



## The investigation on SIMPLE and SIMPLER algorithm through lid driven cavity

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### ABSTRACT

The present study analyzes in details to compare SIMPLE and SIMPLER algorithm in terms of their convergence rate, iteration number and computational time. The work which is based on primitive variables ( $u, v, P$ ) formulation of Navier-Stokes equations to investigate the velocity and pressure distribution in the square cavity at Reynolds number of 100 and 400. The solutions are obtained for grid size  $16 \times 16$  up to  $256 \times 256$ . From the plots of velocity profiles along centerline geometry, it shows good agreement with the benchmark solution from past researchers. The velocity and pressure in the cavity varies as the Reynolds number increases from 100 to 400. SIMPLER algorithm is proven to be more efficient compared to SIMPLE as iteration number required for a given Reynolds number and grid size is lower than that of SIMPLE. The values of under-relaxation factors for velocity components and pressure play significant role in terms of convergence rate of a numerical scheme.

#### Keywords:

SIMPLE algorithm, SIMPLER algorithm,  
Lid driven cavity, Navier-Stokes  
equations, Computational cost

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## 1. Introduction

Lid driven cavity [1,2] is a classic benchmark problem for viscous incompressible flow [3-5]. The model is able to exhibit various types of phenomena that can happen in an incompressible flow such as secondary flows, transition to turbulence, eddy flows and complex three-dimensional patterns [6,7]. In order to solve the incompressible Navier-Stokes equations, various methods have been developed and the commonly used numerical procedure is Semi-Implicit Method for Pressure Linked Equation (SIMPLE) and SIMPLER (SIMPLE – Revised) by [8].

Yapici and Uludag [9] have used finite volume method (FVM) of two-dimensional square lid driven cavity flow at high Reynolds number ( $Re$ ). The coupled flow equation is solved by SIMPLE algorithm. Moreover, he has used QUICK scheme to approximate the convection terms in the flow equations. In the findings, the accuracy of a numerical solution can be improved by using a smaller mesh in the regions of high gradients than the mesh size of bulk flow.

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Jing Yang *et al.* [10] have presented a model for pool boiling called CAS model. The numerical model is commonly used to measure the heat transfer in the industries application. SIMPLER algorithm is integrated with a cellular automata technique to investigate the pressure and temperature during the boiling process as the cellular automata technique alone is not effective to investigate the boiling process. From the results shown, the integration of the technique into the algorithm has proven to be a good approach in obtaining data coherent with the benchmark solution.

Yin and Chow [11] have computed comparison of four algorithms in simulating atrium fire. The four algorithms for solving the velocity-pressure coupled equations are SIMPLE, SIMPLER, SIMPLEC and PISO. The numerical schemes are each tested with the relaxation factors. In the results, all four algorithms provide similar data for the flow variables except for pressure. It is concluded in the studies that SIMPLER is the viable algorithms used to solve the equations in simulating atrium fire.

Although SIMPLE and SIMPLER method is widely used to solve velocity-pressure coupling fluid problems, the numerical comparison between them is still unclear. Hence, the objective of the present study is to compare SIMPLE and SIMPLER in terms of convergence, iteration number and computational time.

## 2. Numerical details

### 2.1. The governing equations

The incompressible two-dimensional Navier-Stokes equations can be written as follows:

$$\rho \left( \frac{\partial u}{\partial t} + \frac{\partial uu}{\partial x} + \frac{\partial uv}{\partial y} \right) = -\frac{\partial P}{\partial x} + \mu \nabla^2 u \quad (1)$$

$$\rho \left( \frac{\partial v}{\partial t} + \frac{\partial vv}{\partial y} + \frac{\partial uv}{\partial x} \right) = -\frac{\partial P}{\partial y} + \mu \nabla^2 v \quad (2)$$

$$\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} = 0 \quad (3)$$

with  $\nabla = i \frac{\partial}{\partial x} + j \frac{\partial}{\partial y}$ . Expanding the terms on x- and y-momentum equations results in:

$$\rho \left( \frac{\partial u}{\partial t} + \frac{\partial uu}{\partial x} + \frac{\partial uv}{\partial y} \right) = -\frac{\partial P}{\partial x} + \mu \left( \frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} \right) \quad (4)$$

$$\rho \left( \frac{\partial v}{\partial t} + \frac{\partial vv}{\partial y} + \frac{\partial uv}{\partial x} \right) = -\frac{\partial P}{\partial y} + \mu \left( \frac{\partial^2 v}{\partial x^2} + \frac{\partial^2 v}{\partial y^2} \right) \quad (5)$$

Based on Eq.s (3) – (5), a general transport equation can be written as follows:

$$\frac{\partial}{\partial t} (\rho \phi) + \frac{\partial}{\partial x} (\rho u \phi) + \frac{\partial}{\partial y} (\rho v \phi) = \frac{\partial}{\partial x} \left( \Gamma \frac{\partial \phi}{\partial x} \right) + \frac{\partial}{\partial y} \left( \Gamma \frac{\partial \phi}{\partial y} \right) + S_\phi \quad (6)$$

where  $\phi$  is the dependent variable such as velocity, temperature and enthalpy,  $\Gamma$  is the diffusion coefficient and  $S_\phi$  represent the source term. The first term on LHS is the unsteady term and the second and third term on LHS is the convection terms. Consider only the x-momentum equation, the  $\phi$  in Eq. 6 is replaced by u-velocity. Using discretization method by staggered grid as explained in detail by [4,10], discretized x-momentum equation is as follows:

$$a_P u_P = a_E u_E + a_W u_W + a_N u_N + a_S u_S + b_u = \sum_{nb} a_{nb} u_{nb} + b_u \quad (7)$$

where the coefficient  $a_E, a_W, a_N, a_S$  are the convection – diffusion at the neighboring cell faces and  $b_u = (p_e - p_w) + S_e \Delta x \Delta y$ .

## 2.2. SIMPLE algorithm

The Semi-Implicit Method for Pressure-Linked Equations (SIMPLE) is originally proposed by [8]. The principle of SIMPLE is to create discrete pressure equation based on discrete continuity equation. The  $u$ -momentum equation for control volume centred at  $e$  is given as:

$$a_e u_e = \sum_{nb} a_{nb} u_{nb} + A_e (P - P_E) + b_e \quad (8)$$

A guessed pressure field denoted as  $P^*$  is to replace onto the Eq. 8 to obtain guessed velocity components of  $u^*$  and  $v^*$ :

$$a_e u_e^* = \sum_{nb} a_{nb} u_{nb}^* + A_e (P_P^* - P_E^*) + b_e \quad (9)$$

However, the guessed velocity components would not able to satisfy conservation of mass, in that case, velocity and pressure are corrected by adding correction values:

$$\begin{aligned} u &= u^* + u' \\ P &= P^* + P' \\ v &= v^* + v' \end{aligned} \quad (10)$$

Relating Eq.s 8 - 10 gives:

$$a_e u_e' = \sum_{nb} a_{nb} u_{nb}' + A_e (P_P' - P_E') \quad (11)$$

The neighbouring values in Eq. 11 are omitted for approximation as the terms will not affect the final solution due to the correction values,  $u'$  will be zero when the solution converged. Then, relating to Eq. 10 becomes:

$$u_e = u_e^* + d_e (P_P' - P_E') \quad (12)$$

At this point, Eq. 12 is needed to satisfy the discretized continuity equation  $(\rho u A)_e - (\rho u A)_w + (\rho v A)_n - (\rho v A)_s = 0$ , hence it is substitute into the continuity equation. The same goes for  $u_w, u_n, u_s$  which gives:

$$\begin{aligned} [(\rho d A)_e + (\rho d A)_w + (\rho d A)_n + (\rho d A)_s] P_P' &= (\rho d A)_e P_E' + (\rho d A)_w P_W' + (\rho d A)_n P_N' + (\rho d A)_s P_S' + \\ [(\rho u^* A)_w - (\rho u^* A)_e + (\rho u^* A)_s - (\rho u^* A)_n] &= 0 \end{aligned} \quad (13)$$

Simplifying Eq. 13 leads to:

$$a_P P_P' = a_E P_E' + a_W P_W' + a_N P_N' + a_S P_S' + b_P' \quad (14)$$

where,

$$a_E = (\rho dA)_e$$

$$a_W = (\rho dA)_w$$

$$a_N = (\rho dA)_n$$

$$a_S = (\rho dA)_s$$

$$a_P = \sum_{nb} a_{nb}$$

$$b'_P = (\rho u^* A)_w - (\rho u^* A)_e + (\rho u^* A)_s - (\rho u^* A)_n$$

Eq. 14 is a pressure correction equation, the momentum source term  $b'$  is the mass imbalance due to incorrect velocity field. When the source term reaches zero, it means that the solution has converge.

### 2.3. SIMPLER algorithm

SIMPLER is a revised version of SIMPLE in which discretized continuity equation is used to derived discretized equation for pressure instead of pressure correction equation. Pseudo-velocities are introduced in SIMPLER, which can be defined as follows:

$$\hat{u}_e = \frac{\sum_{nb} a_{nb} u_{nb} + b_e}{a_e} \quad (15)$$

Substitute Eq. 15 into Eq. 8 gives:

$$u_e = \hat{u}_e + d_e(p_P - p_E) \quad (16)$$

Substitute Eq. 16 into discretized continuity equation and rearranging the terms produces:

$$[(\rho dA)_e + (\rho dA)_w + (\rho dA)_n + (\rho dA)_s] p'_P = (\rho dA)_e p_E + (\rho dA)_w p_W + (\rho dA)_n p_N + (\rho dA)_s p_S + [(\rho \hat{u} A)_w - (\rho \hat{u} A)_e + (\rho \hat{v} A)_s - (\rho \hat{v} A)_n] \quad (17)$$

Eq. 17 can be further simplified into:

$$a_P p_P = a_E p_E + a_W p_W + a_N p_N + a_S p_S + b_P \quad (18)$$

where

$$a_E = (\rho dA)_e$$

$$a_W = (\rho dA)_w$$

$$a_N = (\rho dA)_n$$

$$a_S = (\rho dA)_s$$

$$a_P = \sum_{nb} a_{nb}$$

$$b'_P = (\rho \hat{u} A)_w - (\rho \hat{u} A)_e + (\rho \hat{v} A)_s - (\rho \hat{v} A)_n$$

After obtaining the pressure value, the following sequence is the same as SIMPLE in which the pressure value is used to solve the discretized momentum equation.

### 3. Results and discussion

#### 3.1. Mesh independence study and validation

Prior to comparative study on computational efficiency of SIMPLE and SIMPLER model, the validation is done by comparing the computed velocity value with the work of [13].

Extrema of velocity along geometry centreline at  $Re = 100$  and  $Re = 400$  are tabulated in Table 1 and Table 2. It is shown that both algorithms are able to produce results that are good agreement with Ghia's benchmark solution [13] as the grid increases. It can be said that grid independence is achieved in this case.

For SIMPLE algorithm, the Navier-Stokes equations can only be solved up to  $128 \times 128$  grid due to the under-relaxation factors. Optimal value of relaxation factors could not be obtained, hence, the solution oscillates and diverge at one point of the iteration. In the present study, convergence criterion is set as  $10^{-3}$  at which the simulation is terminated and assumed to reach steady state. The convergence criterion defined in the present study is the summation of error of velocity components and pressure,

$$\epsilon = \sum |\phi^{n+1} - \phi^n| \leq 10^{-3} \quad (19)$$

where  $\phi$  represents primitive variables,  $n$  is the iteration step.

**Table 1**

Extrema of velocity along geometry centerline at  $Re = 100$

Reference	Grid	$U_{min}$	$V_{max}$	$V_{min}$
SIMPLE	$16 \times 16$	-0.18011	0.14960	-0.20606
SIMPLER	$16 \times 16$	-0.18741	0.16002	-0.23098
SIMPLE	$32 \times 32$	-0.20687	0.17349	-0.24592
SIMPLER	$32 \times 32$	-0.20555	0.17387	-0.24588
SIMPLE	$64 \times 64$	-0.21265	0.17834	-0.25247
SIMPLER	$64 \times 64$	-0.21183	0.17810	-0.25167
SIMPLE	$128 \times 128$	-0.21373	0.17932	-0.25356
SIMPLER	$128 \times 128$	-0.21349	0.17924	-0.25335
SIMPLER	$256 \times 256$	-0.21391	0.17950	-0.25371
Ghia <i>et al.</i> [13]	$129 \times 129$	-0.21090	0.17527	-0.24533

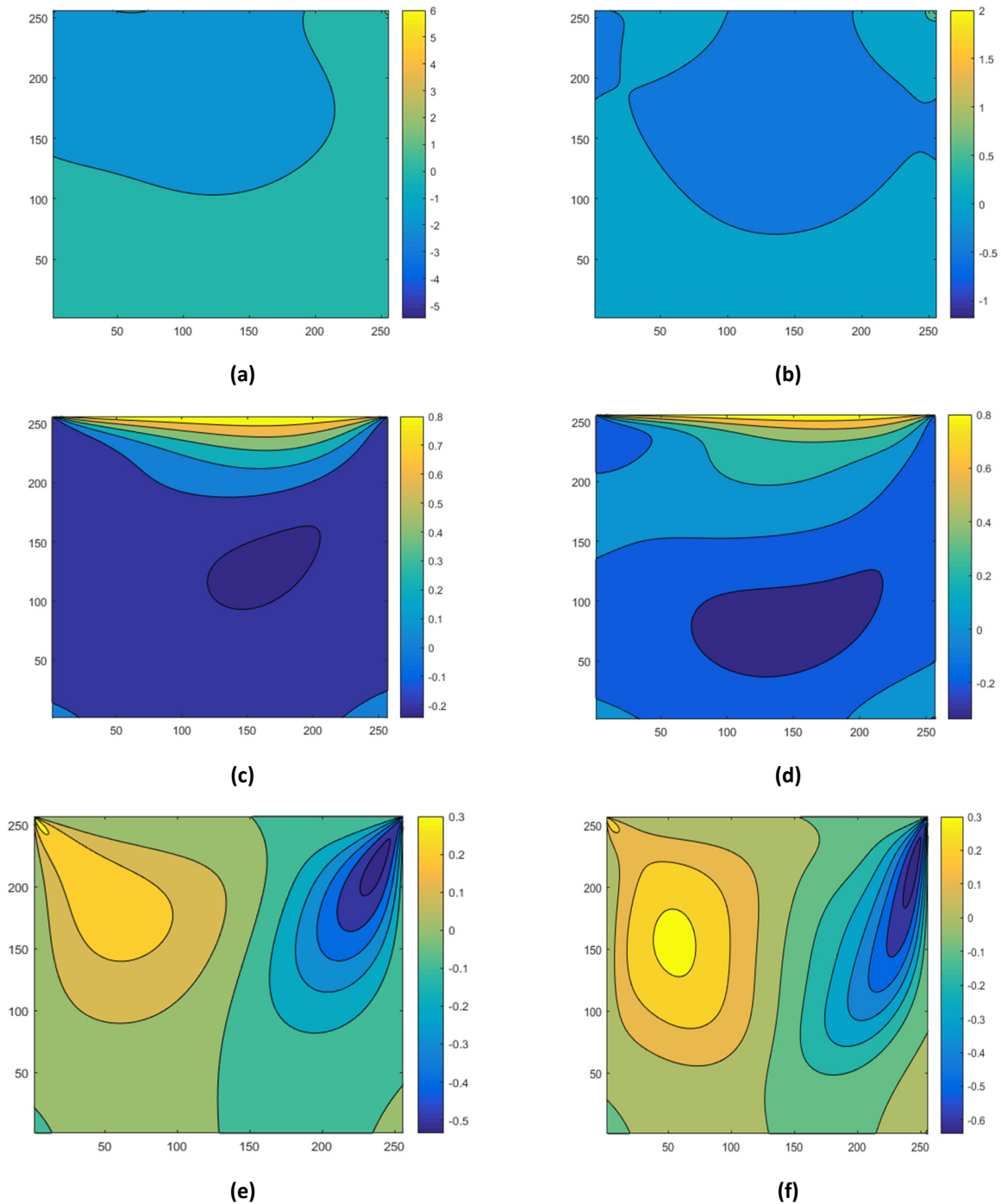
**Table 2**

Extrema of velocity along geometry centerline at  $Re = 400$

Reference	Grid	$U_{min}$	$V_{max}$	$V_{min}$
SIMPLE	$16 \times 16$	-0.17234	0.16559	-0.28274
SIMPLER	$16 \times 16$	-0.17200	0.16585	-0.28220
SIMPLE	$32 \times 32$	-0.24566	0.23069	-0.36796
SIMPLER	$32 \times 32$	-0.24533	0.23085	-0.36778
SIMPLE	$64 \times 64$	-0.29837	0.27849	-0.42560
SIMPLER	$64 \times 64$	-0.29770	0.27749	-0.42458
SIMPLE	$128 \times 128$	-0.31973	0.29701	-0.44629
SIMPLER	$128 \times 128$	-0.31928	0.29602	-0.44564
SIMPLER	$256 \times 256$	-0.32613	0.30172	-0.45178
Ghia <i>et al.</i> [13]	$129 \times 129$	-0.32726	0.30203	-0.44993

### 3.2. Pressure-Velocity contour plot

As both algorithms produced similar results, finest grid size of contour plots are illustrated from Fig. 1(a) - 1(f). With the increasing of Reynolds number from 100 to 400, the pressure in the cavity has decreases. The maximum pressure of the flow is present at the top right corner of the cavity, whereas, the minimum pressure occurs at the top left corner of the cavity. As the fluid moves from left to right on the top lid, the fluid starts to spreads throughout the cavity after knocking the right wall. The pressure is then decreases at the lower part of the cavity.



**Fig. 1.** Contour plots with at  $256 \times 256$  grid for (a) pressure,  $Re = 100$ ; (b) pressure,  $Re = 400$ ; (c)  $u$ -velocity,  $Re = 100$ ; (d)  $u$ -velocity,  $Re = 400$ ; (e)  $v$ -velocity,  $Re = 100$ ; (f)  $v$ -velocity,  $Re = 400$

In the  $u$ -velocity contour plot, the velocity flow is dominant at the top lid due to stationary walls on both sides. In addition to that, it can be seen that the boundary layer of the flow near the top moving lid is thinner as the Reynolds number increases. The region of the minimum velocity has increases and shifted towards the center of the cavity.

Due to the increase of Reynolds number, the velocity components have a higher magnitude throughout the region inside the cavity. The bottom left and right corner of low velocity has covers larger region as compared to at  $Re = 100$ . In  $v$ -velocity contour, the fluid flow is dominant on the left wall and the flow is reverse on the right wall. At higher  $Re$ , the maximum and minimum  $v$ -velocity regions spreads out, covers larger area in the cavity.

### 3.3. Velocity profile analysis

From Fig. 2 - 5, it is shown that the  $u$ -velocity and  $v$ -velocity profile along vertical and horizontal centerline of geometry of cavity respectively are coherent with Ghia's benchmark solution as the grid size increases. However, SIMPLE algorithm unable to be implemented for  $256 \times 256$  grid size due to incompatible relaxation factors. Optimum relaxation factors for velocity and pressure cannot be found, hence, cause the solution to oscillates and diverge.

The minimum  $u$ -velocity along the vertical centerline of the cavity and  $v$ -velocity at minimum and maximum along horizontal centerline for various grid sizes are computed in Table 3. The minimum  $u$ -velocity is denoted as  $u_{min}$  and minimum and maximum  $v$ -velocity are denoted as  $v_{min}$  and  $v_{max}$  respectively. As can be seen from the table, the extrema of velocity of grid size  $128 \times 128$  and  $256 \times 256$  of SIMPLER algorithm does not differ much. This in turns shows that, the numerical solution will no longer changes with the increasing of grid size, in other words, grid independence. Furthermore, both SIMPLE and SIMPLER algorithms have implemented and converge to similar results.

**Table 3**  
 Extrema of velocity along the centerline of the cavity,  $Re = 100$

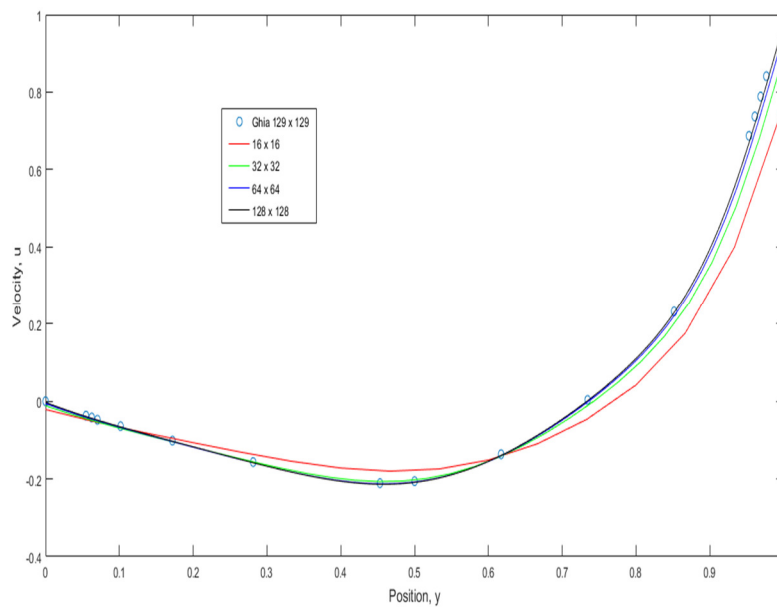
Reference	Grid	$u_{min}$	$v_{max}$	$v_{min}$
SIMPLE	$16 \times 16$	-0.18011	0.14960	-0.20606
SIMPLER	$16 \times 16$	-0.18741	0.16002	-0.23098
SIMPLE	$32 \times 32$	-0.20687	0.17349	-0.24592
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SIMPLE	$64 \times 64$	-0.21265	0.17834	-0.25247
SIMPLER	$64 \times 64$	-0.21183	0.17810	-0.25167
SIMPLE	$128 \times 128$	-0.21373	0.17932	-0.25356
SIMPLER	$128 \times 128$	-0.21349	0.17924	-0.25335
SIMPLER	$256 \times 256$	-0.21391	0.17950	-0.25371
Ghia <i>et. al</i> [10]	$129 \times 129$	-0.21090	0.17527	-0.24533

In the simulation runs at  $Re = 400$ , the results obtained are also coherent with the benchmark solution as shown in Fig.s 6 - 9. Both algorithms are implemented and matches well with Ghia as the size of the grid increases. SIMPLE algorithm can only be implemented to solve up until  $128 \times 128$  due to incompatible relaxation parameters found.

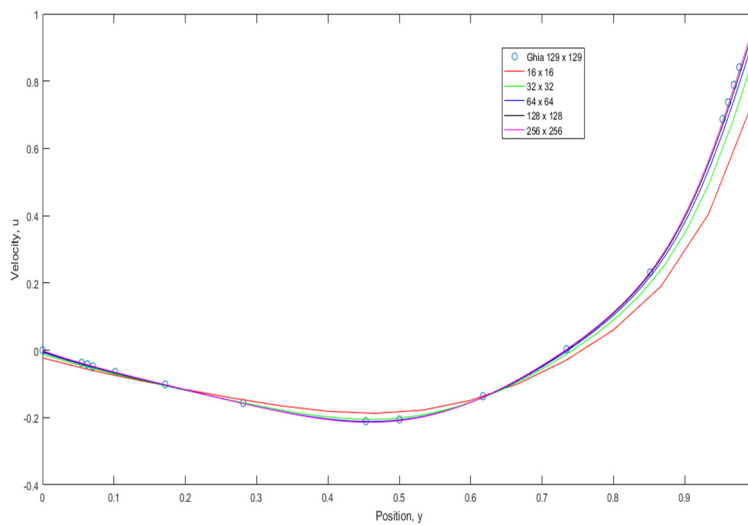
As previously mentioned in the results at  $Re = 100$ , there is not much difference in extrema velocity of grid size  $128 \times 128$  and  $256 \times 256$ . However, at  $Re = 400$ , the velocity between the two grid sizes has larger difference values as compared to the solution at  $Re = 100$ . It can be said that for larger Reynolds number, finer grid size is required in order to reach grid independence. Similarly, both SIMPLE and SIMPLER algorithm implemented is able to converge to the same extrema velocity profiles at all grid sizes. This can be shown through Table 4.

**Table 4**  
 Extrema of velocity along the centerline of the cavity,  $Re = 400$

Grid	Umin	Vmax	Vmin
16 x 16	-0.17234	0.16559	-0.28274
16 x 16	-0.17200	0.16585	-0.28220
32 x 32	-0.24566	0.23069	-0.36796
32 x 32	-0.24533	0.23085	-0.36778
64 x 64	-0.29837	0.27849	-0.42560
64 x 64	-0.29770	0.27749	-0.42458
128 x 128	-0.31973	0.29701	-0.44629
128 x 128	-0.31928	0.29602	-0.44564
256 x 256	-0.32613	0.30172	-0.45178
129 x 129	-0.32726	0.30203	-0.44993

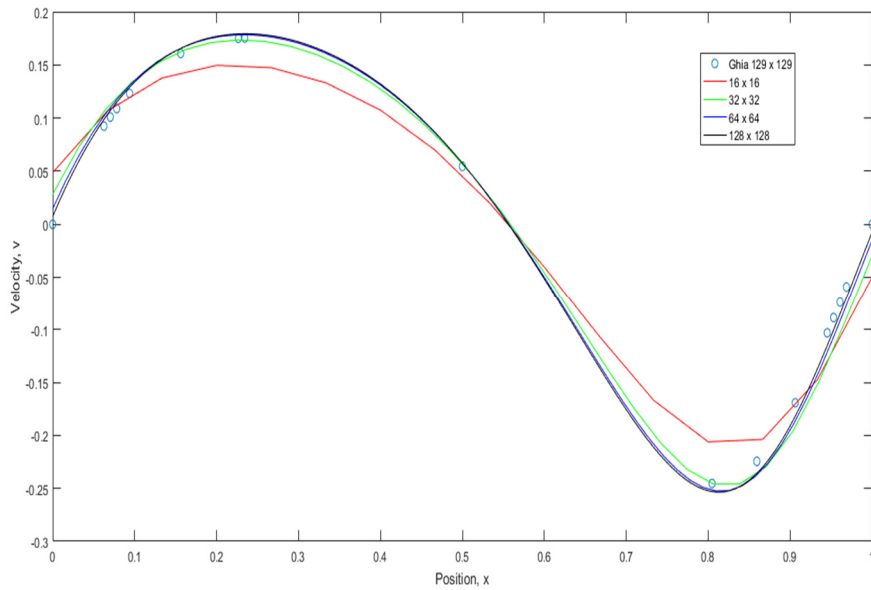


**Fig. 2.** U-velocity profile along vertical centerline by SIMPLE algorithm at  $Re = 100$

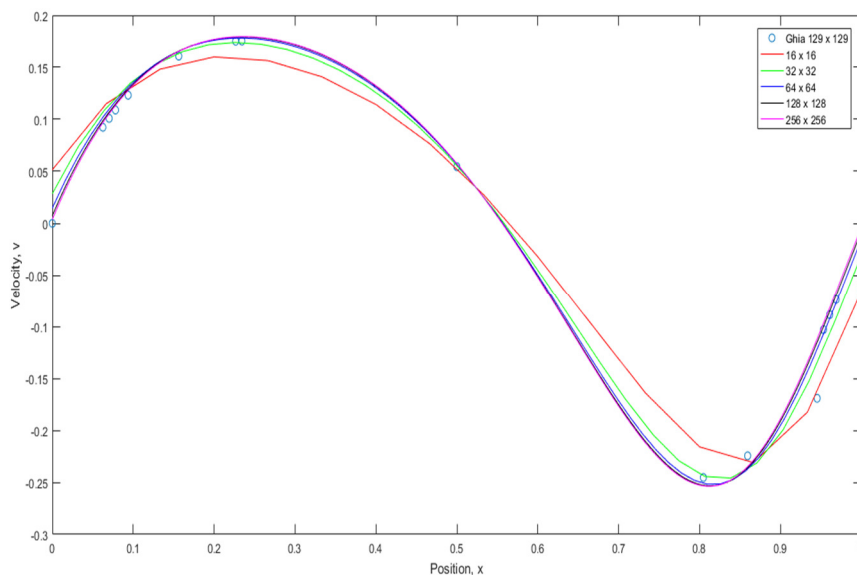


**Fig. 3.** V-velocity profile along vertical centerline by SIMPLE algorithm at  $Re = 100$





**Fig. 4.** U-velocity profile along horizontal centerline by SIMPLE algorithm at  $Re = 100$



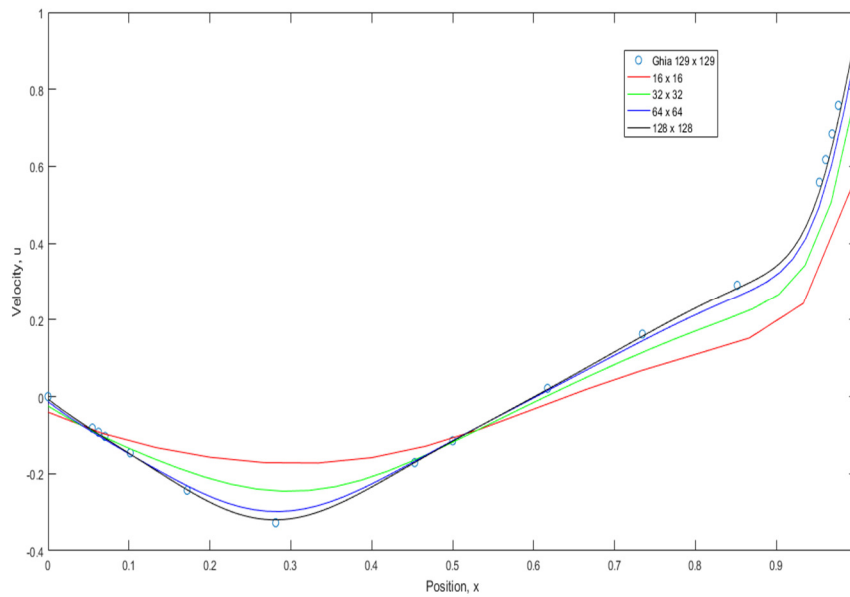
**Fig. 5.** V-velocity profile along horizontal centerline by SIMPLE algorithm at  $Re = 100$

### 3.4. Computational Cost Study

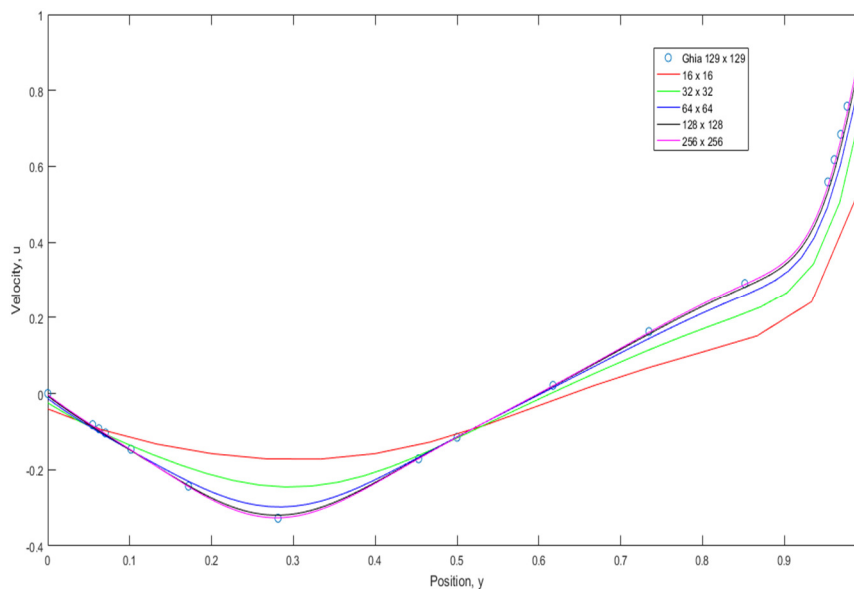
The numerical solution is obtained on PC with Intel® Core™i5 processor and 8GB RAM. In general, it can be seen that the iteration number and computational time to implement SIMPLE is much larger than SIMPLER. For  $Re = 400$  and at grid size  $128 \times 128$ , the iteration number and computational time has reach as high as 127999 and 16228.38 seconds. Whereas, for SIMPLER algorithm, it can go as fast as 1.03 seconds and only require 309 iterations to obtain the solution.

However, there is a set of values which does not follow the trend, at which at  $Re = 100$  of grid size  $128 \times 128$ , the iteration number and computational time required for SIMPLER is larger than that of SIMPLE. The reason of this discrepancy is due to the relaxation factor used in the SIMPLE algorithm. As mentioned in Chapter III, the algorithm is largely dependent on the relaxation factors. For this

case, the relaxation factor selected could be the optimum value for the algorithm to run at that given Reynolds number and grid size. The iteration number and computational time for SIMPLE algorithm can be improved if an optimum relaxation factor can be found.



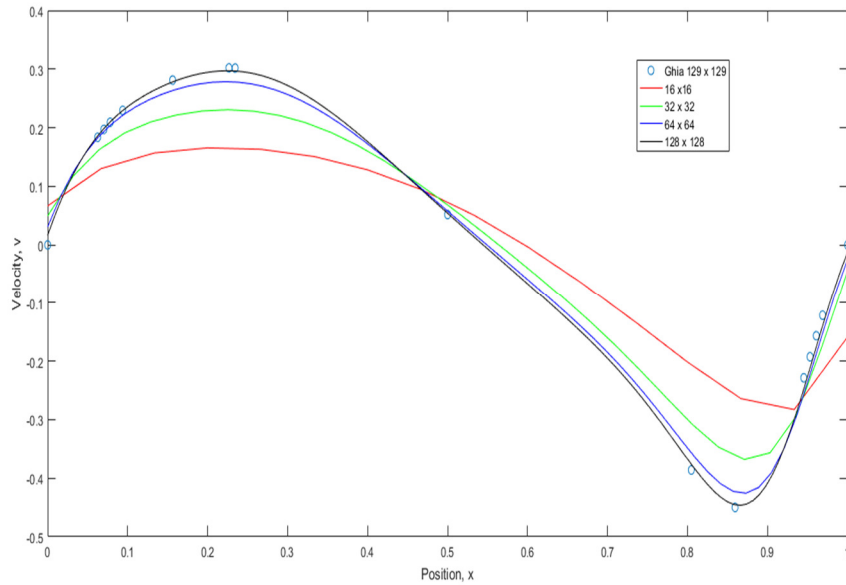
**Fig. 6.** U-velocity profile along vertical centerline by SIMPLE algorithm at  $Re = 400$



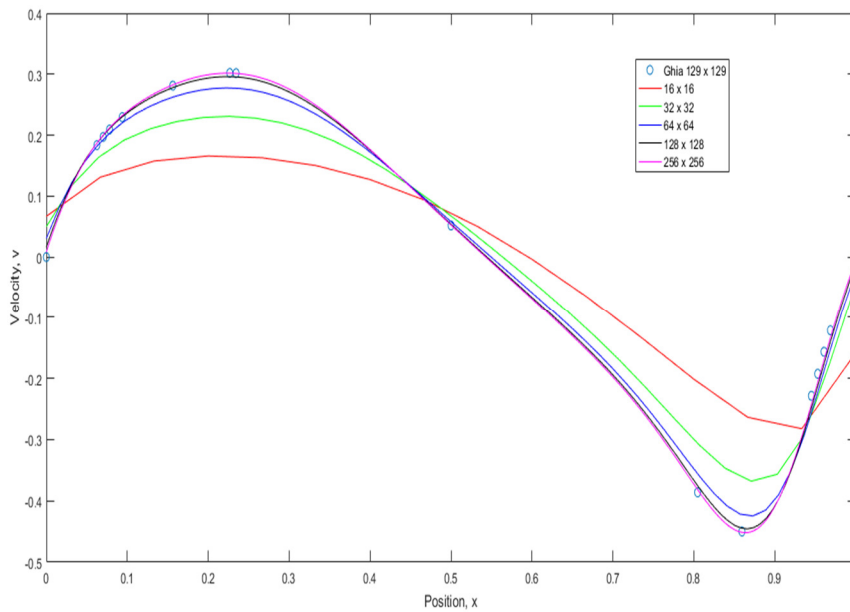
**Fig. 7.** V-velocity profile along vertical centerline by SIMPLE algorithm at  $Re = 400$

The convergence rate between SIMPLE and SIMPLER algorithms are compared and computed in the Table 5 - 7. Referring to [14], the rate of convergence can be calculated with the formula given as follows:

$$convergence\ rate = \log_2 \frac{|u_{min}^{32 \times 32} - u_{min}^{128 \times 128}|}{|u_{min}^{64 \times 64} - u_{min}^{128 \times 128}|} \quad (19)$$



**Fig. 8.** U-velocity profile along horizontal centerline by SIMPLE algorithm at  $Re = 400$



**Fig. 9.** V-velocity profile along horizontal centerline by SIMPLE algorithm at  $Re = 400$

Grid size  $128 \times 128$  is chosen as the reference solution. The ratio of the two errors can get an estimate of the convergence.  $u_{min}$  and  $v_{min}$  of grid size  $32 \times 32$ ,  $64 \times 64$  and  $128 \times 128$  at  $Re = 100$  and  $Re = 400$  are select from Table 1 – 2.  $Rate_u$  and  $Rate_v$  are the convergence rate for the  $u_{min}$  and  $v_{min}$  respectively. In the table, it shows that SIMPLER algorithm implemented at  $Re = 100$  and  $Re = 400$  has better convergence rate as compared to SIMPLE algorithm due to the smaller ratio in error.

**Table 5**  
 Iteration number and computational time at  $Re = 100$

Re = 100	Grid	Iteration Number	Computational Time (s)
SIMPLE	16 × 16	7039	17.17
SIMPLER	16 × 16	309	1.03
SIMPLE	32 × 32	11974	85.87
SIMPLER	32 × 32	1175	12.26
SIMPLE	64 × 64	13922	305.51
SIMPLER	64 × 64	4576	146.94
SIMPLE	128 × 128	17296	1244.98
SIMPLER	128 × 128	18169	2038.38

**Table 6**  
 Iteration number and computational time at  $Re = 400$

Re = 400	Grid	Iteration Number	Computational Time (s)
SIMPLE	16 × 16	2745	9.40
SIMPLER	16 × 16	437	1.12
SIMPLE	32 × 32	8366	94.54
SIMPLER	32 × 32	1321	11.94
SIMPLE	64 × 64	21069	753.22
SIMPLER	64 × 64	3840	129.86
SIMPLE	128 × 128	127999	16228.38
SIMPLER	128 × 128	13705	1542.31

**Table 7**  
 Convergence rate at  $Re = 100$  and  $Re = 400$

Reference	Reynolds Number	Rate <sub>u</sub>	Rate <sub>v</sub>
SIMPLE	100	2.667	2.809
SIMPLER	100	2.258	2.153
SIMPLE	400	1.794	1.921
SIMPLER	400	1.777	1.886

#### 4. Conclusion

In the present work, SIMPLE and SIMPLER are employed to investigate the pressure and velocity distribution in lid driven cavity. Comparison have made between the two algorithms in terms of convergence, iteration number and computational time. Numerical solution for the incompressible flow at  $Re = 100$  and  $Re = 400$  up to  $256 \times 256$  grid are computed. The results obtained compared well with the benchmark solution from previous literature. The pressure and velocity distribution changes according to the Reynolds number. The magnitude of the pressure and the location of the minimum  $u$ -velocity region are affected by the variation of Reynolds number. From this study, it is found that SIMPLER require less iteration number and computational time to converge solution despite the extra computational load. The findings from this study are able to be used as a reference by future researchers in the comparison of these numerical schemes.

Future improvement can be made on this study to improve the computational time of the numerical schemes. FORTRAN can be used as it is better as compared to MATLAB with its recognizable computational efficiency. This in turns improve the performance and encourages more findings at higher Reynolds number and finer grid size in shorter amount of time. In addition, an application of improvised under-relaxation method on SIMPLE algorithm can improve the convergence rate and computational time. In this way, more results can be obtained if optimal

relaxation factors are used in the numerical scheme. The solution will no longer oscillates heavily or diverge.

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