is plotted in which the increasing values of Prandtl number result in a thinner temperature boundary layer thickness. Fluids having larger Prandtl number have lower thermal diffusivity, and hence the temperature decreases. The same decreasing trend of Pr number on the mass concentration profile is observed in Figure 9.



The influence of Brownian motion parameter on concentration and temperature profiles is depicted through Figures 10 and 11. From the figures, it can be seen that as the values of Brownian motion parameter rises, the thermal boundary layer thickness increases and at the surface, the temperature gradient demises. But we witnessed an opposite result on the concentration profiles and concentration boundary layer thickness as Brownian motion parameter upsurges.



**Fig. 10.** Influence of Nb on  $\theta(\eta)$ 

**Fig. 11.** Influence of Nb on  $\phi(\eta)$ 

Figures 12 and 13 are devoted to demonstrate the impact of thermophoresis parameter on temperature and concentration profiles. From the figures, it is perceived that when thermophoresis parameter rises, there is an improvement of the thermal and concentration boundary layer thickness.



The temperature and nanoparticle concentration curves for different values of thermal radiation parameter are depicted in Figures 14 and 15. From the graph, it is possible to observe that as the values of thermal radiation parameter upsurge, the temperature graph and the temperature boundary layer thickness are snowballing.



In Figures 16 and 17, the effect of the diffusion thermo parameter Du on the temperature and nanoparticle concentration profiles. it is observed that the nanoparticle concentration decreases with an increment in Du, the reversal behaviour has observed in the case of temperature.



Figure 18 and Figure 19 illustrate that the Soret number Sr decreases temperature profile while there is an increase in concentration profile and boundary layer thickness. Higher temperature difference and a lower concentration difference are observed because of increasing values of the Soret number. This variation in the temperature and concentration differences is liable for the decrease in the temperature and an increase in the concentration. It is also noticed that the Dufour and Soret numbers have fairly contrary effects for temperature and nanoparticle concentration fields.



Table 1 shows the Comparison of the presently computed values of wall temperature gradient –  $\theta^{I}$  (0) with those of Bilal *et al.*, [11].

Table 1									
The Comparison of the presently computed									
values of wall temperature gradient $-\theta^{I}$ (0)									
with those of Bilal et al., [11]									
٨	С	Pr	Bilal et al., [11] Present stu						
1	0.5	2	1.01694	1.015478					
0.5			2.296655	2.278547					
1.0			2.243930	2.245785					
1.5	.5		2.19501	2.197521					
0.3			2.09403	2.047855					
	0.6		2.31293	2.301247					
	1.0		2.55918	2.564785					
		4	1.60165	1601547					
7 2.		2.24393	2.24578						
10 2.75508 2.721452									

The Numerical results of the local Nusselt and Sherwood numbers for various values of different parameters are tabulated in Table 2. From Table 2, it is observed that the rate of heat flux decreases for the increasing values of Deborah number  $\Lambda$  and magnetic parameter M. It happens due to the fact that an increase in the magnetic parameter will enhance the Lorentz force which slows down the motion of the fluid and resultantly the rate of heat flux is reduced. The same phenomenon is observed for the increasing value of  $\Lambda$  and M for the case of Sherwood number  $\varphi(0)$ . An increment is observed in the rate of the heat flux for the thermal radiation parameter Rd, the temperature ratio parameter  $\theta_w$  and the stretching ratio c. Similarly for temperature ratio parameter  $\theta_w$ , thermal radiation parameter Rd and stretching ratio c, a decreasing trend is noticed for the mass transfer rate. The influence of the thermophoresis parameter Nt, Brownian motion parameter Nb, Prandtl number Pr, land the Lewis number Le on the rate of heat and mass transfer is also shown in Table 2. From the numerical values, it is noticeable that Nt, Nb and Le have a decreasing effect on Nusselt number while this increases for the increasing values of Prandtl number. On the other hand, Sherwood number decreases for the increasing thermophoresis parameter Nt, however the rate of mass transfer enhances for the increasing values of Nb, Pr and Le.

The Numerical results of the local Nusselt and Sherwood numbers for various values of	of
different parameters	

	p												
٨	Kr	М	Rd	θw	С	Nt	Nb	Pr	Du	Sr	Le	Nuz	Shz
1.0	0.5	2.0	1.0	1.5	0.5	1.2	0.8	0.2	0.5	0.2	1.0	1.578521	0.7542141
0.2												1.495214	0.714245
0.4												1.401547	0.648752
0.6												1.364587	0.614578
		0.5										1.245775	0.612478
		1.0										1.002544	0.607247
		1.5										0.895475	0.601247
			0.1									0.787852	0.354785
			0.3									0.894578	0.547851
			0.6									0.942147	0.754782
				1.2								0.898542	0.354785
				1.4								0.987524	0.547852
				1.6								1.125878	0.745214
					0.2							1.078541	0.654785
					0.3							1.987852	0.697852
						0.5						1.345785	0.987852
						1.0						1.297854	0.854578
							0.3					1.457851	0.785452
								0.6				1.120124	0.987852
									0.2			0.785452	0.457852
									0.4			0.794521	0.403214
										0.5	1.0	1.245785	0.647851
										1.0	1.2	1.124785	0.874512
	1.2											0.898542	0.354785
	1.4											0.987524	0.547852
	1.6											1.125878	0.745214

## **5.**Conclusions

This study in the present paper reveals the influence of non-linear thermal radiation of electrically conducting upper convected Maxwell fluid over a bi-directional stretching surface. Non-linear differential equations are solved numerically by shooting method with fourth order Runge-Kutta integration technique. The main features of the study are as follows

- i. UCM fluids have lower boundary layer thickness as compared to Newtonian fluid. Nusselt and Sherwood number both are gradually increased when temperature ratio is enhanced.
- ii. The impact of Du on temperature and concentration are opposite. Same behavior has been observed in Sr.
- iii. Nanoparticle concentration decreases for Nb and increases for Nt. Flow velocity decreases for increasing value of thermal radiation parameter, the reversal behavior has observed in the case of diffusion thermo specification.
- iv. An increase in thermal boundary layer thickness is observed in temperature and concentration profiles.

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#### References

- [1] Bird, Robert Byron, Robert Calvin Armstrong, and Ole Hassager. "Dynamics of polymeric liquids. Vol. 1: Fluid mechanics." (1987).
- [2] Fosdick, R. L., and K. R. Rajagopal. "Anomalous features in the model of "second order fluids"." Archive for Rational Mechanics and Analysis 70 (1979): 145-152. <u>https://doi.org/10.1007/BF00250351</u>
- [3] Hayat, T., Z. Abbas, and M. Sajid. "Series solution for the upper-convected Maxwell fluid over a porous stretching plate." *Physics Letters A* 358, no. 5-6 (2006): 396-403. <u>https://doi.org/10.1016/j.physleta.2006.04.117</u>
- [4] Sadeghy, Kayvan, Amir-Hosain Najafi, and Meghdad Saffaripour. "Sakiadis flow of an upper-convected Maxwell fluid." *International Journal of Non-Linear Mechanics* 40, no. 9 (2005): 1220-1228. https://doi.org/10.1016/j.ijnonlinmec.2005.05.006
- [5] Rajagopal, Kumbakonam R., A. S. Gupta, and Alan S. Wineman. "On a boundary layer theory for non-Newtonian fluids." *International Journal of Engineering Science* 18, no. 6 (1980): 875-883. <u>https://doi.org/10.1016/0020-7225(80)90035-X</u>
- [6] Mohamadali, Meysam, and Nariman Ashrafi. "Similarity solution for high Weissenberg number flow of upperconvected maxwell fluid on a linearly stretching sheet." *Journal of Engineering* 2016 (2016). <u>https://doi.org/10.1155/2016/9718786</u>
- [7] Mushtaq, A., S. Abbasbandy, M. Mustafa, T. Hayat, and A. Alsaedi. "Numerical solution for Sakiadis flow of upperconvected Maxwell fluid using Cattaneo-Christov heat flux model." *AIP Advances* 6, no. 1 (2016): 015208. <u>https://doi.org/10.1063/1.4940133</u>
- [8] Omowaye, Adeola John, and Isaac Lare Animasaun. "Upper-convected maxwell fluid flow with variable thermophysical properties over a melting surface situated in hot environment subject to thermal stratification." *Journal of applied fluid mechanics* 9, no. 4 (2016): 1777-1790. <u>https://doi.org/10.18869/acadpub.jafm.68.235.24939</u>
- [9] Krupalakshmi, Koneri L., Bijjanal J. Gireesha, Basavarajappa Mahanthesh, and Rama Subba Reddy Gorla. "Influence of nonlinear thermal radiation and magnetic field on upperconvected Maxwell fluid flow due to a convectively heated stretching sheet in the presence of dust particles." *Commun. Numer. Anal.(ISPACS)* 2016, no. 1 (2016): 57-73. <u>https://doi.org/10.5899/2016/cna-00254</u>
- [10] Waini, Iskandar, Nurul Amira Zainal, and Najiyah Safwa Khashi'ie. "Aligned magnetic field effects on flow and heat transfer of the upper-convected Maxwell fluid over a stretching/shrinking sheet." In MATEC Web of Conferences, vol. 97, p. 01078. EDP Sciences, 2017. <u>https://doi.org/10.1051/matecconf/20179701078</u>
- [11] Bilal, M., M. Sagheer, and S. Hussain. "On MHD 3D upper convected Maxwell fluid flow with thermophoretic effect using nonlinear radiative heat flux." *Canadian Journal of Physics* 96, no. 1 (2018): 1-10. <u>https://doi.org/10.1139/cjp-2017-0250</u>
- [12] Kodi, Raghunath, Charankumar Ganteda, Abhishek Dasore, M. Logesh Kumar, G. Laxmaiah, Mohd Abul Hasan, Saiful Islam, and Abdul Razak. "Influence of MHD mixed convection flow for maxwell nanofluid through a vertical cone with porous material in the existence of variable heat conductivity and diffusion." *Case Studies in Thermal Engineering* 44 (2023): 102875. <u>https://doi.org/10.1016/j.csite.2023.102875</u>
- [13] Raghunath, Kodi, Mopuri Obulesu, and Konduru Venkateswara Raju. "Radiation absorption on MHD free conduction flow through porous medium over an unbounded vertical plate with heat source." *International Journal* of Ambient Energy (2023): 1-9. <u>https://doi.org/10.1080/01430750.2023.2181869</u>
- [14] Li, Shuguang, Kodi Raghunath, Ayman Alfaleh, Farhan Ali, A. Zaib, M. Ijaz Khan, Sayed M. ElDin, and V. Puneeth. "Effects of activation energy and chemical reaction on unsteady MHD dissipative Darcy–Forchheimer squeezed flow of Casson fluid over horizontal channel." *Scientific Reports* 13, no. 1 (2023): 2666. <u>https://doi.org/10.1038/s41598-023-29702-w</u>
- [15] Suresh Kumar, Y., Shaik Hussain, K. Raghunath, Farhan Ali, Kamel Guedri, Sayed M. Eldin, and M. Ijaz Khan. "Numerical analysis of magnetohydrodynamics Casson nanofluid flow with activation energy, Hall current and thermal radiation." *Scientific Reports* 13, no. 1 (2023): 4021. <u>https://doi.org/10.1038/s41598-023-28379-5</u>
- [16] Raghunath, Kodi. "Study of Heat and Mass Transfer of an Unsteady Magnetohydrodynamic (MHD) Nanofluid Flow Past a Vertical Porous Plate in the Presence of Chemical Reaction, Radiation and Soret Effects." *Journal of Nanofluids* 12, no. 3 (2023): 767-776. <u>https://doi.org/10.1166/jon.2023.1965</u>
- [17] Maatoug, Samah, K. Hari Babu, V. V. L. Deepthi, Kaouther Ghachem, Kodi Raghunath, Charankumar Ganteda, and Sami Ullah Khan. "Variable chemical species and thermo-diffusion Darcy–Forchheimer squeezed flow of Jeffrey nanofluid in horizontal channel with viscous dissipation effects." *Journal of the Indian Chemical Society* 100, no. 1 (2023): 100831. <u>https://doi.org/10.1016/j.jics.2022.100831</u>
- [18] Pantokratoras, Asterios, and Tiegang Fang. "Sakiadis flow with nonlinear Rosseland thermal radiation." *Physica Scripta* 87, no. 1 (2012): 015703. <u>https://doi.org/10.1088/0031-8949/87/01/015703</u>

- [19] Dogonchi, A. S., and D. D. Ganji. "Investigation of MHD nanofluid flow and heat transfer in a stretching/shrinking convergent/divergent channel considering thermal radiation." *Journal of Molecular Liquids* 220 (2016): 592-603. <u>https://doi.org/10.1016/j.molliq.2016.05.022</u>
- [20] Khan, Umair, Aurang Zaib, Mohsen Sheikholeslami, Abderrahim Wakif, and Dumitru Baleanu. "Mixed convective radiative flow through a slender revolution bodies containing molybdenum-disulfide graphene oxide along with generalized hybrid nanoparticles in porous media." *Crystals* 10, no. 9 (2020): 771. https://doi.org/10.3390/cryst10090771
- [21] Bafakeeh, Omar T., Kodi Raghunath, Farhan Ali, Muhammad Khalid, El Sayed Mohamed Tag-ElDin, Mowffaq Oreijah, Kamel Guedri, Nidhal Ben Khedher, and Muhammad Ijaz Khan. "Hall current and Soret effects on unsteady MHD rotating flow of second-grade fluid through porous media under the influences of thermal radiation and chemical reactions." *Catalysts* 12, no. 10 (2022): 1233. <u>https://doi.org/10.3390/catal12101233</u>
- [22] Deepthi, V. V. L., Maha MA Lashin, N. Ravi Kumar, Kodi Raghunath, Farhan Ali, Mowffaq Oreijah, Kamel Guedri, El Sayed Mohamed Tag-ElDin, M. Ijaz Khan, and Ahmed M. Galal. "Recent development of heat and mass transport in the presence of Hall, ion slip and thermo diffusion in radiative second grade material: application of micromachines." *Micromachines* 13, no. 10 (2022): 1566. <u>https://doi.org/10.3390/mi13101566</u>
- [23] Ganjikunta, Aruna, Hari Babu Kommaddi, Venkateswarlu Bhajanthri, and Raghunath Kodi. "An unsteady MHD flow of a second-grade fluid passing through a porous medium in the presence of radiation absorption exhibits Hall and ion slip effects." *Heat Transfer* (2023). <u>https://doi.org/10.1002/htj.22716</u>
- [24] Raghunath, Kodi, and Ravuri Mohanaramana. "Hall, Soret, and rotational effects on unsteady MHD rotating flow of a second-grade fluid through a porous medium in the presence of chemical reaction and aligned magnetic field." *International Communications in Heat and Mass Transfer* 137 (2022): 106287. <u>https://doi.org/10.1016/j.icheatmasstransfer.2022.106287</u>
- [25] Shojaei, Ahmadreza, A. Jafarian Amiri, S. Saedi Ardahaie, Kh Hosseinzadeh, and D. D. Ganji. "Hydrothermal analysis of Non-Newtonian second grade fluid flow on radiative stretching cylinder with Soret and Dufour effects." *Case Studies in Thermal Engineering* 13 (2019): 100384. <u>https://doi.org/10.1016/j.csite.2018.100384</u>
- [26] Zangooee, M. R., Kh Hosseinzadeh, and D. D. Ganji. "Hydrothermal analysis of MHD nanofluid (TiO2-GO) flow between two radiative stretchable rotating disks using AGM." *Case Studies in Thermal Engineering* 14 (2019): 100460. <u>https://doi.org/10.1016/j.csite.2019.100460</u>
- [27] Hayat, T., S. A. Shehzad, and A. Alsaedi. "Soret and Dufour effects on magnetohydrodynamic (MHD) flow of Casson fluid." *Applied Mathematics and Mechanics* 33 (2012): 1301-1312. <u>https://doi.org/10.1007/s10483-012-1623-6</u>
- [28] Pal, Dulal, and Hiranmoy Mondal. "Influence of thermophoresis and Soret–Dufour on magnetohydrodynamic heat and mass transfer over a non-isothermal wedge with thermal radiation and Ohmic dissipation." *Journal of Magnetism and Magnetic Materials* 331 (2013): 250-255. <u>https://doi.org/10.1016/j.jmmm.2012.11.048</u>
- [29] Hayat, T., M. Mustafa, and I. Pop. "Heat and mass transfer for Soret and Dufour's effect on mixed convection boundary layer flow over a stretching vertical surface in a porous medium filled with a viscoelastic fluid." *Communications in Nonlinear Science and Numerical Simulation* 15, no. 5 (2010): 1183-1196. <u>https://doi.org/10.1016/j.cnsns.2009.05.062</u>
- [30] Kodi, Raghunath, and Mohana Ramana Ravuri. "Soret and Chemical Reaction Effects on Heat and Mass Transfer in MHD Flow of a Kuvshinski Fluid Through Porous Medium with Aligned Magnetic Field and Radiation." In *Nonlinear Dynamics and Applications: Proceedings of the ICNDA 2022*, pp. 377-391. Cham: Springer International Publishing, 2022. <u>https://doi.org/10.1007/978-3-030-99792-2\_32</u>
- [31] Mohana Ramana, R., K. Venkateswara Raju, and K. Raghunath. "Chemical reaction with aligned magnetic field effects on unsteady MHD Kuvshinski fluid flow past an inclined porous plate in the presence of radiation and Soret effects." *Heat Transfer* 51, no. 7 (2022): 6431-6449. <u>https://doi.org/10.1002/htj.22598</u>
- [32] Ramzan, Muhammad, and Muhammad Bilal. "Time dependent MHD nano-second grade fluid flow induced by permeable vertical sheet with mixed convection and thermal radiation." *PloS one* 10, no. 5 (2015): e0124929. https://doi.org/10.1371/journal.pone.0124929
- [33] Ibrahim, Wubshet, and Rizwan UI Haq. "Magnetohydrodynamic (MHD) stagnation point flow of nanofluid past a stretching sheet with convective boundary condition." *Journal of the Brazilian Society of Mechanical Sciences and Engineering* 38, no. 4 (2016): 1155-1164. <u>https://doi.org/10.1007/s40430-015-0347-z</u>