

Multiphase CFD Investigation on Convective Heat Transfer Enhancement for Turbulent Flow of Water-Al₂O₃ Nanofluid

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ARTICLE INFO	ABSTRACT
Article history: Received 14 August 2021 Received in revised form 10 September 2021 Accepted 11 September 2021 Available online 31 October 2021	Because of extraordinary heat transfer capability, nanofluids have become a potential interest in engineering sectors. Despite being a multiphase fluid, nanofluids were treated as single phase fluids in many previous studies and comparison between single and two phase models was drawn. Examining nanofluids capability to augment heat transfer is one of the keys to utilize them properly in the field of thermofluids. However, the optimal multiphase model to simulate nanofluids heat transfer enhancement is yet to be found out. In this study, the method of computational fluid dynamics has been used to simulate flow of water-Al2O3 nanofluid in a circular pipe in the purpose of identifying the best multiphase model to simulate heat transfer enhancement of nanofluids. Two multiphase models have been taken into account: Volume of Fluid and Mixture model. Three different volume fractions of nanoparticles in nanofluid have been tested for each of these models such as 1%,4% and 6% for highly turbulent flows where Reynolds number was ranged between 20000 to 80000. The standard k-ɛ turbulence model has been employed to model the flow of nanofluid with the mentioned multiphase models in the present study. The results have been carried out in forms of correlation between Re and Nu and have been compared with existing experimental results. The results showed that the heat transfer enhancement of nanofluid for cases with high particles present in the fluid and suggested that Mixture model is suitable for predicting convective heat transfer enhancement of nanofluid for cases with high particle concentration though the
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1. Introduction

A range of engineering instruments and systems operate depending on the mechanism of heat transfer and their basic working principle includes a fluid to transfer the heat from one part to another whose efficiency depends upon the heat transfer capability of the working fluid. The time was 1873 and it was the revolutionary idea of Maxwell to add solid particles to Heat Transfer Fluids (HTF) to increase their thermal conductivity [1]. While the addition of micrometer and millimeter sized solid particles was causing issues such as clogging, increased pressure drop and pipe erosion,

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some light was shed on this concept when S.U.S Choi and J. Eastman introduced nanoscale metallic particles and carbon nanotubes as nanoparticles where they conducted experiments with variety of fluids and found out the results to be satisfactory [2]. Since then, nanofluids are known for their improved heat transfer characteristics and have successfully proved their importance in the industrial atmosphere in terms of transferring heats. The key variable that controls the thermophysical properties and heat transfer capability of nanofluids is the nanoparticle volume concentration [3]. Nanoparticles are spherical solid particles those have a diameter of less than 100 nm such as Al₂O₃, CuO, TiO₂, Cu, Fe and carbon-based material such as carbon nanotubes (CNTs). Over past few years many studies have been conducted on the improved heat transfer behavior and on the thermophysical properties of nanofluid. While this is quite apparent that nanofluid is a multiphase fluid because of the presence of two different phases such as base fluid which is a liquid and nanoparticles which are solid, several studies have been carried out on nanofluids assuming them as single phase fluid. Even in some of the recent works, such as where the thermal and hydrodynamic behavior were examined using 2D CFD simulation, single phase model was depended upon [4]. Though in some cases these assumptions were proved convenient, but they caused several errors too.

A numerical study on laminar convective heat transfer of nanofluids in a circular tube under constant wall temperature was carried out using CFD approach where both single and two phase models were employed. The results displayed comparatively stronger cooperation of two phase model with experimental results than single phase model [5]. A different opinion was made when Saghir *et al.*, [6] carried out an experiment with the flow of nanofluids in a square cavity and compared the result of single and two phase models with experimental results. Their conclusion suggested that though multiphase model provides deep comprehension on the liquid and solid phase mixture but the single phase model predicts the heat transfer more accurately. This finding aligns with the outcome of another numerical investigation of single and multiphase model conducted by Esfandiary *et al.*, [7]. The simplicity of single phase model was acknowledged by Kakaç and Pramuanjaroenkij [8]. But taking slip velocity between nanoparticles and the base fluid they suggested that that the multiphase model provides a better view of nanofluids flow field.

In another recent research on forced convection of nanofluid, single and two phase models were examined. It was seen that two phase model result seems to be more convincing when compared to single phase when compared to experimental data [9]. Another contemporary study picked up that two phase model is more convincing in terms of predicting heat transfer though with the increase in particle concentration the two phase model seem to overestimate the heat transfer enhancement [10]. In a more recent study where single and multiphase models were employed for nanofluids convection at the entrance of a uniformly heated tube. It was picked up that two phase models tend to predict heat transfer parameters better than single phase model [11]. After that Safaei et al., [12] conducted a review of latest works on nanofluids mathematical modelling for simulation. Though they concluded that realistic results can be achieved by using temperature-dependent thermophysical properties of nanofluid in homogeneous model but vouched for better accuracy of two phase models. Subsequently, comparison of heat and mass transfer between single and two phase models was drawn via numerical study for nanofluid liquid film which was flowing downward a vertical channel. It was deduced that two phase model was more practical as it accounts for thermophoresis and Brownian effects [13]. Latterly, Ambreen et al., [14] carried out very comprehensive research on single phase and the multiphase models where they noticed that at low Reynolds number, single and multiphase models can precisely predict the thermal fields of diluted nanofluids but at denser concentration and higher Reynold number the results are overestimated. In

all these investigations, the main focus was to make comparison between single and multiphase models.

Now, there are two approaches of looking into a multiphase fluid flow. The first one is called the Euler-Langrange Approach which treats the fluid phase as a continuum by solving the momentum equations, but a large number of particles are tracked through the calculated flow field for solving the dispersed phase. It allows the dispersed phase to interact with the fluid phase by exchanging momentum, mass, and energy. In this model, there is a presumption. That is, the dispersed second phase takes up a small volume fraction, despite the fact that high mass loading is acceptable. During the calculation of fluid phase, the particle or droplet trajectories are computed individually at specified intervals.

The seccond one is known as Euler-Euler approach where the distinct phases are mathematically handled as interpenetrating continuum considering idea of phasic volume fraction since the volume of a phase cannot be filled by other phases. These volume fractions are believed to be continuous space and time functions with a mathematical total of one. Conservation equations for each phase are generated to obtain a set of equations with a similar structure for all phases. These equations are solved by supplying constitutive relations based on observations. There are three different Euler-Euler multiphase models available: the volume of fluid (VOF) model, the mixture model, and the Eulerian model among which Mixture model and VOF model has been used to simulate the flow of nanofluid in this study.

The VOF model is a surface tracking technique employed on a Eulerian mesh which is fixed. It has been designed for two or more fluids those are unable to form a homogenous mixture where point of interest is the interface betwen the fluids considered. The fluids in this model share a single set of momentum equations, and each fluids volume fraction in each computational cell is monitored across the domain.

For treating two or more phases (fluid or particulate) Mixture model is designed. The phases are considered as interpenetrating continua in the Euler-Euler technique. Mixture momentum equation is solved by the mixture model, taking into consideration the relative velocities of the phases, and by prescription of it the model describes the dispersed phases.

A few researches on above mentioned multiphase models were also conducted. Hanafizadeh *et al.,* [15] examined and compared the multiphase models in terms of predicting heat transfer and found out that at low Reynolds number and developing region of the flow, Mixture model performs better heat transfer coefficient prediction than other models. The study of Lotfi *et al.,* [9] on numerical study of forced convective heat transfer of nanofluids found out that two phase Eulerian model underestimates the Nusselt number. He also concluded mixture model to be more convincing. Meanwhile, Davarnejad and Jamshidzadeh [16] observed that among three multiphase models (VOF, Eulerian and Mixture) VOF and Mixture model predicted friction factor and Nusselt number dramatically.

This is quite apparent that, though numerous researches have been conducted for comparing single and multiphase models, the domain of multiphase models remained heavily understudied. The conducted researches on multiphase models are limited to their particular focuses. Though the scale tipped a little bit on the side of mixture model, VOF model also holds a fair share of its accuracy. This leads to an absolute confusion regarding the best multiphase model for simulating nanofluids heat transfer. In addition, the information on heat transfer behavior of nanofluids for different nanoparticle concentrations is hazy. Which is why examining enhancement of convective heat transfer for turbulent flow of nanofluid with variable particle concentration using multiphase models remains as a vital necessity. Therefore, the present study aims to investigate the behavior of nanofluids convective heat transfer enhancement employing Mixture and VOF models by varying

particle concentration and Reynolds number. In addition, it intends to find out the most effective multiphase model to simulate nanofluids heat transfer enhancement by comparing the multiphase model results with existing experimental data.

2. Governing Equations

There are three principal equations associated with multiphase flows which have been derived from the basic concepts of fluid dynamics. First one is the continuity equation that talks about the conservation of mass. The second one is momentum equation talking about the conservation of momentum. Last one is the energy equation that represents the conservation of energy in a fluid element. All these equations are applicable to the flow of nanofluids.

2.1 Continuity Equation

According to this equation, the rate of mass entering the system exactly equals the rate of mass exiting the system plus the aggregation of mass in the system. The continuity equation for nanoparticles and base fluid can be represented as [5]:

$$\frac{\partial}{\partial t} (\varphi_{\alpha} \rho_{\alpha}) + \nabla (\varphi_{\alpha} \rho_{\alpha} U_{\alpha} - \Gamma_{\alpha} \nabla \varphi_{\alpha}) = 0$$
(1)

Here, ϕ , ρ , U and Γ stand for volume fraction, density, interstitial velocity vector and dispersion coefficient. The subscript α represents phase index.

2.2 Momentum Equation

The momentum equation which is also called Navier-Stokes equation refers to Newton's Second Law relating the rate of momentum change to the number total of forces that act on a component of liquid. The differential form of this equation is as following [5]:

$$\frac{\partial}{\partial t} \cdot (\varphi_{\alpha} \rho_{\alpha} U_{\alpha}) + \{\varphi_{\alpha} [\rho_{\alpha} U_{\alpha} U_{\alpha} - \mu_{e\alpha} (\nabla U_{\alpha} + (\nabla U_{\alpha})^{T})]\} = \varphi_{\alpha} (B_{\alpha} - \nabla P) + F_{\alpha}$$
(2)

T, *B*, ∇P and *F* indicate temperature, body force, pressure drop and interphase force respectively.

2.3 Energy Equation

The last equation is about the conservation of energy which states that energy cannot be created or destroyed and it only changes from one form to another. The final amount of energy in a system is same as the previous amount of it but just in a different form. In an equational manner it is represented as [5]:

$$\frac{\partial}{\partial t} \cdot (\varphi_{\alpha} \rho_{\alpha} U_{\alpha}) + \nabla \cdot [\varphi_{\alpha} (\rho_{\alpha} U_{\alpha} h_{\alpha} - k_{\alpha} \nabla T_{\alpha})] = \sum_{\beta=1}^{N} (\Gamma_{\alpha\beta} + h_{\beta s} - \Gamma_{\beta\alpha} \dot{h_{\alpha s}}) + Q_{\alpha} + S_{\alpha}$$
(3)

In this equation, enthalpy, thermal conductivity, interphase heat transfer and external heat source in energy equation are denoted by h, k, Q and S, whereas the subscripts β and s indicate phase index and solid particles.

3. Geometry and Meshing

For this simulation the geometry considered is a simple pipe as represented in Figure 1, which is horizontally placed with respect to the ground that will have a turbulent flow of nanofluid. The geometry has been obtained from benchmark research paper Bianco *et al.*, [17].



Fig. 1. Geometry for numerical simulation

Geometry specifications are mentioned in Table 1 as following:

Table 1	
Geometry specifications	
Specification	Magnitude
Material	Aluminium
Diameter (mm)	10
Length(mm)	1000
Heat transfer flow area (mm ²)	31416
Cross sectional area (mm ²)	78.54

Meshing is one of the most crucial part of CFD simulation. The accuracy of the analysis hugely depends on meshing. For statistical reliability and higher precision high density meshing is preferred. However, creating a mesh denser than necessary has a lot of side effects also including faulty results. Considering these factors orthogonal mesh was created. Near to the walls the mesh was created to be comparatively denser than the axis of the pipe according to the calculated first cell thickness. Figure 2 and Figure 3 represent the mesh created on the geometry for simulation and the Fluent grid close up respectively.



Fig. 2. Created mesh on 2D pipe geometry



Fig. 3. Grid for simulation in Fluent

4. Turbulence Modelling

In this study the standard k- ε model has been used for simulation of the turbulence flow of water-Al₂O₃ nanofluid. This model takes turbulent kinetic energy, k and its dissipation rate, ε into account and they are described as [18]

$$\nabla .(\rho_{eff}kU) = \nabla .\left[\left(\frac{\mu_t}{\sigma_k}\right)\nabla(k)\right] + G_k - \rho_{eff}\varepsilon$$
(4)

$$\nabla (\rho_{eff} \varepsilon U) = \nabla \left[\frac{\mu_t}{\sigma_{\varepsilon}} \nabla \varepsilon \right] + \frac{\varepsilon}{k} \left(C_{1\varepsilon} G_k - C_{2\varepsilon} \rho_{eff} \varepsilon \right)$$
(5)

$$G_k = \mu_t (\nabla U + (\nabla U)^T)$$
(6)

$$\mu_t = \rho_{eff} C_\mu \frac{k^2}{\varepsilon} \tag{7}$$

where, μ represents viscosity. C_1 and C_2 are coefficients in approximated turbulent transport equation. In addition, the subscript *eff* and *t* indicate effective and turbulent.

5. Boundary Conditions

The boundary conditions for investigation of convective heat transfer for turbulent flow of nanofluid have been obtained from the benchmark paper. The properties of fluid and particles were taken from there as well. In addition, the necessary thermophysical properties of the nanofluid for analysis and simulation were calculated using the formulas provided in the benchmark paper [17]. Table 2 represents the imposed boundary conditions on the geometry for the flow.

Table 2				
Boundary conditions used for the simulation				
Zone	Nature	Condition imposed		
Inlet	Velocity inlet	- Uniform velocity, Vo		
		- Uniform temperature, 1 _o = 293 K		
Outlet	Pressure outlet	Gauge pressure = 0 pa		
Walls	-	 No slip conditions 		
		- Constant temperature T _w = 350 K		

6. Mesh Independence Study (MIS)

Mesh independence test is a crucial step towards CFD simulation. As this is known that the accuracy of the results of CFD simulation depends on how good the mesh is, the optimal mesh has to be designed in a way that output parameter does not change by significant amount when the mesh is manipulated.

For this simulation the meshing was done by creating two different edge sizing, one along the vertical edges and one along the horizontal edges. The mesh independence test has been done by setting outlet average temperature as output parameter and then by varying the number of divisions at the inlet. This is quite apparent that when the number of divisions are changed the nodes, elements and cell numbers vary. Face meshing was done in order to achieve structured mesh. To make the mesh denser near to the walls according to the calculated first cell thickness, biasing method was used.

Five different mesh types were considered where the number of divisions at the inlet were varied from 10 to 50 divisions as presented in Table 3 and for each case outlet average temperature was recorded while keeping an eye towards the convergence iteration. At the same time, the difference between two consecutive iterations was calculated. Figure 4 shows the variation of pipe outlet temperature as element numbers increase due to increase in division.



As seen on Table 3, the difference between mesh type 1 and mesh type 2 was comparatively higher. The difference went down for mesh type 3 and got further reduced by a good amount in mesh type 4. After that it showed a small rise in mesh type 5. This is noticeable that the differences between outlet temperatures for the mesh types were very insignificant, specially starting from mesh type 3. It can be observed that, the iteration for convergence was the highest in mesh type 1. After that it suddenly dropped remarkably and started showing decent increase as divisions were increasing. Considering the differences in outlet temperature and the fact that higher iteration for convergence increases computational time, mesh type 4 was considered as the optimal mesh and all the simulations were run using this mesh type which contains 49241 nodes and 48000 elements. For the optimal mesh, the skewness and mesh quality were tested. The maximum and average skewness for this mesh was 1.3253×10^{-10} and 1.3061×10^{-10} respectively with an aspect ratio of 3.54781 which are within limits [19]. The orthogonal quality of the mesh is 1.00 which indicates the best orthogonal meshing.

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Mesh	Divisions	Nodes	Elements	Iteration for	Outlet average	Difference
Туре				Convergence	temperature (K)	(%)
1	10	13211	12000	474	316.08	-
2	20	25221	24000	366	316.20	0.1267
3	30	37231	36000	360	316.49	0.0379
4	40	49241	48000	380	316.24	0.0032
5	50	61252	60000	393	316.55	0.0727

Table 3 Mesh Independence Study (MIS)

7. Validation

The multiphase models were validated by comparing with the experimental result of Pak and Cho [20] which has also been presented in benchmark research paper Bianco *et al.*, [17]. The same boundary conditions and turbulence model as the benchmark paper such as specified inlet and wall temperature and standard k- ϵ turbulence model were used to carry out the result. The validation has been done by examining the change in Nusselt number with Reynolds number ranging from 20000 to 80000 for 4% particle concentration. Reynolds number and Nusselt number has been calculated using following equations:

$$Re = \frac{\rho VD}{\mu}$$
(8)

$$Nu = \frac{hD}{k}$$
(9)

Here V,h and D express flow velocity at fully developed region, heat flux and pipe diameter. The graphs in Figure 5 represents the comparison between simulated and experimental Re vs Nu for Mixture model and VOF model respectively for particle concentration of 4%. Both model show very close results. For both cases the error from experimental result ranges from 11 to 15 percent. The average error shown by these two models for 4 different Reynolds numbers are 12.3674% and 12.3799% for Mixture and VOF model respectively.



Fig. 5. Re vs Nu for particle concentration of 4%

8. Results and Discussion

Three different concentrations (1%,4% and 6%) have been tested using both models by calculating values of Nu against variable Re. The obtained result via simulation has been compared with the experimental result of Pak and Cho [20] which has also been presented in the benchmark paper. The graphs in Figure 6, Figure 7 and Figure 8 represent Re vs Nu for 1%,4% and 6% concentrations and the variation from the experimental result result respectively.

For particle concentration of 1 percent as Re goes from 20000 to 80000, Nu changes from 104.3131 to 326.4327 for mixture model and from 104.3268 to 326.4359 for VOF model. The average variation from experimental result for mixture model is 29.1955% and for VOF model is 29.1929%.

As nanoparticle concentration increases by 3% the pattern of Re vs Nu remains similar but this time both model predicts higher Nu for the same range of Re. Both models depict the same pattern of results while keeping a very small difference between each other. In fact in some cases the results for two models are so close that the difference can be counted as negligible and for a very few cases, specially at lower Re they yielded the same result. As Re goes from 20000 from 80000 the Nu increases from 196.77 to 575.99 for Mixture model and from 196.77 to 576.13 for VOF model. The results provided by Mixture and VOF model varies from the experimental result by 11% to 15%. The average difference from experimental result shown by Mixture and VOF models for 4 percent concentration is 12.3674% and 12.3799% respectively.

For the highest amount of particle concentration in this study (6%), Nu ranges between 256.9398 and 721.4352 according to Mixture model and between 256.9616 and 721.9857 according to VOF model as Re ranges between 20000 and 80000. The difference from experimental result ranges from 25% to 29%. To be more precise, in average Mixture model holds a variation of 28.6621% and VOF model holds a variation of 28.6898% from the experimental result. So, this can be derrived from the results that, for a given Re the heat transfer capability of nanofluids increases with the increase in particle concentration.



Fig. 6. Nusselt number with respect to Reynolds number for particle concentration of 1%



Fig. 7. Nusselt number with respect to Reynolds number for particle concentration of 4%



Fig. 8. Nusselt number with respect to Reynolds number for particle concentration of 6%

For visualizing the amount of difference from experimental data for each multiphase model, a comparison is shown in Table 4 . In the table, the difference range presented refers to the deviation of numerical simulation results from the experimental result as Re moves to 80000 from 20000. The average difference for each particle concentration has been obtained by calculating the mean value of differences for each Re that has been presented in the graphs. The difference between the results of two models were observed to be very small. In fact the difference between the Nu prediction of these two models are around 0.02%. Still considering this amount of difference it is observed that for particle concentration of 1%, VOF model is more convincing in the prediction of Nu while for particle concentrations VOF model is more accurate and for higher concentration Mixture model is more convincing for the prediction of convective heat transfer enhancement.

Table 4						
Difference between simulated and experimental result						
Particle concentration(%)	Difference range (%)		Average difference(%)			
	Mixture model	VOF model	Mixture model	VOF model		
1	27-29.6	27-29.6	29.1955	29.1929		
4	11-15	11-15	12.3674	12.3799		
6	25-29	25-29	28.6621	28.6898		



Fig. 9. Temperature contour for Re 40000 for particle concentration (1%, (b) 4% and (c) 6% for Mixture model

The reasons behind difference in performence with the variation in particle concentration lie in the principles of this two models. Whereas the VOF model solves only one set of momentum equation which is shared by both phases with respective densities, mixture model solves the mixture momentum equation where the mixture density and mixture viscocity are taken into account. Furthermore, the VOF model recognizes nanoparticles not as solids but as another much denser fluid which are spherical and have different properties and not immiscible with the base fluid. This is why VOF model takes surface tension between fluids into account which causes impact on heat transfer. As for the mixture model, it takes base fluid and nanoparticles as two different phases where particles

are treated as solids and the model includes drag force and collisions in the calculation. In addition it considers the slip velocities between phases that the VOF model tends to ignore by which the prediction of heat trasnfer is varied. At lower particle concentration the presence and effect of nanoparticles on the properties and behaviour of nanofluid as a distinct phase is low and mostly at these conditions nanofluids behaviour tips on the side of fluid. But as concentration is increased the effect of nanoparticles in the fluid starts becoming much visible and apparent in terms of exerted forces, difference in properties and other related variables. So with the increase of particle concentration it becomes more important to treat these phases differently and to treat phase interactions accordingly that the mixture model does but the VOF model seems to disregard specially when one phase is solid.

One more point to be noted that, for lower concentration numerical simulation underestimates Nu whereas for higher concentrations it overestimates Nu and this is true for both models. This implies that, there must be a certain concentration between 1% and 4% which will yield the same result by simulation and experiment in terms of heat transfer enhancement (Nu) and will contain 0% error. Further experimental work as well as simulation need to be conducted on this particle concentration range to find out such concentration that will yield 0% error with experimental data.

Some of the temperature contours for both models simulation are shown below in Figure 9 and Figure 10.





Fig. 10. Temperature contour for Re 40000 for particle concentration (a) 1%, (b) 4% and (c) 6% for VOF model

9. Conclusion

Both models show good agreement with experimental data at intermediate concentration. As particle concentration gets higher the deviation from experimental data seems to be getting significant. This can be said that heat transfer of nanofluids increases with rise in particle concentration and Re. At lower concentration VOF model seems to predict heat transfer enhancement better but for higher concentrations Mixture model should be considered. Some further study can be conducted on the particle concentration range 1% to 4% to examine the heat transfer behavior of water-Al₂O₃ nanofluid more perfectly.

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