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# The Effect of Thermophoresis on MHD Stream of a Micropolar Liquid Through a Porous Medium with Variable Heat and Mass Flux and Thermal Radiation

P. Roja<sup>1,\*</sup>, T. Sankar Reddy<sup>2</sup>, S. M. Ibrahim<sup>3</sup>, G. Lorenzini<sup>4</sup>, Nor Azwadi Che Sidik<sup>5</sup>

- 1 Department of Humanities and Sciences, Annamacharya Institute of Technology and sciences, Rajmpeta, Kadapa-516126, A.P., India
- <sup>2</sup> Department of Humanities and Sciences, Annamacharya Institute of Technology and sciences, C. K. Dinne, Kadapa-516003, A.P., India
- Department of Mathematics, GITAM (Deemed to be University), Visakhapatnam, Andhra Pradesh, -520045, India
- <sup>4</sup> Department of Industrial Engineering, University of Parma, Parco Area delle Scienze 181/A, Parma, 43124, Italy
- Malaysia-Japan International Institute of Technology, Universiti Teknologi Malaysia, Jalan Sultan Yahya Petra, Kuala Lumpur, Malaysia

#### **ARTICLE INFO**

#### **ABSTRACT**

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In this paper, the combined possessions of thermal radiation and thermophoresis on stable Magnetohydrodynamic free convection stream of a micropolar liquid past an erect porous laminate during a porous medium in the occurrence of variable heat and mass fluxes are engaged into report is measured. The leading non-linear partial differential equations of the crisis are changed into a scheme of nonlinear ordinary differential equations during suitable similarity conversion and Runge—Kutta Fourth order with shooting procedure scheme. The possessions of a variety of substantial parameters on the dimensionless stream, microrotation, temperature, and concentration profiles are discussed and offered graphically. In the end, numerical ideals of the substantial quantities, such as the limited skin factor, the combine stress coefficient, the local Nusselt quantity and the local Sherwood quantity are tabulated with the variant of magnetic constraint, coupling invariable, Darcy constraint, modified Forchheimer number, radiation constraint, and thermophoretic constraints.

### 1. Introduction

The hypothesis of micropolar has inward massive courtesy throughout the current lifetime since the conventional Newtonian liquids cannot explicitly portray the quality of liquid with suspended particles, polar liquids, suspension solutions, liquid crystals, colloidal solutions and liquid containing minute additives. Actually, micropolar liquids may present the non-Newtonian liquids consisting of tiny inflexible cylindrical fundamentals or dumb-bell molecules, polymer liquids, liquids suspensions and animal blood. The survival of grime or smoulder exacting in a gas may also be modelled by means of micropolar liquid dynamics. Eringen [1] earliest imitative the hypothesis of micropolar liquids, which illustrates the microrotation possessions to the microstructures. Eringen [2] extensive his proposal to the hypothesis of thermomicropolar liquids, which attention to the particular possessions

E-mail address: tsthummalamaths@gmail.com (P. Roja)

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<sup>\*</sup> Corresponding author.

of microstructures on the liquid stream. The mathematical hypothesis of equations of micropolar liquids and applications of these liquids in the hypothesis of lubrication and in the hypothesis of porous media are given in latest books by Eringen [3] and Lukaszewicz [4].

Free convection in the border layer stream of a micropolar liquid along a vertical wavy shell was developed by Chiu and Chou [5]. Hassanien and Gorla [6] derived the heat transport to a micropolar liquid from a non-isothermal elongating area with suction and blowing. Mixed convection border layer stream of a micropolar liquid on a flat laminate was derived by Gorla [7]. Besides, the stream description of the border layer of micropolar liquid over a semi-infinite laminate in altered situations has been studied by numerous authors [8-15]. In the beyond mentioned mechanism the consequence of the induced magnetic field was ignored.

The crisis of the heat and mass transport for non-Newtonian liquids in porous media is of to large extent significance appropriate to its realistic manufacturing applications, such as lubricate healing, food dispensation, and resources dispensation [16-22]. The kind of convective heat and mass transport of non-Newtonian liquids in porous media are moderately altered those that of Newtonian liquids in porous media as of the non-linear scenery of non-Newtonian liquids.

A latest measurement is added to the border layer stream and heat transport by taking into consideration the thermal radiation. At high effective temperature, radiation consequence can be moderately considerable. Various processes in manufacturing areas occur at high temperature and facts of radiation heat transport becomes extremely significant in electrical power production, astrophysical streams, solar power technology, nuclear plants, gas turbines and various propulsion devices or aircraft and other manufacturing areas. Cogley et al., [23] showed that in the optically lean boundary, the liquid does not attract it is possessed emitted radiation but the liquid does suck up radiation emitted by the boundaries. Kim and Fedorov [24] moderated the case of mixed convection stream of a micropolar liquid past a semi-infinite, steadily stirring porous laminate with varying suction flow normal to the laminate in the occurrence of thermal radiation. The transient free convection interface with thermal radiation of an absorbing emitting liquid besides moving vertical leaky laminate was navigated by Makinde [25]. Ibrahim et al., [26] explained the case of mixed convection stream of a micropolar liquid past a semi infinite, steady moving porous plate with changing suction flow regular to the laminate in occurrence of thermal radiation and viscous dissipation. Rahman and Sattar [27] derived passing convective heat transport stream of a micropolar liquid past a constantly moving vertical porous laminate with time reliant suction in the occurrence of radiation.

Most of the valid time manufacturing processes occupy heat and mass transport. Heat or mass flux ought to be isolated, added or moved from one stream procedure to a further. This is a foremost task during any valid time manufacturing industries such as fuel industries, oceanic manufacturing, pharmaceutical, nuclear up and down processes, and distillation columns etc. The improvement of cooling or heating in manufacturing procedure creates economy in energy, raises thermal score, reduces process time and helps to elongate the operational life of the tools. Consequently, there has been a considerable stipulate for the inventive technologies that will assist in the heat and mass transport fluxes. The heat and mass transport on an elongating/shrinking sheet becomes more attractive when the heat flux and mass flux circumstances at the border are taken into consideration. In heat transport manufacturing, the heat flux occurrence plays a crucial position in controlling the rate of heat transport. In several realistic situations transpire in which the hot plane is subject to an invariable heat flux instead of being at a prescribed temperature. Dutta *et al.*, [28] primary investigated the effect of uniform heat flux on the temperature field in case of stream due to elongating sheet. After that, many researchers measured uniform or non- uniform heat flux at the border for elongating sheet stream [29-31]. The MHD stream towards a permeable plane with

prescribed wall heat flux was measured by Ishak *et al.*, [32]. Mandal and Mukhopadhyay [33] reported the mutual consequences of porous medium and heat flux on border layer stream and heat transport due to a sheet elongated with exponential flow. Ganesan and Palani [34] offered a numerical solution of the transient free convection MHD stream of an incompressible viscous liquid past a semi infinite inclined laminate with variable surface heat and mass flux.

Thermophoresis is an admirable trend by which tiny sized particles suspended in a non-isothermal gas acquire a flow relative to the gas in the path of declining temperature. The flow acquired by the particles is called thermophoretic flow and the force skilled by the pendant particles due to the temperature rise is known as thermophoretic force. Goren [38] was the initial to study the character of thermophoresis in laminar stream of a viscous incompressible liquid. He used the classical problem of stream over a flat laminate to estimate the deposition rates and showed that considerable changes in surface deposition can be obtained by increasing the variation between the plane and free stream temperature. Thermophoretic deposition of radioactive particles is measured to be one of the significant factors causing accidents in nuclear reactors. Epstein et al., [39] investigated the thermophoretic transport of tiny particles through a free convection border layer bordering to a cold, vertical deposition plane in a viscous incompressible liquid. Garg and Jayaraj [40] studied the thermophoretic transport of tiny particles in forced convection stream over an inclined plate. Opiolka et al., [41] analyzed the mutual consequences of electrophoresis and thermophoresis on particle evidence onto flat plane. The consequence of plane mass transport on mixed convection stream past a heated vertical flat permeable plate with thermophoresis was studied by Selim et al., [42]. Wang [43] discussed the mutual consequences of inertia and thermophoresis on particle deposition onto a wafer with wavy plane. Thermophoresis causes tiny particles to deposition cold surfaces. Alam et al., [44] examined the consequences of variable suction and thermophoresis on steady MHD mutual free-forced convective heat and mass transport stream over a semi-infinite permeable inclined laminate in the existence of thermal radiation. Duwairi and Damseh [45] developed the consequences of thermophoresis particle deposition on mixed convection from vertical surfaces surrounded in saturated porous medium. Pakravan and Yaghoubi [46] theoretically proved that the mutual thermophoresis, Brownian movement and Dufour consequences on natural convection of nanoliquids. Mehdi and Hosseinalipour [44] examined particle movement in nanoliquids considering thermophoresis and its consequence on convective heat transport. Lately Anbuchezhian et al., [45] have derived thermophoresis and Brownian movement consequences on border layer stream of nanoliquid in the occurrence of thermal stratification due to solar energy. To our awareness, there are no published results that include the consequences of thermal radiation and viscous dissipation on MHD mixed convection stream of micropolar liquid in the occurrence of thermophoresis.

Most of earlier works are not deliberated heat and mass transport MHD free convective stream of micropolar liquid through a porous medium with heat and mass fluxes in the occurrence of the thermophoresis. Consequently, in the present work, we have performed a numerical investigation on the mutual consequences of thermal radiation and thermophoresis on steady Magnetohydrodynamic free convective heat and mass transport stream of a micropolar liquid past a past a vertical porous laminate with heat and mass flux border conditions.

## 2. Mathematical Analysis

Consider a 2D steady MHD free convective stream of viscous incompressible electrically conducting liquid past a semi-infinite permeable inclined smooth laminate; while a magnetic field of uniform strength  $B_0$  is applied in the *y*-direction which is normal to the stream direction (see Figure 1). Liquid suction is imposed at the laminate plane and the suction whole size is taken to be constant.

The temperature of the plane is supposed consistent at  $T_{\rm w}$  which is higher than the ambient temperature  $T_{\infty}$ . The Rosseland estimate is used to illustrate the radioactive heat flux in the x-direction which is considered negligible in assessment to the y-direction. The consequences of thermophoresis are being taken into account to assist in the thoughtful of the mass deposition difference on the plane. Under the above assumptions, the leading equations for this problem can be written as:

(i) Continuity:

$$\frac{\partial u}{\partial x} + \frac{\partial u}{\partial y} = 0 \tag{1}$$

(ii) Momentum:

$$u\frac{\partial u}{\partial x} + v\frac{\partial u}{\partial y} = v_a \frac{\partial^2 u}{\partial y^2} + \frac{S}{\rho} \frac{\partial N}{\partial y} + g\beta_T 2(T - T_{\infty}) + g\beta_C (C - C_{\infty}) - \frac{\sigma B_0^2 u}{\rho} - \frac{v_a}{K'} (u - U_{\infty}) - \frac{b}{K'} (u - U_{\infty})^2$$
 (2)

(iii) Angular momentum:

$$u\frac{\partial N}{\partial x} + v\frac{\partial N}{\partial y} = \frac{v_s}{\rho j}\frac{\partial^2 N}{\partial y^2} - \frac{S}{\rho j}\left(2N + \frac{\partial u}{\partial y}\right) = 0$$
(3)

(vi) Energy:

$$u\frac{\partial T}{\partial x} + v\frac{\partial T}{\partial y} = \frac{k}{\rho C_n}\frac{\partial^2 T}{\partial y^2} - \frac{1}{\rho C_n}\frac{\partial q_r}{\partial y}$$
(4)

(v) Concentration:

$$u\frac{\partial C}{\partial x} + v\frac{\partial C}{\partial y} = D_m \frac{\partial^2 C}{\partial y^2} - \frac{\partial}{\partial y}(V_T C)$$
(5)

where u and v are the flow apparatus in the x, y directions,  $v_a = (\mu + s)/\rho$  is the noticeable kinematic viscosity, g is the acceleration due to gravity, T is the temperature of the liquid in the border layer, g is the acceleration due to gravity,  $\beta$  is the volumetric coefficient of thermal expansion,  $\beta_T$  and  $\beta_C$  are the coefficient of thermal and volumetric expansions, correspondingly,  $v_s = (\mu + s/2)j$  (see Rees and Bassom [46]) is the microrotation viscosity or spin-gradient viscosity, j is the micro-inertia density, T is the temperature of thermal border layer liquid, T0 is the concentration of the liquid in the border layer, T1 is the temperature far away from the laminate, T2 is the concentration of the solute far away from the laminate, T3 is the electrical conductivity, T4 is the magnetic induction, T5 is the liquid thermal conductivity, T6 is the liquid density, T7 is the specific heat at constant pressure, T8 is the radiative heat flux in the T3 is the radiative heat flux in the T4 is the radiative heat flux in the T5 is the radiative heat flux in the T5 is the radiative heat flux in the T6 is the radiative heat flux in the T6 is the radiative heat flux in the T8 is the radiative heat flux in the T9 is the radiative heat

direction,  $\mu$  is the dynamic viscosity, D is the molecular diffusivity of the species concentration and  $V_T$  is the thermophoretic flow.

The border conditions for the sculpt are as follows

$$u = 0, \ v = \pm v_w(x), \ N = -n\frac{\partial u}{\partial y}, \ \frac{\partial T}{\partial y} = -\frac{q_m}{k}, \ \frac{\partial C}{\partial y} = -\frac{m}{D_m} \ at \ y = 0$$

$$u \to U_\infty, \ N \to 0, \ T \to T_\infty, \ C \to C_\infty \ \text{as } y \to \infty$$
(6)

where  $U_0$  is the uniform laminate flow and  $v_w(x)$  represents liquid suction/injection on the porous plane. The transpiration function variable  $v_w(x)$  of order  $x^{-1/2}$  1/2 is considered, while  $v_w=0$  corresponds to an impermeable laminate. When microrotation constraint n=0 we obtain N=0 which represents no-spin situation i.e., the microelements in a concentrated particle stream-close to the wall are not able to spin as assured by Jena and Mathur [47]. The case n=0.5 represents diminishing of the anti-symmetric part of the stress tensor and represents weak concentration. For this case Ahmadi [8] optional that in a fine particle suspension the particle rotate is equal to the liquid flow at the wall. The case consequent to n=1.0 be representative of turbulent border layer streams [48]. In Eq. (8), the last two circumstances represent non-uniform heat and mass fluxes at the surface of the laminate.

By means of the Rosseland estimate, the radiative heat flux in the y' direction is given by [49]

$$q_r = -\frac{4\sigma_1}{3k_1} \frac{\partial T^4}{\partial Y} \tag{7}$$

where  $\sigma_1$  is the Stefan-Boltzmann invariable and  $k_1$  is the mean absorption coefficient.

Presumptuous that the temperature differences surrounded by the stream are adequately tiny so that  $T^4$  can be extended in Taylor series about the free stream temperature  $T_\infty$  to yield

$$T^4 \cong 4T_\infty^3 T - 3T_\infty^4 \tag{8}$$

where the higher-order terms of the expansion are ignored.

By using Eq. (6) and Eq. (7), Eq. (4) gives

$$u\frac{\partial T}{\partial x} + v\frac{\partial T}{\partial y} = \frac{k_e}{\rho c_p} \frac{\partial^2 T}{\partial y^2} - \frac{16\sigma_1 T_{\infty}^3}{3\rho c_p k_1} \frac{\partial^2 T}{\partial y^2}$$
(9)

Now the thermophoretic flow  $V_T$ , which appears in the Eq. (4) can be written as [35]:

$$V_T = -kv \frac{\nabla T}{T_{ref}} = \frac{-kv}{T_{ref}} \frac{\partial T}{\partial y} \tag{10}$$

where  $T_{ref}$  is an orientation temperature and k is the thermophoretic coefficient with variety of value from 0.2 to 1.2 as indicated by Batchelor and Chen [36] and is defined from the hypothesis of Talbot et al., [35] by

$$k = \frac{2Cs\left(\lambda_{g} / \lambda_{p} + C_{t}K_{n}\right)\left[1 + K_{n}\left(C_{1} + C_{2}e^{-C_{3}/K_{n}}\right)\right]}{\left(1 + 3C_{m}K_{n}\right)\left(1 + 2\lambda_{g} / \lambda_{p} + 2C_{t}K_{n}\right)}$$
(11)

where  $C_1$ ,  $C_2$ ,  $C_3$ ,  $C_m$ ,  $C_s$ ,  $C_t$  are constants,  $\lambda_g$  and  $\lambda_p$  are the thermal conductivities of the liquid and diffused particles correspondingly and  $K_n$  is the Knudsen number.

A thermophoretic constraint  $\tau$  can be defined as follows [35]:

$$\tau = \frac{-k\left(T_{w} - T_{\infty}\right)}{T_{w}} \tag{12}$$

Characteristic values of  $\tau$  are 0.01, 0.05 and 0.1 consequent to estimated values of  $-k\left(T_w-T_\infty\right)$  equal to 3K, 15K and 30 K for an indication temperature of  $T_r=300K$ .

## 3. Similarity Transformation

The solutions of the leading equations are obtained by introducing the subsequent nondimensional variables:

$$\eta = \left(\frac{U_{\infty}}{2v_{a}x}\right)^{\frac{1}{2}} y, \quad u = U_{0} f'(\eta), \quad \theta(\eta) = \frac{T - T_{\infty}}{Q/k} \sqrt{\frac{U_{\infty}}{2v_{a}x}}, \quad \phi(\eta) = \frac{C - C_{\infty}}{m/D_{m}} \sqrt{\frac{U_{\infty}}{2v_{a}x}}, \\
\psi = \left(2v_{a}U_{\infty}x\right)^{\frac{1}{2}} f(\eta), \quad v = -\sqrt{\frac{2v_{a}U_{\infty}}{x}} \left[f(\eta) - \eta f'(\eta)\right], \quad N = \left(\frac{U_{\infty}^{3}}{2v_{a}x}\right)^{\frac{1}{2}} g(\eta)$$
(13)

If the dimensional stream function  $\psi(x, y)$  then  $u = \frac{\partial \psi}{\partial y}$  and  $u = -\frac{\partial \psi}{\partial x}$ .

The continuity equation is involuntarily fulfilled and the scheme of Eq. (2), Eq. (3), Eq. (5) and Eq. (9) becomes:

$$f''' + ff'' + Kg' + Gr\theta + Gc\phi - Mf' - 2\lambda(f'-1) - Fs(f'-1)^{2} = 0$$
(14)

$$G_2g'' - 2G_1(2g + f'') + f'g + fg' = 0$$
(15)

$$(3R+4)\theta'' + 3R \operatorname{Pr} f \theta' + 3R \operatorname{Pr} f' \theta = 0$$
(16)

$$\phi'' + Sc(f - \tau\theta')\phi' - Sc\tau\theta''\phi = 0$$
(17)

The primes indicate differentiation with respect to  $\eta$ ,  $M=\frac{\sigma B_0^2 2x}{\rho U_\infty}$  is the is the magnetic field constraint,  $Gr=g\beta_T\sqrt{\frac{V_a(2x)^3}{U_\infty^5}}\frac{Q}{k}$  is the local thermal Grashof number,  $Gc=g\beta_c\sqrt{\frac{V_a(2x)^3}{U_\infty^5}}\frac{m}{D_m}$  is the local solute Grashof number,  $K=\frac{s}{\rho v_a}$  is the coupling constraint,  $\lambda=\frac{1}{Da}$  is the Darcy constraint, Da0 = is the modified Darcy number,  $Fs=\frac{bx}{K}$  is the modified Forchheimer number,  $G_1=\frac{sx}{\rho jU_\infty}$  is the vortex viscosity constraint,  $G_2=\frac{v_s}{\rho jv_a}$  is the spin gradient viscosity constraint,  $G=\frac{G_1U_0}{2vx}$  is the micro-rotation constraint,  $G=\frac{\rho vc_p}{k}$  is the Prandtl number,  $G=\frac{kk_e}{4\sigma_s T_\infty^3}$  is the thermal radiation constraint,  $G=\frac{v}{D_\infty}$  is the Schmidt number constraint.

The transformed border conditions (6) are given by

$$f(0) = \pm f_{w}, \ f'(0) = 0, \ g(0) = 0, \ \theta(0) = -1, \ \phi(0) = -1$$

$$f(\infty) = 0, \ g(\infty) = 0, \ \theta(\infty) = 0, \ \phi(\infty) = 0$$
(18)

Where  $f_w = -v_w(x)\sqrt{\frac{2x}{gU_0}}$  is the permeability of the porous plane which is positive for suction and negative for injection.

The substantial quantities of awareness are the local friction factor, the wall heat transport coefficient (or the local Nusselt number) and the wall deposition flux (or the local Stanton number) which are distinct as correspondingly where the skin friction  $C_f$ , the heat transport  $q_{\scriptscriptstyle W}(x)$  and the mass transport  $Sh_{\scriptscriptstyle Y}$  from the wall are given by

$$C_f \operatorname{Re}_x^{-1/2} = \frac{\tau_w}{(1/2)\rho U_o^2} = 2f''(0), \ \tau_w = \mu \left(\frac{du}{dy}\right)_{y=0}$$
 (19)

The equation defining the laminate couple stress is

$$M_{w} = v_{s} \left( \frac{\partial N}{\partial y} \right)_{y=0} \tag{20}$$

The dimensionless couple stress is defined by

$$M_{s} = \frac{M_{w}}{1/2 \rho v_{a} U_{\infty}} = \frac{G_{2} K}{G_{1}} g'(0)$$
 (21)

Thus, the local couple stress in the border layer is relative to g'(0).

From the temperature field, we can study the rate of heat transport which is given by

$$Nu_{x}\operatorname{Re}_{x}^{-1/2}\left(\frac{3R}{3R+4}\right) = \frac{q_{w}(x)}{\lambda\left(T_{w} - T_{\infty}\right)} = -\frac{1}{2}\theta'(0); q_{w}(x) = -k\left(\frac{\partial T}{\partial y}\right)_{y=0} - \frac{4\sigma_{1}}{3k_{1}}\left(\frac{\partial T^{4}}{\partial y}\right)_{y=0}$$
(22)

From the concentration field, we can study the rate of mass transport which is given by

$$Sh_x St \operatorname{Re}_x^{-1/2} = -\frac{J_s}{U_0 C_\infty}; J_s = -D\left(\frac{\partial C}{\partial y}\right)_{y=0} = -\phi'(0)$$
(23)

where  $\operatorname{Re}_{x} = U_{0}x/v$  the local Reynolds number.

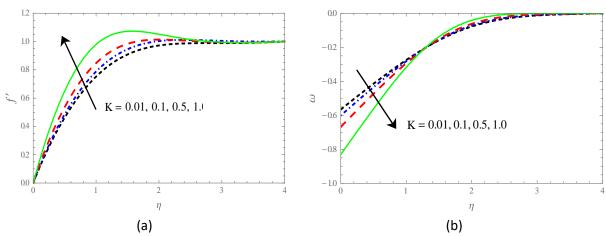
## 4. Method of Solution

The structure of ordinary differential Eq. (14) to Eq. (17) subject to the border surroundings (18) are solved numerically with Runge – Kutta fourth-order with shooting iteration procedure. A step size of  $\Delta \eta = 0.01$  was selected to be satisfactory for a convergence standard of  $10^{-6}$  in all belongings. The results are presented graphically in Figure 1 to Figure 12 and conclusions are drained for stream field and other substantial quantities of attention that have considerable consequences.

### 5. Results and Discussion

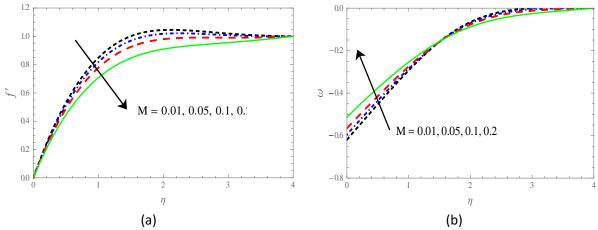
Eq. (11) to Eq. (13) comprise extremely non-linear coupled border value problem of third and second order. Thus, we have used the shooting iteration procedure with Runge–Kutta fourth-order integration algorithm. For numerical results we measured the non dimensional constraint ideals as M=1.0, K=0.01, G=0.01, G=0.01,

For dissimilar values of coupling invariable K on the flow and microrotation profiles are obtained in Figure 1(a) and Figure 1(b). It is established that the liquid flow amplifies when the coupling constant is enlarged (See Figure 1(a)). The results also show that the microrotation declines near the porous laminate and contradictory trends far away from the laminate as coupling constant amplifies.



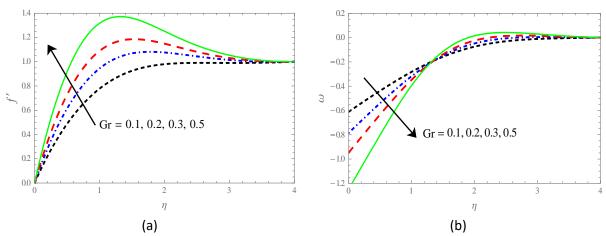
**Fig. 1.** (a) Consequences of K on flow distribution  $f'(\eta)$ , (b) Consequences of K on microrotation distribution  $\omega(\eta)$ 

The consequences of the magnetic constraint M on the flow and microrotation profiles are publicized in Figure 2(a) and Figure 2(b), correspondingly. It is obviously seen From Figure 2(a) that the flow profiles dwindle with mounting values of magnetic constraint M. It is also seen Figure 2(b) that the microrotation amplifies near the porous plate and then declines far away from the laminate as magnetic constraint M raises.

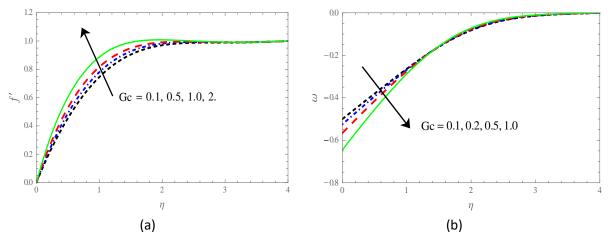


**Fig. 2.** (a) Consequences of M on flow distribution  $f'(\eta)$ , (b) Effect of K on microrotation distribution  $\omega(\eta)$ 

The liquid flow and microrotation profiles for dissimilar values of thermal Grashof number *Gr* and solutal Grashof number *Gc* are exhibited in Figure 3 and Figure 4, correspondingly. It is observed that mounting in *Gr* or *Gc* leads to escalating in the values of flow, whereas microrotation dwindles near the porous laminate and then amplifies far away from the laminate.

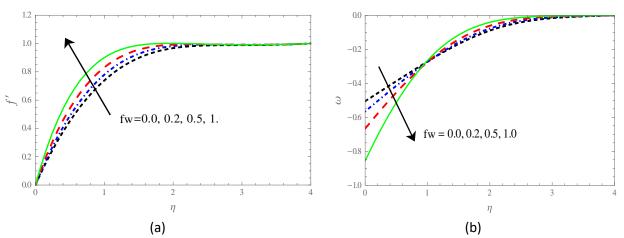


**Fig. 3.** (a) Consequences of Gr on flow distribution  $f'(\eta)$ , (b) Consequences of Gr on microrotation distribution  $g(\eta)$ 



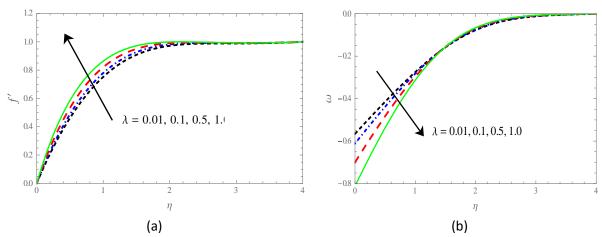
**Fig. 4.** (a) Consequences of Gc on flow distribution  $f'(\eta)$ , (b) Consequences of Gc on microrotation distribution  $\omega(\eta)$ 

For dissimilar values of suction constraint fw on the flow, microrotation and concentration profiles are obtained in Figure 5(a) to Figure 5(c). It is observed that the flow profiles amplify with the raise of suction constraint fw representative the usual fact that suction stabilizes the border layer expansion (see Figure 5(a)). The results also show that the microrotation profile dwindles near the porous laminate and contradictory trends far away from the porous laminate as suction constraint fw amplifies where viscosity is overriding. From Figure 5(c), it is scrutinized that the concentration profiles diminish with enlarge of the suction constraint fw.



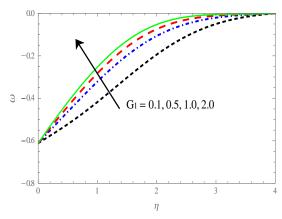
**Fig. 5.** (a) Consequences of  $f_W$  on flow distribution  $f'(\eta)$ , (b) Consequences of  $f_W$  on Microrotation distribution  $\omega(\eta)$ 

The consequence of the local Darcy constraint  $\lambda$  on the flow field is publicized in the Figure 6(a). From this outline we observed that flow profiles decline with the raise of  $\lambda$ . Darcy number is the quantity of the porosity of the medium, as the porosity of the medium enlarges, the value of Da raises and hence  $\lambda$  diminishes. For large porosity of the medium liquid gets more space to stream, subsequently liquid flow amplifies. Figure 6(b) illustrates that microrotation amplifies with the raise of local Darcy constraint  $\lambda$ .



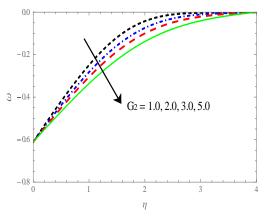
**Fig. 6.** (a) Consequences of  $\lambda$  on Flow distribution  $f'(\eta)$ , (b) Consequences of  $\lambda$  on microrotation distribution  $\omega(\eta)$ 

For different values of the vortex viscosity constraint  $G_1$  on the microrotation distribution plotted in Figure 7. It is observed from figure that the escalating values of the vortex viscosity constraint  $G_{1}$ , the microrotation distribution boost-up.



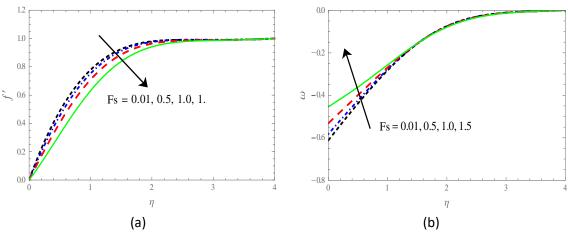
**Fig. 7.** Consequences of  $G_{\rm I}$  on microrotation distribution  $\omega(\eta)$ 

The influences of the spin-gradient viscosity constraint  $G_2$  on the microrotation distribution are painted in Figure 8. From this outline, we observed that microrotation distribution decline with the mounting values of spin-gradient viscosity constraint  $G_2$ .



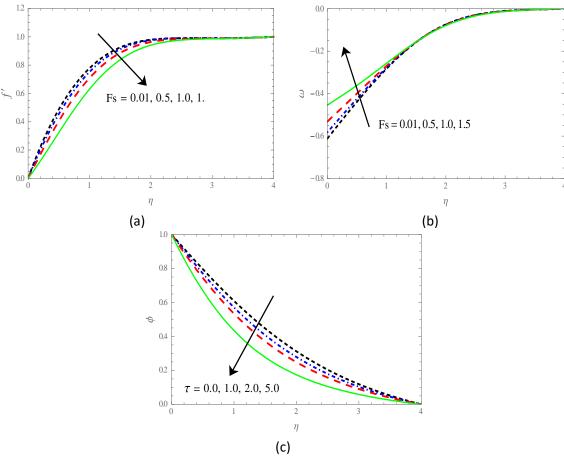
**Fig. 8.** Consequences of  $G_2$  on microrotation distribution  $\omega(\eta)$ 

Figure 9(a) and Figure 9(b) correspondingly, show the flow and microrotation, profiles for different values of customized Forchheimer number Fs. From Figure 9(a), we see that flow diminishes with the amplify of Fs. Figure 9(b) shows the effect of in the microrotation profiles. From this figure, we scrutinize Fs as escalating effect on the microrotation profiles.



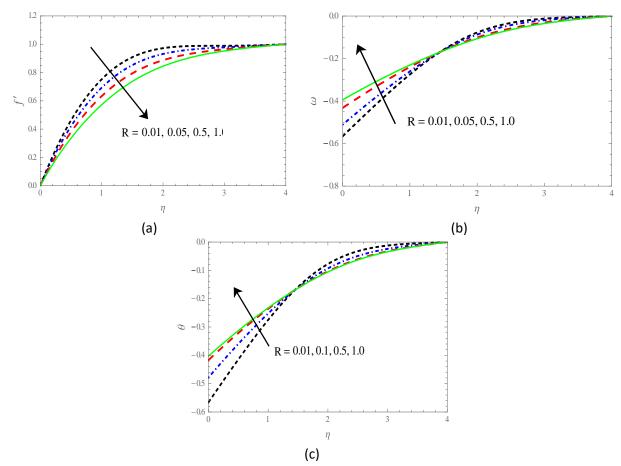
**Fig. 9.** (a) Consequences of Fs on flow distribution  $f'(\eta)$ , (b) Consequences of Fs on Microrotation distribution  $\omega(\eta)$ 

For a variety of values of thermophoretic constraint  $\tau$  on the flow, microrotation and concentration profiles are plotted in Figure 10(a) to Figure 10(c). It can be seen that the liquid flow declines with the raise of thermophoretic parameter  $\tau$ . The results also show that the microrotation profiles raises near the porous laminate and contradictory trends far away from the laminate as thermophoretic constraint enlarges. From Figure 10(c), we scrutinized that the concentration profiles diminish with escalating values of the thermophoretic constraint  $\tau$ .



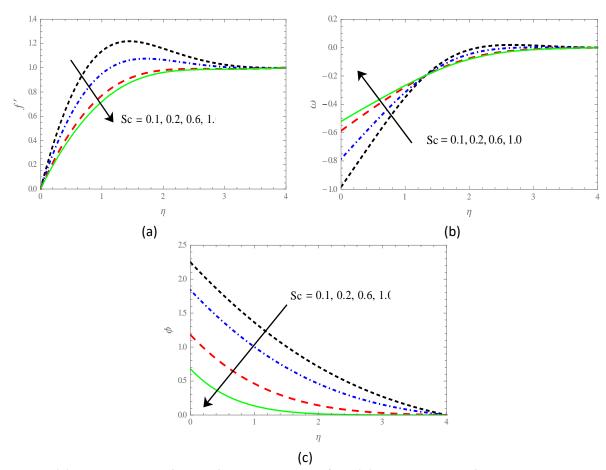
**Fig. 10.** (a) Consequences of  $\tau$  on flow distribution  $f'(\eta)$ , (b) Consequences of  $\tau$  on microrotation distribution  $\omega(\eta)$ , (c) Consequences of  $\tau$  concentration distribution  $\phi(\eta)$ 

For dissimilar values of thermal radiation constraint *R*, the flow, microrotation and temperature profiles are plotted in Figure 11(a) to Figure 11(c). It is evident that the liquid flow distribution transversely the border layer diminishes with the mounting values of radiation constraint *R*. The results also show that both the microrotation and temperature on the vertical laminate amplifies near the porous laminate and contradictory trends far away from the laminate as escalating radiation constraint.



**Fig. 11.** (a) Consequences of R on flow distribution  $f'(\eta)$ , (b) Consequences of R on microrotation distribution  $\omega(\eta)$ , (c) Consequences of R on temperature distribution  $\theta(\eta)$ 

The consequences of a variety of values of Schmidt number *Sc* on the flow, microrotation and concentration profiles are accessible in Figure 12(a) to Figure 12(c). It is publicized that the liquid flow transversely the border layer diminishes with escalating values of *Sc*. The results also, it is emerged that the microrotation rises near the porous laminate and contradictory trends far away from the laminate as *Sc* enlarges. From Figure 12(c), we scrutinized that the concentration profiles decline with escalating values of the Schmidt number *Sc*.



**Fig. 12.** (a) Consequences of Sc on flow distribution  $f'(\eta)$ , (b) Consequences of Sc on microrotation distribution  $g(\eta)$ , (c) Consequences Sc of on concentration distribution  $\phi(\eta)$ 

The numerical values of the skin-friction factor, local Nusselt number and local Stanton number are tabulated in Table 1 for dissimilar values of magnetic constraint M and coupling constant K, local Darcy constraint  $\lambda$ , modified Forchheimer number Fs, radiation constraint R and thermophoretic constraint  $\tau$ . Scrutiny of the tabular data Table 1 shows that magnetic constraint, modified Forchheimer number, radiation constraint R and thermophoretic constraint  $\tau$ , increase the values of the skin-friction factor, whereas reverse trend is seen by escalating the values of K,  $\lambda$ . It is also observed that the couple stress coefficient enlarge with escalating values of K,  $\lambda$  while contradictory consequence is seen with escalating of M, Fs, R,  $\tau$ . Additional, it is clear that the local Nusselt number amplifies with raise M, Fs and  $\tau$  while reverse trend is seen by escalating values of K,  $\lambda$  and R. Finally, the consequence of escalating the value of M, Fs,  $\tau$  has the tendency to amplify local Stanton number but the other constraints like K,  $\lambda$  and R have the effect of declining  $-\phi'(0)$ .

**Table 1** Numerical standards of friction factor, couple stress coefficient, local Nusselt number and local Sherwood number for dissimilar constraints  $\lambda = 0.01$ , Fs = 0.01, M=0.1, K=0.01, Gr=0.1, Gc=0.5,  $G_1=1.0$ ,  $G_2=2.0$ , Fr=0.71,  $G_2=0.1$ ,  $G_2$ 

М	К	λ	Fs	R	τ	$C_f$	$C_w$	$Nu_x$	$Sh_x$
0.1	-	-	-	-	-	-1.26648	0.408349	0.924601	0.750603
0.2						-1.24389	0.384579	0.928207	0.751901
0.5						-1.22389	0.336181	0.937051	0.755149
	0.1	-	-	-	-	-1.42553	0.424223	0.776691	0.540305
	0.5					-1.46607	0.511458	0.759985	0.535309
	1.0					-1.53191	0.679302	0.732618	0.526823
	-	0.1	-	-	-	-1.12245	0.408349	0.984603	0.899218
		0.5				-1.12826	0.449561	0.984031	0.898127
		1.0				-1.13418	0.493023	0.983447	0.898031
	-	-	0.1	-	-	-1.41585	0.393671	0.781246	0.541941
			0.5			-1.40742	0.324814	0.787479	0.543919
			1.0			-1.39362	0.227774	0.797479	0.547239
	-	-	-	0.1	-	-1.41751	0.408349	0.779991	0.541531
				0.5		-1.39024	0.360379	0.584137	0.499207
				1.0		-1.38516	0.348689	0.500063	0.481113
	-	-	-	-	2.0	-1.49978	0.122987	0.508741	0.275812
					3.0	-1.48151	0.119315	0.528991	0.184856
					5.0	-1.46029	0.113910	0.554104	0.095341

#### 6. Conclusions

The mutual consequences of thermal radiation and thermophorises on MHD free convection heat and mass transport stream of a micropolar liquid past a vertical porous laminate during a porous medium with heat and mass fluxes are investigated. The consequential partial differential equations, describing the problem are transformed into ordinary differential equations by using similarity transformations. These equations are more expediently solved numerically by Runge-Kutta fourth order with shooting iteration procedure for the calculation of stream, heat and mass transport description, the friction factor, the couple stress, heat and mass transport coefficients at vertical laminate in a porous medium for a variety of values of magnetic constraint, local Darcy constraint, modified Forchheimer number, radiation constraint, and thermophoretic constraint.

The foremost outcomes of this study can be outlined as:

- i. The flow diminishes with raise in magnetic constraint M, modified Forchheimer number Fs, thermophoresis constraint  $\tau$ , radiation constraint R and Schmidt number Sc but raises with enlarge in coupling constant K, suction constraint fw, local Darcy constraint  $\lambda$ .
- ii. The microrotation raise near the surface and then decline far away from the surface with amplify in magnetic constraint M, modified Forchheimer number Fs, thermophoresis constraint  $\tau$ , radiation constraint R and Schmidt number Sc but reverse trends observed for the coupling constant K, suction constraint fw, local Darcy constraint  $\lambda$ .
- iii. The Temperature rises near the surface and then declines way from the surface with amplify in radiation constraint *R*.
- iv. The concentration dwindles with enlarge in suction constraint fw, thermophoresis constraint  $\tau$  and Schmidt number Sc.
- v. The friction factor coefficient amplifies with raise in M, Fs, R and  $\tau$  and decline for the values of K and  $\lambda$  but reverse trends observed for the couple stress coefficient.

vi. Both the rate of heat and mass transport coefficients dwindles with raise in K,  $\lambda$  and R and they amplifies with in M and Fs.

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## References

- [1] Eringen, A. Cemal. "Theory of micropolar fluids." *Journal of Mathematics and Mechanics* 16 (1966): 1-18. https://doi.org/10.1512/iumj.1967.16.16001
- [2] Eringen, A. Cemal. "Theory of thermomicrofluids." *Journal of Mathematical Analysis and Applications* 38, no. 2 (1972): 480-496. <a href="https://doi.org/10.1016/0022-247X(72)90106-0">https://doi.org/10.1016/0022-247X(72)90106-0</a>
- [3] Eringen, A. Cemal. Microcontinuum field theories: II. Fluent media. Vol. 2. Springer Science & Business Media, 2001.
- [4] Lukaszewicz, Grzegorz. *Micropolar fluids: theory and applications*. Springer Science & Business Media, 1999. https://doi.org/10.1007/978-1-4612-0641-5 5
- [5] Chiu, C-P., and H-M. Chou. "Free convection in the boundary layer flow of a micropolar fluid along a vertical wavy surface." *Acta Mechanica* 101, no. 1 (1993): 161-174. <a href="https://doi.org/10.1007/BF01175604">https://doi.org/10.1007/BF01175604</a>
- [6] Hassanien, I. A., and R. S. R. Gorla. "Heat transfer to a micropolar fluid from a non-isothermal stretching sheet with suction and blowing." *Acta Mechanica* 84, no. 1 (1990): 191-199. https://doi.org/10.1007/BF01176097
- [7] Gorla, R. S. R. "Mixed convection boundary layer flow of a micropolar fluid on a horizontal plate." *Acta Mechanica* 108, no. 1 (1995): 101-109. <a href="https://doi.org/10.1007/BF01177331">https://doi.org/10.1007/BF01177331</a>
- [8] Ahmadi, Goodarz. "Self-similar solution of imcompressible micropolar boundary layer flow over a semi-infinite plate." *International Journal of Engineering Science* 14, no. 7 (1976): 639-646. <a href="https://doi.org/10.1016/0020-7225(76)90006-9">https://doi.org/10.1016/0020-7225(76)90006-9</a>
- [9] Gorla, Rama Subba Reddy, Richard Pender, and John Eppich. "Heat transfer in micropolar boundary layer flow over a flat plate." *International Journal of Engineering Science* 21, no. 7 (1983): 791-798. <a href="https://doi.org/10.1016/0020-7225(83)90062-9">https://doi.org/10.1016/0020-7225(83)90062-9</a>
- [10] Soundalgekar, V. M., and H. S. Takhar. "Flow of micropolar fluid past a continuously moving plate." *International Journal of Engineering Science* 21, no. 8 (1983): 961-965. https://doi.org/10.1016/0020-7225(83)90072-1
- [11] Takhar, H. S., and V. M. Soundalgekar. "Flow and heat transfer of micropolar fluid past a porous plate." *Indian Journal of Pure and Applied Mathematics* 16, no. 5 (1985): 552-558.
- [12] Hassanien, I. A., and R. S. R. Gorla. "Heat transfer to a micropolar fluid from a non-isothermal stretching sheet with suction and blowing." *Acta Mechanica* 84, no. 1 (1990): 191-199. https://doi.org/10.1007/BF01176097
- [13] Takhar, Harmindar S., R. S. Agarwal, Rama Bhargava, and S. Jain. "Mixed convection flow of a micropolar fluid over a stretching sheet." *Heat and Mass Transfer* 34, no. 2 (1998): 213-219. https://doi.org/10.1007/s002310050252
- [14] Mansour, M. A., and R. S. R. Gorla. "Micropolar fluid flow past a continuously moving plate in the presence of magnetic field." *Applied Mechanics and Engineering* 4, no. 4 (1999): 663-672.
- [15] Mansour, M. A., A. A. Mohammadein, S. MM El-Kabeir, and Rama Subba Reddy Gorla. "Heat transfer from moving surfaces in a micropolar fluid." *Canadian Journal of Physics* 77, no. 6 (1999): 463-471. <a href="https://doi.org/10.1139/p99-046">https://doi.org/10.1139/p99-046</a>
- [16] Nayan, Asmahani, Nur Izzatie Farhana Ahmad Fauzan, Mohd Rijal Ilias, Shahida Farhan Zakaria, and Noor Hafizah Zainal Aznam. "Aligned Magnetohydrodynamics (MHD) Flow of Hybrid Nanofluid Over a Vertical Plate Through Porous Medium." *Journal of Advanced Research in Fluid Mechanics and Thermal Sciences* 92, no. 1 (2022): 51-64. https://doi.org/10.37934/arfmts.92.1.5164
- [17] Hanafi, Hajar, and Sharidan Shafie. "Unsteady Free Convection MHD Flow over a Vertical Cone in Porous Media with Variable Heat and Mass Flux in Presence of Chemical Reaction." *Journal of Advanced Research in Fluid Mechanics and Thermal Sciences* 92, no. 2 (2022): 1-12. <a href="https://doi.org/10.37934/arfmts.92.2.112">https://doi.org/10.37934/arfmts.92.2.112</a>
- [18] Sannad, Mohamed, Youcef Mehdi, Afaf Zaza, Youness El Hammami, Youssef Idihya, and Othmane Benkortbi. "A Numerical Simulation Under Milk Fouling in A Plate Heat Exchanger in The Presence of a Porous Medium." *Journal of Advanced Research in Fluid Mechanics and Thermal Sciences* 91, no. 1 (2022): 1-17. <a href="https://doi.org/10.37934/arfmts.91.1.117">https://doi.org/10.37934/arfmts.91.1.117</a>
- [19] Yang, Yue-Tzu, and Sae-Jan Wang. "Free convection heat transfer of non-Newtonian fluids over axisymmetric and two-dimensional bodies of arbitrary shape embedded in a fluid-saturated porous medium." *International Journal of Heat and Mass Transfer* 39, no. 1 (1996): 203-210. https://doi.org/10.1016/S0017-9310(96)85016-2

- [20] Rastogi, S. K., and D. Poulikakos. "Double-diffusion from a vertical surface in a porous region saturated with a non-Newtonian fluid." *International Journal of Heat and Mass Transfer* 38, no. 5 (1995): 935-946. https://doi.org/10.1016/0017-9310(94)00198-5
- [21] Kim, Youn J. "Heat and mass transfer in MHD micropolar flow over a vertical moving porous plate in a porous medium." *Transport in Porous Media* 56, no. 1 (2004): 17-37. <a href="https://doi.org/10.1023/B:TIPM.0000018420.72016.9d">https://doi.org/10.1023/B:TIPM.0000018420.72016.9d</a>
- [22] Reddy, T. Sankar, V. Ramachandra Prasad, P. Roja, and N. Bhaskar Reddy. "Radiation consequences on MHD mixed convection stream of a micropolar liquid past a semi-infinite moving porous plate in a porous medium with heat absorption." *International Journal of Applied Mathematics and Mechanics* 6, no. 18 (2010): 80-101.
- [23] Cogley, Allen C., Walter G. Vincent, and Scott E. Gilles. "Differential approximation for radiative transfer in a nongrey gas near equilibrium." *AIAA Journal* 6, no. 3 (1968): 551-553. https://doi.org/10.2514/3.4538
- [24] Kim, Youn J., and Andrei G. Fedorov. "Transient mixed radiative convection flow of a micropolar fluid past a moving, semi-infinite vertical porous plate." *International Journal of Heat and Mass Transfer* 46, no. 10 (2003): 1751-1758. https://doi.org/10.1016/S0017-9310(02)00481-7
- [25] Makinde, Oluwole D. "Free convection flow with thermal radiation and mass transfer past a moving vertical porous plate." *International Communications in Heat and Mass Transfer* 32, no. 10 (2005): 1411-1419. <a href="https://doi.org/10.1016/j.icheatmasstransfer.2005.07.005">https://doi.org/10.1016/j.icheatmasstransfer.2005.07.005</a>
- [26] Ibrahim, F. S., A. M. Elaiw, and A. A. Bakr. "Influence of viscous dissipation and radiation on unsteady MHD mixed convection flow of micropolar fluids." *Applied Mathematics & Information Sciences* 2, no. 2 (2008): 143-162.
- [27] Rahman, M. M., and M. A. Sattar. "Transient convective flow of micropolar fluid past a continuously moving vertical porous plate in the presence of radiation." *International Journal of Applied Mechanics and Engineering* 12, no. 2 (2007): 497-513.
- [28] Dutta, B. K., P. Roy, and A. S. Gupta. "Temperature field in flow over a stretching sheet with uniform heat flux." *International Communications in Heat and Mass Transfer* 12, no. 1 (1985): 89-94. <a href="https://doi.org/10.1016/0735-1933(85)90010-7">https://doi.org/10.1016/0735-1933(85)90010-7</a>
- [29] Elbashbeshy, Elsayed M. A. "Heat transfer over a stretching surface with variable surface heat flux." *Journal of Physics D: Applied Physics* 31, no. 16 (1998): 1951-1956. <a href="https://doi.org/10.1088/0022-3727/31/16/002">https://doi.org/10.1088/0022-3727/31/16/002</a>
- [30] Elbashbeshy, E. M. A., and M. A. Bazid. "The mixed convection along a vertical plate with variable surface heat flux embedded in porous medium." *Applied Mathematics and Computation* 125, no. 2-3 (2002): 317-324. https://doi.org/10.1016/S0096-3003(00)00134-X
- [31] Rahman, M. M., and Tamanna Sultana. "Radiative heat transfer flow of micropolar fluid with variable heat flux in a porous medium." *Nonlinear Analysis: Modelling and Control* 13, no. 1 (2008): 71-87. https://doi.org/10.15388/NA.2008.13.1.14590
- [32] Ishak, Anuar, Roslinda Nazar, and Ioan Pop. "Heat transfer over a stretching surface with variable heat flux in micropolar fluids." *Physics Letters A* 372, no. 5 (2008): 559-561. https://doi.org/10.1016/j.physleta.2007.08.003
- [33] Mandal, Iswar Chandra, and Swati Mukhopadhyay. "Heat transfer analysis for fluid flow over an exponentially stretching porous sheet with surface heat flux in porous medium." *Ain Shams Engineering Journal* 4, no. 1 (2013): 103-110. https://doi.org/10.1016/j.asej.2012.06.004
- [34] Ganesan, P., and G. Palani. "Finite difference analysis of unsteady natural convection MHD flow past an inclined plate with variable surface heat and mass flux." *International Journal of Heat and Mass Transfer* 47, no. 19-20 (2004): 4449-4457. <a href="https://doi.org/10.1016/j.ijheatmasstransfer.2004.04.034">https://doi.org/10.1016/j.ijheatmasstransfer.2004.04.034</a>
- [35] Talbot, L., R. K. Cheng, R. W. Schefer, and D. R. Willis. "Thermophoresis of particles in a heated boundary layer." Journal of Fluid Mechanics 101, no. 4 (1980): 737-758. https://doi.org/10.1017/S0022112080001905
- [36] Batchelor, G. K., and C. Shen. "Thermophoretic deposition of particles in gas flowing over cold surfaces." *Journal of Colloid and Interface Science* 107, no. 1 (1985): 21-37. <a href="https://doi.org/10.1016/0021-9797(85)90145-6">https://doi.org/10.1016/0021-9797(85)90145-6</a>
- [37] Mills, A. F., Hang Xu, and F. Ayazi. "The effect of wall suction and thermophoresis on aerosol particle deposition from a laminar boundary layer on a flat plate." *International Journal of Heat and Mass Transfer* 27, no. 7 (1984): 1110-1113. https://doi.org/10.1016/0017-9310(84)90127-3
- [38] Goren, Simon L. "Thermophoresis of aerosol particles in the laminar boundary layer on a flat plate." *Journal of Colloid and Interface Science* 61, no. 1 (1977): 77-85. https://doi.org/10.1016/0021-9797(77)90416-7
- [39] Epstein, Michael, G. M. Hauser, and R. E. Henry. "Thermophoretic deposition of particles in natural convection flow from a vertical plate." *Journal of Heat Transfer* 107, no. 2 (1985): 272-276. https://doi.org/10.1115/1.3247410
- [40] Garg, Vijay K., and S. Jayaraj. "Thermophoresis of aerosol particles in laminar flow over inclined plates." *International Journal of Heat and Mass Transfer* 31, no. 4 (1988): 875-890. <a href="https://doi.org/10.1016/0017-9310(88)90144-5">https://doi.org/10.1016/0017-9310(88)90144-5</a>

- [41] Opiolka, S., F. Schmidt, and H. Fissan. "Combined effects of electrophoresis and thermophoresis on particle deposition onto flat surfaces." *Journal of Aerosol Science* 25, no. 4 (1994): 665-671. <a href="https://doi.org/10.1016/0021-8502(94)90007-8">https://doi.org/10.1016/0021-8502(94)90007-8</a>
- [42] Selim, A., M. A. Hossain, and D. A. S. Rees. "The effect of surface mass transfer on mixed convection flow past a heated vertical flat permeable plate with thermophoresis." *International Journal of Thermal Sciences* 42, no. 10 (2003): 973-982. https://doi.org/10.1016/S1290-0729(03)00075-9
- [43] Wang, Chi-Chang. "Combined effects of inertia and thermophoresis on particle deposition onto a wafer with wavy surface." *International Journal of Heat and Mass Transfer* 49, no. 7-8 (2006): 1395-1402. https://doi.org/10.1016/j.ijheatmasstransfer.2005.09.036
- [44] Alam, M. S., M. M. Rahman, and M. A. Sattar. "Effects of variable suction and thermophoresis on steady MHD combined free-forced convective heat and mass transfer flow over a semi-infinite permeable inclined plate in the presence of thermal radiation." *International Journal of Thermal Sciences* 47, no. 6 (2008): 758-765. https://doi.org/10.1016/j.ijthermalsci.2007.06.006
- [45] Duwairi, H. M., and Rebhi A. Damseh. "Effect of thermophoresis particle deposition on mixed convection from vertical surfaces embedded in saturated porous medium." *International Journal of Numerical Methods for Heat & Fluid Flow* 18, no. 2 (2008): 202-216. https://doi.org/10.1108/09615530810846347
- [46] Pakravan, Hossein Ali, and Mahmood Yaghoubi. "Combined thermophoresis, Brownian motion and Dufour effects on natural convection of nanofluids." *International Journal of Thermal Sciences* 50, no. 3 (2011): 394-402. <a href="https://doi.org/10.1016/j.ijthermalsci.2010.03.007">https://doi.org/10.1016/j.ijthermalsci.2010.03.007</a>
- [47] Jena, S. Ko, and M. N. Mathur. "Similarity solutions for laminar free convection flow of a thermomicropolar fluid past a non-isothermal vertical flat plate." *International Journal of Engineering Science* 19, no. 11 (1981): 1431-1439. https://doi.org/10.1016/0020-7225(81)90040-9
- [48] Peddieson, J., and R. P. McNitt. "Boundary-layer theory for a micropolar fluid Recent." *Adv. Eng. Sci.* 5 (1970): 405-476.
- [49] Brewster, M. Quinn. Thermal radiative transfer and properties. John Wiley & Sons, 1992.