



# Matlab Implementation using Holtrop and Mennen Method of Bare Hull Resistance Prediction for Surface Combatant Ship Coupled with CFD

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## ABSTRACT

Holtrop's & Mennen's method is one of the most widely used technique in resistance and powering prediction for tankers, general cargo ships, container ships and combatant surface ships. Holtrop's Statistical Analysis method is utilized, as in comparison to the other options, more complete and closer to the actual results. The main purpose of this paper is to develop a Matlab application using Holtrop's & Mennen's method for studying and research the total resistance of DTMB 5415 combatant ship. The solid modelling is developed using Maxsurf. The computational fluid dynamic (CFD) technique is applied to analyze the hydrodynamic behaviour of hull form and predict the total resistance ( $R_t$ ) to provide a description of the other prediction methods. The simulation process was executed using ANSYS software based on fluid flow (STAR-CCM+) solver. The variation of computational grid used in computation is SST (Shear Stress Transport) coarse and fine mesh size for hull speed up to 32 kn.  $R_t$  resulted from CFD computation is validated with results from Holtrop that has been developed by Matlab implementation. The larger the grid meshing size, the better the validation of the results. The CFD technique demonstrated good agreement with Holtrop formulae in predicting the ( $R_t$ ) of DTMB 5415.

## 1. Introduction

The most important factor to consider when designing a ship's power requirements is the ship's resistance, or the sea drag forces acting on the ship. It is critical to estimate ship resistance when designing the propulsion system because the power required to overcome sea drag forces contributes to propulsion system losses. To calculate ship resistance, three methods are used: statistical methods such as the Holtrop-Mennen (HM) method, numerical analysis or Computational Fluid Dynamics (CFD) simulations, and model testing in towing tank [1].

In the preliminary design stage, total ship resistance is predicted using statistical data or empirical formulas as an important first step before calculating ship resistance using a scaled model tested in a towing tank. It is also possible to predict several methods of ship resistance based on the ship type and method limitations. The HM method is based on regression analysis of full-scale data that is already available. It is a very useful tool for estimating ship resistance early in the ship design process

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[2]. However, it is important to understand that statistical methods provide only a rough estimate and may differ significantly from actual ship resistance values.

These computations' algorithms were created. Using the developed algorithms, simple MATLAB scripts were written, and attempts were made to compare the programs with the supply vessel specifics and standard commercial software, the MAXSURF resistance module. Once the design is complete, ship model tests in towing tanks are carried out to determine the ship's resistance. Scaled model and testing in towing tanks are both costly and time-consuming procedures. Furthermore, the results of the model tests must be scaled to the actual size of the ship, a process fraught with uncertainty [3]. Due to the availability of powerful computational resources and advancements in the field of CFD, CFD analysis is becoming the preferred method over model tests for calculating ship resistance.

The primary goal of this paper is to investigate and study ship resistance for a 142-meter combatant vessel. A CFD simulation procedure is used to calculate the calm water ship resistance using a case study of a DTMB 5415. Star CCM+ is the software used. Ship resistance was calculated at various ship speeds ranging from 5 knots on average to 32 knots at maximum. Because the mesh has an impact on the results of any CFD simulation, multiple meshes were used to test the mesh's sensitivity [4]. All simulation results were compared to Matlab calculations using the HM method. Star CCM+'s ability to perform ship resistance analysis was demonstrated.

## 2. Holtrop-Mennen Method

### 2.1 Hull Geometry and Ship Particulars

The HM method is arguably the most popular method for estimating displacement-type ship resistance and powering. This method employs the regression approach and allows for the analysis of various resistance components, such as the viscous frictional effect of sea water, the appendages of the vessel that house the anchors and the bilge, the possible resistance effects of the wave, the components that arise from the bulbous bow, and the theoretical ship. It is the only method that employs the ITTC form factor  $k$ . The hull-propeller interaction parameters thrust deduction, full-scale wake fraction, and relative rotative efficiency is also estimated using HM formulas [5].

The MATLAB implementation of the HM method is based on equations modelled using regression principles and is as follows:

$$R_{\text{total}} = R_f (1+k_1) + R_{\text{App}} + R_w + R_B + R_{\text{TR}} + R_A \quad (1)$$

Where  $R_f$  is the frictional resistance calculated using the ITTC-1957 friction formula, and  $1+k_1$  is the form factor describing the viscous resistance of the hull form in relation to  $R_f$ .  $R_{\text{App}}$  stands for appendage resistance.  $R_w$  is the resistance of making and breaking waves.  $R_B$  denotes the additional pressure resistance of the bulbous bow near the water's surface.  $R_{\text{TR}}$  is the additional pressure resistance of immersed transom stern.  $R_A$  denotes the model-ship correlation resistance.

The effective power required to overcome a given resistance,  $R_{\text{tot}}$ , at a given speed,  $V$ , is given as:

$$P_E = R_{\text{tot}} V \quad (2)$$

Where  $P_E$  is in KW,  $R_{\text{tot}}$  in KN and  $V$  in  $\text{ms}^{-1}$ . The shaft power required to overcome a given resistance,  $R_{\text{tot}}$  with a given speed  $V$  is given as:

$$P_S = P_E / \eta \quad (3)$$

Where  $P_s$  is in KW,  $\eta$  is the efficiency.

The MATLAB implementation requires the ship's length, beam, draught, and speed to be entered. Water density and kinematic viscosity are also required. This method is an efficient and accurate way to estimate a ship's resistance in calm water [6].

A database was created that contained the model test results of the DTMB 5415 combatant ship. The calculations are performed sequentially for the various resistance components and propulsion factors. Figure 1 and Table 1 show and list the hull geometry and main ship particulars for speeds up to 32 knots [7].



Fig. 1. DTMB #5415 Model geometry

**Table 1**  
 Main particulars of combatant Ship DTMB 5415

Particulars	Ship	Particulars	Ship	Particulars	Ship
$L_{OA}$ (m)	153.300	T (m)	6.150	GM (m)	1.938
$L_{PP}$ (m)	142.200	V ( $m^3$ )	8424.4	LCG (m)	70.137
$B_{OA}$ (m)	20.540	$\Delta$ (t)	8636	$C_B$	0.505
$B_{WL}$ (m)	19.082	KM (m)	9.493	$C_P$	0.616
D (m)	12.470	KG (m)	7.555	$C_M$	0.815

## 2.2 Source Code Implementation

The below mathematical models are best implemented using functional implementations [8]. Figure 2 depicts only the frictional component of total resistance, as represented by the r f.m file.

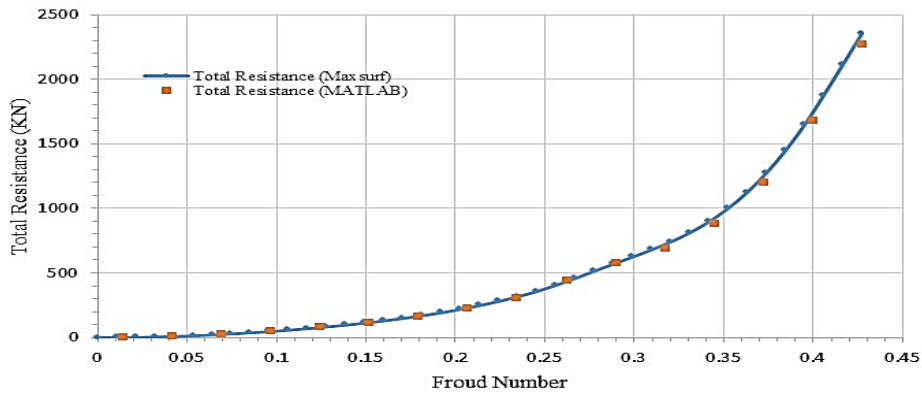
```

%%Calculations%%
% SApp=sum(double(Appen(:,2)));
% Req=sum(double(Appen(:,2)).*double(Appen(:,3)))/SApp-1;
Rn=Vs.*(Dens*LWL/Visc);
Fn=Vs./sqrt(9.81*LWL);
Tm=(Ta+TE)/2;
CB=Disp/(LWL*B*Tm);
Cp=CB/CH;
C13=1+0.003*Cstern;
if Tm/LWL > 0.05
    C12=(Tm/LWL)^0.2228446;
elseif 0.02<Tm/LWL && Tm/LWL<0.05
    C12=48.20*(Tm/LWL - 0.02)^2.078 + 0.479948;
else
    C12 =0.479948;
end
lcb=LCB;
LR=LWL*(1-Cp+0.06*Cp*lcb/(4*Cp-1));
K1=C13*(0.93+C12*(B/LR)^0.92497)*{(0.95-Cp)^(-0.521448)}*{(1-Cp+0.0225*lcb)^0.6906}-1;
% NSA=LWL*(2*Tm+B)*sqrt(CH)*(0.453+0.4425*CB-0.2862*CM-0.003467*B/Tm+0.3696*CB)+2.38*ABT/CB;
NSA=2976.7;
Cf=0.075./((log10(Rn)-2).^2);
if B/LWL < 0.11
    C7=0.229577*((B/LWL)^(1/3));
elseif B/LWL>0.11 && B/LWL< 0.25
    
```

Fig. 2. Source code implementation

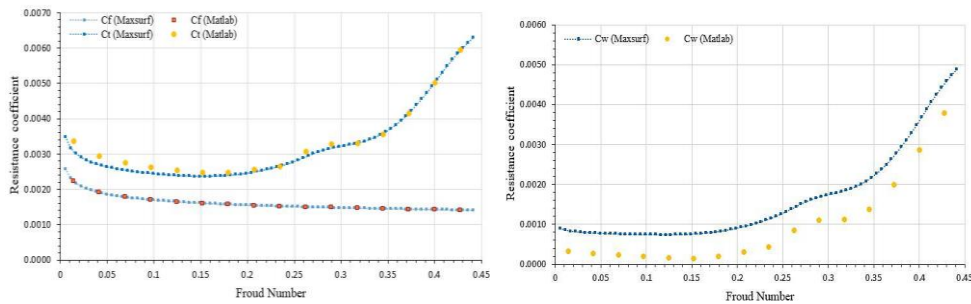
## 2.3 Matlab Results

The DTMB 5415 total resistance was calculated in the first preliminary step using a MATLAB implementation of the HM method with speeds ranging from 1 to 32 Kn, or  $F_n$  0.01 to 0.43. The calculated drag on the hull was measured, plotted, and compared with the Maxsurf results to assess the convergence of the solution depicted in Figure 3.

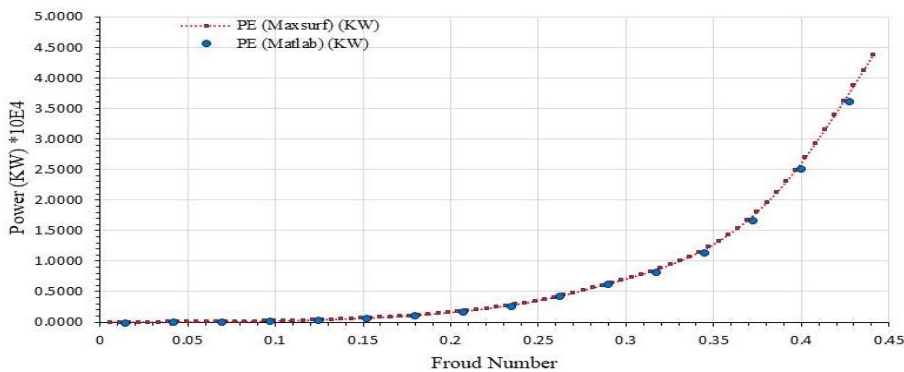


**Fig. 3.** Resistance curve by MATLAB for DTMB 5415 comparing with Maxsurf

Figure 4 depicts graphs of total and residual resistance coefficients ( $C_{TM}$  and  $C_R$  vs.  $Fr$ , respectively). The ITTC 57 formula has also been used to calculate viscous resistance.  $C_{TM}$  gradually decreases between 0.01 and 0.15, remains constant ( $C_{TM}=0.0028$ ) between 0.15 and 0.225, gradually increases between 0.225 and 0.35, and rapidly increases when  $Fr$  exceeds 0.35.  $C_R$  is essentially piecewise linear, with a rising slope for  $Fr$  values ranging from 0.1 to 0.35. In both cases, the presence of humps and hollows is minimal. Figure 5 depicts the effective power curve versus  $Fr$  for the Maxsurf and Matlab implementations. When we tested the Maxsurf resistance module against this formulation, we obtained the very good agreement shown below. Finally, Figure 6 depicts the free surface wave and volume fraction (water) contours of the hull model at various Froude numbers



**Fig. 4.** The curves of total and residual resistance coefficient  $C_{TM}$  and  $C_R$



**Fig. 5.** The effective power against  $Fr$

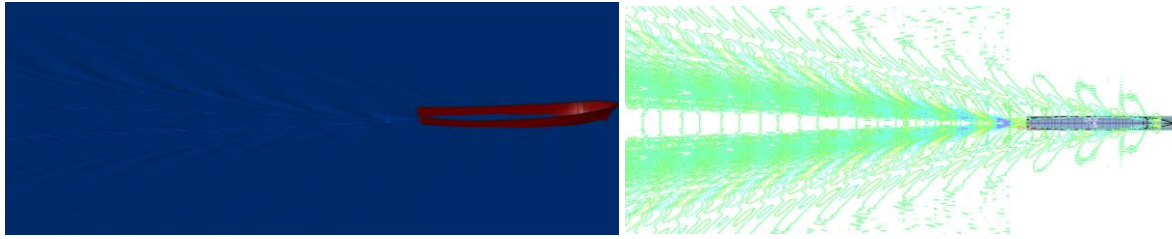


Fig. 6. Free surface wave and volume fraction contours at various Froude numbers  $Fn = 0.40$

### 3. Resistance Computation on STAR-CCM+

#### 3.1 Hull Geometry

The surface combatant DTMB model 5415 is a well-known test model, with numerous experimental and CFD test results made public and addressed at numerous workshops and conferences. Figure 7 and Table 2 depict the main dimensions and data used to conduct simulation tests on this ship. For computations and experiments, the bare hull condition is used [9, 10].

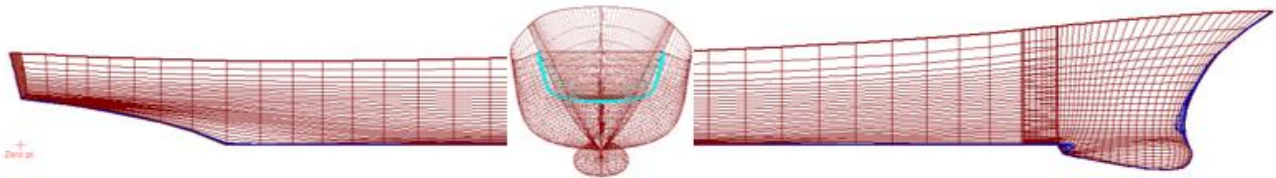


Fig. 7. Hull form of studied case

Table 2

Main particulars of DTMB #5415 (ITTC, 2005)

$L_{OA}$ (m)	6.167	D (m)	0.502	KM (m)	0.186
$L_{PP}$ (m)	5.72	T (m)	0.248	KG (m)	0.148
$B_{OA}$ (m)	0.826	V ( $m^3$ )	0.549	GM (m)	0.038
$B_{WL}$ (m)	0.767	$\Delta$ (t,kg)	0.549	LCG (m)	1.375

It is commonly regarded as the best test sample for validating a new numerical method on this combatant hull [11]. The grid structure and combatant ship profile corresponding to a scale of 24.48 were used for CFD calculations.

#### 3.2 Governing Equations

The Reynolds-averaged equations for mass and momentum conservation are as follows:

$$\frac{\partial u_i}{\partial x_i} = 0 \quad (4)$$

$$\frac{\partial u_i}{\partial t} + u_j \frac{\partial u_i}{\partial x_j} = -\frac{1}{\rho} \left( \frac{\partial P}{\partial x_i} \right) + \nu \frac{\partial^2 u_i}{\partial x_j^2} - \frac{\partial \overline{u_i' u_j'}}{\partial x_j} \quad (5)$$

where  $i, j = 1, 2$  and  $x_1, x_2$  denote the horizontal and the vertical dimensions, respectively,  $u_1$  and  $u_2$  are the mean velocity components,  $\overline{u_i' u_j'}$  defines the Reynolds stress component with  $u_i'$  is the fluctuating part of the velocity,  $p$  represents the dynamic pressure, and  $\rho$  is the fluid density [12].

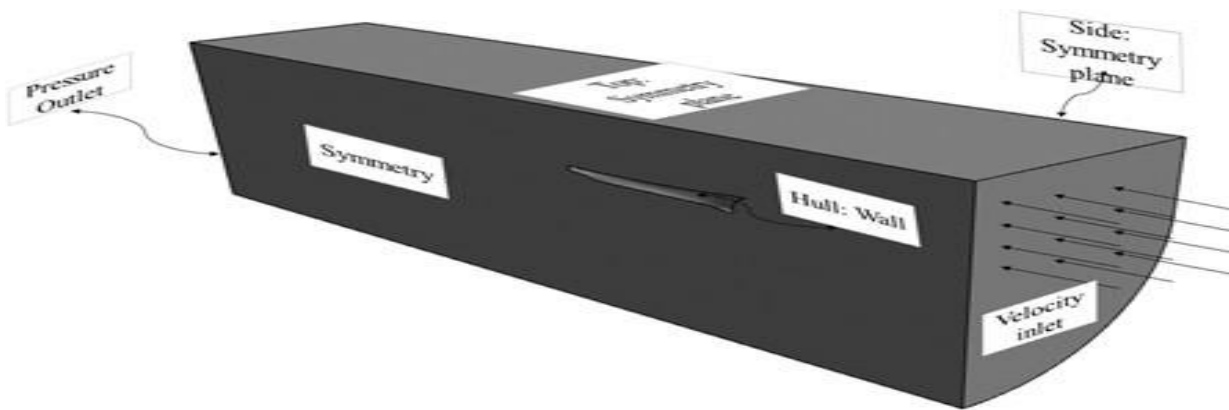
By using the Boussinesq approximation, the Reynolds stress component was defined in terms of a turbulent viscosity,  $\nu_T$ , and the mean flow gradients as follows:

$$-\overline{u'_i u'_j} = \nu_T \left( \frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i} \right) - \frac{2}{3} k \delta_{ij} \quad (6)$$

where  $\delta_{ij}$  denotes Kronecker delta function, and  $k$  denotes turbulent kinetic energy., three-dimensional numerical URANS simulations for the flow past a ship model were performed In this study. A two-layer form of the k-ε model, developed by Star-CCM + software, was used to predict the numerical simulations [13].

### 3.3 Computational Domain, Boundaries and Mesh Generation

A rectangular box defined the numerical computation domains. The dimensions of the computational domain were determined in accordance with the ITTC regulations and recommendations. The size dimensions are listed in Table 3, and Figure 8 depicts the fluid flow computational domain, with the size of the computational field proportional to the size of the model. The arrows on the domain’s left (inlet) side indicate the flow direction [14].The finite volume method was used in this study to discretize the domain into a set of adjoining cells. Furthermore, a fixed mesh method was used, in which it is assumed that the fluid moves at the same speed as the ship model, where the ship model is static [15].

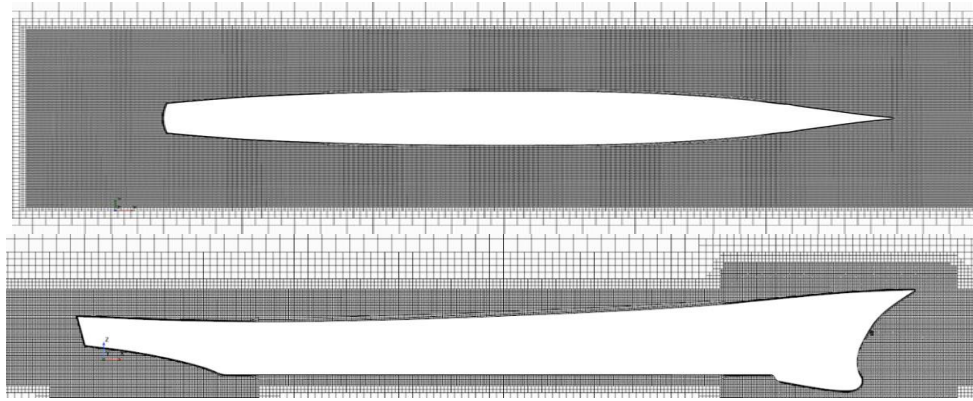


**Fig. 8.** Computational domain and boundary conditions of the DTMB 5415

**Table 3**

Computational domain dimensions		
Upstream	1.0 L <sub>0A</sub>	front of the bow
Down stream	3.0 L <sub>0A</sub>	from the stern
Top	0.5 L <sub>0A</sub>	depth of air zone
Bottom	1.0 L <sub>0A</sub>	depth of water zone
Transverse	1.0 L <sub>0A</sub>	width of both zones

Figure 9 depicts perspective views of the domain as well as slice views of the refinement areas. Grids are finer in regions surrounding the ship model near the free surface and over a longitudinal slice of the ship bow and stern, allowing the generation of inflation layers around the free surface to adequately capture the hull's high-velocity gradients and waves [16].



**Fig. 9.** Top and side view of the computational mesh 2 on the medium grid

In order to use second-order temporal discretization, we implemented the SIMPLE algorithm in code Star-CCM+. While the  $k-\epsilon$  turbulence approach was used for the calculations, the second-order upwind scheme was used. The outlet was placed at the right boundary, where the gradients of outflow velocity in the streamwise direction were set to zero and pressures were assigned a reference value of zero [17]. A slip condition was assumed on the bottom boundaries, while a symmetry condition was assumed on the side boundaries. On the model surface, a non-slip boundary condition was assumed.

A volume of fluid (VOF) model is used to simulate free-surface flow. A conservation equation for the volume fraction of water is used to derive the water surface position implicitly [18]. This equation is discretized using specific compressive discretization schemes to keep the transition between water and air close to a discontinuity. Fine meshes are required at the surface to accurately resolve the volume fraction [19].

The numerical simulations were run on three different grids, each with a finer mesh and a refinement factor of  $c = 1.25$  uniformly specified for all spatial directions. To estimate the discretization errors, one method was used. This method produced good, consistent predictions for a variety of transient problems, including those investigated here [20]. The method demanded that the same refinement factors be applied to all dimensions and that spatial and temporal refinements are performed concurrently [21]. It considered uniform refinement in all directions (space and time) with a constant CFL number. The one-dimensional CFL number, which is a good measure for convection-dominated flow, was written as follows:

$$r = \frac{\Delta x_{i+1}}{\Delta x_i} = \frac{\Delta t_{i+1}}{\Delta t_i} \Rightarrow \text{CFL} = u \frac{\Delta t}{\Delta x} = \text{const} \quad (7)$$

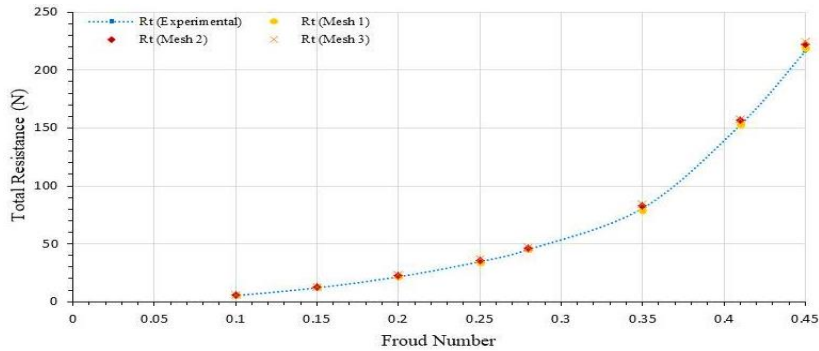
Where  $\Delta x$  and  $\Delta t$  are the spatial and time-step sizes, respectively, the index  $i$  denotes the level of refinement,  $r$  is the refinement factor, and  $u$  is the fluid velocity. To ensure numerical stability in all cases, the  $y^+$  value was set to one. Mesh 3 represented the coarse grid, mesh 2 the medium grid, and mesh 1 the fine grid, all of which were well-matched with the factor.

## 4. Results and Discussion

### 4.1 Numerical Calculations

The calm water resistance of the DTMB 5415 model was tested using CFD against model  $F_n$ , ranging from 0.01 to 0.45. The experimental results of the ship's towing tank test are required to validate the results obtained by Star-CCM+ using specific mesh densities and the conditions applied to boundaries and solver. Resistance tests for the bare hull at different speeds up to 3.75 m/sec were run for 9 days on a computer with 16 cores and a mesh density of 2.1 million cells. To estimate the

hydrodynamic performances for the CFD mesh investigation, three different mesh sizes were used. To evaluate the convergence of the solution as depicted in Figure 10, the calculated drag on the hull was measured, plotted, and compared with the experimental results. The findings for the coarse, medium and fine grid results are extremely similar and the difference  $\epsilon = (\text{medium} - \text{coarse}) / (\text{fine} - \text{medium})$ , where  $0 < \epsilon < 1$  is small and acceptable as shown in Table 4.



**Fig. 10.** Resistance curve for DTMB #5415-51 comparing three different sized grids with Maxsurf

**Table 4**

The CFD results for DTMB 5415 model

Fn	0.1	0.15	0.2	0.25	0.28	0.35	0.41	0.45
$R_T$ (N) (C)	5.98	12.88	23.33	36.98	47.32	84.75	157.9	224.48
$R_T$ (N)(M)	5.85	12.81	22.78	35.82	46.32	82.77	156.64	222.32
$R_T$ (N) (F)	5.68	12.72	22.1	34.3	45.3	78.8	152.9	218.91
Difference $\epsilon$	0.764706	0.777778	0.808824	0.763158	0.980392	0.498741	0.336898	0.633431

According to the bare hull results, the mesh generation approach can be used to estimate hydrodynamic performances using CFD, and numerical convergence shows that the overall strategy is suitable for resistance prediction. The results for the coarse and medium grids are very similar, and the difference between the medium and fine grids is larger but still manageable. As a result, the fine grid provides the best match for the calculations and displays the most appropriate results. Table 5 displays the results of the verification and validation exercises for these three grids' total resistance force at a flow stream velocity of 3.37 m/s. After this checking of STAR-CCM+ results, it is possible now move to calculate drag resistance with bulbous using this setting of mesh and solver parameters' which can be considered as reliable.

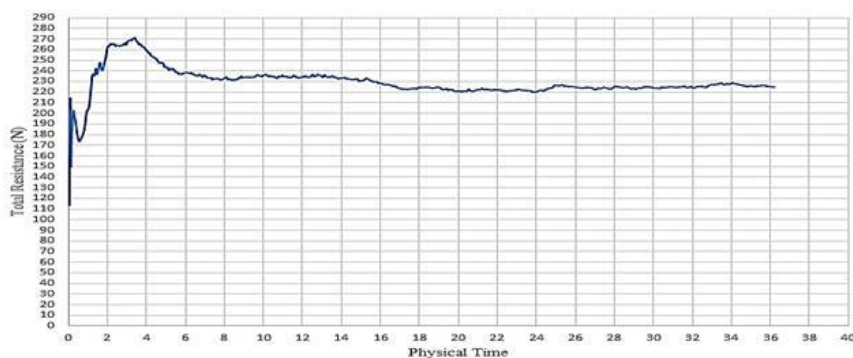
**Table 5**

Grid convergence for a DTMP-5415 model obtained from different grids

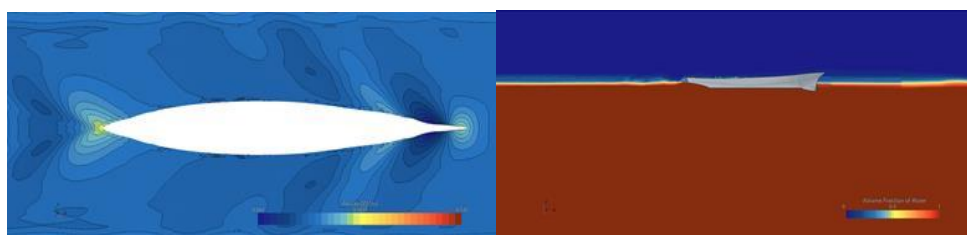
Element	$\Delta x$ [m]	No. of cell x106	$\Delta t$ [sec]	RT (Exp.)	RT (Num.)	$\Delta RT$ (%)
Coarse	0.3	0.542178	0.01	216.13 N	224.48	3.86
Medium	0.21	1.439452	0.0071	216.13 N	222.32	2.86
Fine	0.15	3.711726	0.005	216.13 N	218.91	1.29

Figure 11 depicts the total resistance time histories at Fr 0.38 for the 40 seconds, at which the simulation was run. It is possible to see how the free surface causes the graphs to oscillate. Finally, Figure 12 depicts the wave pattern and water volume fraction hull model for the coarse grid at Froude number 0.40.





**Fig. 11.** Time history of resistance as generated in CFD at  $Fr=0.38$

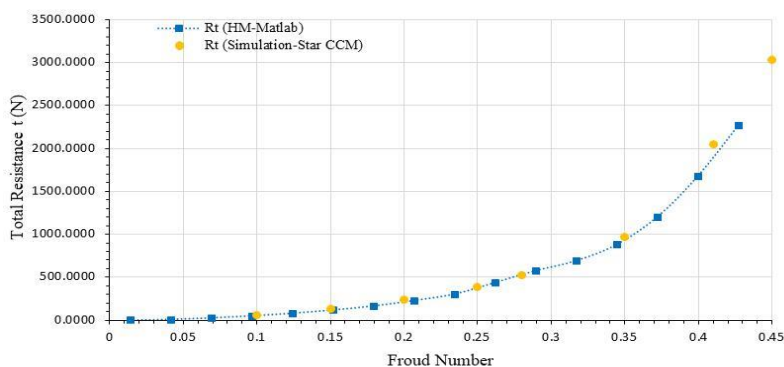


**Fig. 12.** Wave pattern and Water volume fraction on the ship hull and its center symmetry plane at  $Fn = 0.40$  - coarse grid

#### 4.2 Comparison of Resistance Results

The scale model ship was used to investigate the full similarity technique (FST) after the validation study. The resistance components at the hull model were calculated, and the results were presented using both Froude and Reynolds conditions for the naval combatant. Because increasing element numbers result in decreasing wall  $y^+$  values, numerical  $C_F$  values approach the ITTC-1957 formula. In other words, because the boundary layer grid has a low resolution, increasing the wall  $y^+$  value degrades the calculation of  $C_F$  in full-scale resistance prediction. As the number of elements increases, the  $C_R$  values of full-scale ships at various grid sizes reach the value of model-scale ships. The functionality of FST on the prediction of a full-scale ship's  $C_T$  at model scale dimensions was investigated. The previous results were taken and represented on a graph for validation purposes.

Figure 13 depicts the numerical results of STAR-CCM+ and the predicted method of HM for full-scale ship total resistance. Instead of experimental results for this ship that have yet to be performed, these results are for a bare hull without appendages (twin screws, bow thrusters, and two rudders).



**Fig. 13.** Comparisons between Results of Star-CCM+ and HM-Matlab for Bare Hull

At lower speeds, the agreement between the CFD simulation calculations and the Matlab data deteriorates; at  $Fr = 0.35$ , the CFD values deviate significantly from the Matlab data. In general, the results show that the resistance values at various speeds for the fine mesh agree with the HM data very well, with an error of less than 5%. Between the two methods, total resistance has the best match. By being in the range of the two, we can see a good deal of consistency in the results for higher speeds for STAR-CCM+ with the HM method, but there is less agreement for 20 knots.

## 5. Conclusion

To overcome the disadvantages of CFD tools and the difficulties of towing tank tests, this paper attempts to provide a method that provides a fast and reliable estimate of resistance during the initial design stage. Among the hydrodynamic characteristics, resistance evaluation during the initial design stage is critical. The current research contributes total resistance for combatant geometry (DTMB 5415).

This study looked at the mathematical model formulation for computing the vessel's bare hull resistance using the HM method. The algorithm and implementation of these formulations were then developed using the functional programming approach in MATLAB, a scientific computing language.

A significant portion of the current data set was cross-validated using DTMB experimental data, yielding an excellent outcome. Extensive comparisons of our Star-CCM+ calculations and experimental results for DTMB 5415 demonstrate that the method is acceptable and that the mesh refinement method is capable of helping estimate the model's hydrodynamic performance. Many different meshes, time steps, volume mesh domains, and boundary conditions were tested. After comparing the total resistance grid obtained results through the CFD, we reach the conclusion that the fine grid is best suited to the calculation and produces the best results because convergent results are obtained as mesh size decreases, so the fine grid will be used.

The developed algorithms were then compared with a standard Star-CCM+ resistance module and found to have very good agreement and sufficient accuracy. The HM statistical analysis method is more comprehensive and accurate.

## Acknowledgement

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