

Water Infiltration into Sand, Silt, and Clay at Field Capacity

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ABSTRACT

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Field capacity (FC), permanent wilting (PWP), and plant available water (PAW) are essential parameters to estimate for soils because they are essential for water irrigation management. However, these parameters were reported in water volume per unit soil volume. Knowing the soil required water volume does not imply immediate water availability, that is, the speed at which the water could be supplied to the soil. This is because there is a lag time between water irrigation initiation and the water increment in the soil depth. This study uses the field capacity's soil water content to simulate the water infiltration using Richards' equation. The studied soil medium was silt, sand, and clay. The study allows an estimate of water infiltration time and infiltrated water to relate to the soil depth of interest. The clayey has the highest FC, and the silty soil has the highest PAW. The results revealed silty soil could contain more readily water for plant growth than sand and clay. This study also revealed silty soil to be a better soil medium than sand and clay. It has the best trade-off between water infiltration time and the infiltrated amount of water for plant absorption. This study's coupling technique will be a useful tool for farmers and field practitioners to assess any site based on the soil texture at an early stage of water irrigation investigation.

1. Introduction

Soil water is an essential element in crop management [1-3]. Under natural conditions, water supplies through rainfall [4], water flux from deeper soil water like groundwater [5], incoming water flux from neighboring soil at higher soil water content [6], and fog and dew formation on the soil surface [7-10]. Human interventions such as cloud seeding [11-13] and water irrigation system [14] would supply water for plants' needs. When the supplied water hits the ground, it seeps into the soil by the gravitational pull [15]. Also, there are attractive forces between water molecules and soil particles, which results in water mass diffusion. These mechanisms resulted in water variability in space and time in subsurface soil.

A way of reporting quantified water in the soil is in soil water content [16]. Soil water content quantifies the water volume in a unit volume of soil [17]. When the pore spaces between soil particles

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fill with water, the water stage is known as saturated soil water content [18]. When sufficiently drained by the gravitational pull, the saturated soil water content would result in a soil water content level known as field capacity (FC) [19]. FC is the level at which water remains relatively stagnant in the soil [20-21]. The soil water content is susceptible to further reduction by plant roots absorption [22] and water loss by evaporation [23] at this level. The subsequent decrease in soil water content would reach a permanent wilting point (PWP). The PWP is at a soil water content level that the water molecules are firmly attached to the soil particles [24]. The forces between water molecules and soil particles are far greater than absorption forces by the plant roots. Hence, at the PWP's soil moisture level, the plants begin to wilt due to the plant roots' failure to absorb water. The primary purpose of water irrigation is to achieve soil moisture content within the range of FC and PWP. The difference between FC and PWP is known as PAW [8].

The natural way to achieve the PAW's soil water content range is by rainfall [25]. Alternatively, a soil moisture sensor installed at a soil depth could measure soil water content and indicating the need for water irrigation when it falls below the PWP's soil water content level [27]. This method is appropriate given that the existing water irrigation system and the availability of water resources in the immediate surrounding area can supply the water demand. However, such a condition is relatively too late should the existing system fail to meet the plantation water demand. Hence, early-stage water irrigation planning before plantation begins is necessary.

The PAW indicates the necessity of maintaining the minimum water volume in a soil volume unit to sustain plant water needs. However, it does not indicate the rate of water supply. Water supply rate is essential information for planning the crop water requirement because supplying a water volume in a second, a minute, or an hour has a significant implication on the water irrigation system and storage design. Thus, the current study addresses the knowledge gap using the Richards' equation to estimate the water infiltration rate into the soil at field capacity's soil moisture content. The study develops the reference data to relate soil depth, water infiltration time, and water infiltration rate. The information can be useful to farmers or field practitioners as a screening tool for an early-stage site water demand assessment.

2. Methodology

Sandy, silty, and clayey soils were used in the current study. Rosetta [28] was used to generate the van Genuchten equation's parameters [29], and the parameters were used in the characteristic function. The characteristic curve (Eq. (1)) and the unsaturated hydraulic conductivity-water content (Eq. (2)) for van Genuchten equations used to represent the soil, respectively, were,

$$\theta_L(\psi_m) = \theta_r + \frac{\theta_s - \theta_r}{\left[1 + (\alpha\psi_m)^n\right]^{1-1/n}} \quad (1)$$

$$K(\theta_L) = K_s \left(\frac{\theta_L - \theta_r}{\theta_s - \theta_r}\right)^L \left\{1 - \left[1 - \left(\frac{\theta_L - \theta_r}{\theta_s - \theta_r}\right)^{1/m}\right]^m\right\}^2 \quad (2)$$

The field capacity (FC) and permanent wilting point (PWP) were estimated using Eq. (1). The soil matric suction used to estimate soil water content at FC and PWP were -3.3 and -150 m, respectively [30]. The FC and PWP were estimated for sand, silt, and clay.

Richards' equation [31] simulates water infiltration into unsaturated soil. The equation was used in the current study, as below [32]:

$$\frac{\partial \theta_L}{\partial t} = \frac{\partial}{\partial z} \left[K \left(\frac{\partial \psi_m}{\partial \theta_L} \right) \frac{\partial \theta_L}{\partial z} - K \right] \quad (3)$$

Eq. (3) is a mass balance equation in which the right side of the equation governs the mass flux of water enters and leaves the soil volume in space, and the left side of the equation governs the accumulation as in mass appreciation or depreciation with time. Other than diffusion and gravity mechanisms given in Eq. (3), heat could also influence the flow of water in porous media, but not consider in the current study [33]. In some situations, multiphase flows in porous media are also possible [34].

Richards' equation can be solved using finite difference solution, and the solution in the algebra form is as follows [35]:

$$\frac{\theta_{L(k)}^{n+1} - \theta_{L(k)}^n}{\Delta t} = \frac{K_{k+1/2} (\partial \psi_m / \partial \theta_L)_{k+1/2} (\theta_{L(k+1)}^{n+1} - \theta_{L(k)}^{n+1})}{(\Delta z)^2} - \frac{K_{k-1/2} (\partial \psi_m / \partial \theta_L)_{k-1/2} (\theta_{L(k)}^{n+1} - \theta_{L(k-1)}^{n+1})}{(\Delta z)^2} - \frac{K_{k+1/2} \bar{k} - K_{k-1/2} \bar{k}}{\Delta z} \quad (4)$$

A thorough explanation of the numerical scheme used is available in Goh and Noborio [36].

3. Results and Discussion

Figure 1 shows the relation of soil water content with soil matric suction from 0 to -10,000,000 cm negative pressure head for clayey soil. When there is zero matric suction (or zero pressure head), the clayey soil is at a fully saturated state in which the water has filled the entire pore spaces between the soil particles. The fully saturated water content for clayey soil has a value of $0.459 \text{ m}^3 \cdot \text{m}^{-3}$. When the soil matric suction begins to rise, that is, at the increasing suction pressure head, the soil water begins to drain [16]. Initially, the water drains at a low rate, but as the suction pressure keeps increasing, a sudden increase in the water loss rate occurred. Continue increasing the suction pressure would eventually result in a plateau state in the soil water content. The plateau soil water content is known as residual soil water content with a value of $0.098 \text{ m}^3 \cdot \text{m}^{-3}$. In a similar trend, the saturated and residual water contents for sandy soil correspond to 0.375 and $0.053 \text{ m}^3 \cdot \text{m}^{-3}$, while the silty soil has 0.489 and $0.050 \text{ m}^3 \cdot \text{m}^{-3}$, respectively.

The van Genuchten equation in Eq. (1) represents the curvature in Figure 1 for clay. Eq. (1) represents the relation between soil water content and soil matric suction. The field capacity's soil moisture content for clayey soil was predicted using the -3.3 m soil matric suction as input in Eq. (1). Similarly, the permanent wilting point for clayey soil was determined at -150 m soil matric suction using Eq. (1). The same procedure was emulated for sand and silt. The field capacity (FC) and permanent wilting point (PWP) results are shown in Table 1. The FC's soil water content was determined because it indicates the amount of water lower than this limit would remain relatively constant in the soil, except being absorbed by the plant's roots or dry by evaporation. The PWP's soil water content indicates the maximum level at which plant roots could absorb the soil water content;

lower than the PWP's soil water content, the water would firmly attach to the soil greater than plant root absorbing pressure.

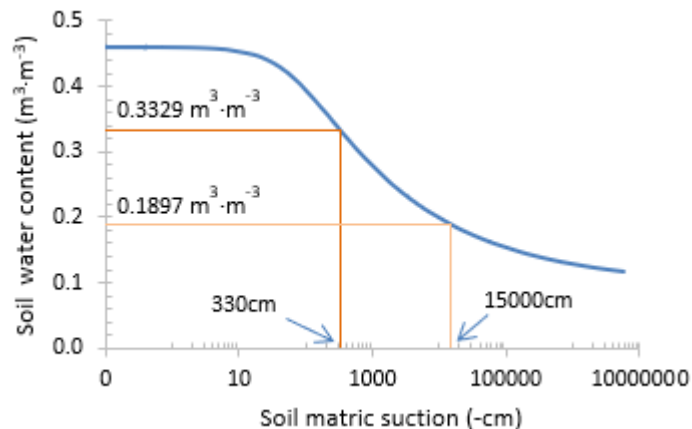


Fig. 1. The characteristic curve for clayey soil texture. The field capacity's soil water content was found as $0.3329 \text{ m}^3 \cdot \text{m}^{-3}$ at soil matric suction of -330 cm
 *Similarly, the permanent wilting point at $0.1897 \text{ m}^3 \cdot \text{m}^{-3}$ soil moisture content was determined at -15000 cm soil matric suction

Table 1 shows the FC and PWP for silt, clay, and sand. The FC's soil water content decreased in the order as $FC_{\text{clay}} > FC_{\text{silt}} > FC_{\text{sand}}$, while the PWP's soil water content was similar in the decreasing order as $PWP_{\text{clay}} > PWP_{\text{silt}} > PWP_{\text{sand}}$. However, the plant available water (PAW), estimated by $PAW = FC - PWP$ [37], was found in the following order $PAW_{\text{silt}} > PAW_{\text{clay}} > PAW_{\text{sand}}$. Thus, clay has the highest water storage (FC) compared to silt and sand; the highest in PWP for clayey soil than silt and sand has reduced its ability to provide readily available water (PAW) for plant root absorption. For this reason, silt has overtaken clay as a soil texture that provides the most readily available water for plant root absorption.

Table 1

Field capacity (FC), permanent wilting point (PWP), and plant available water (PAW) for sand, silt, and clay

Soil texture	FC ($\text{m}^3 \cdot \text{m}^{-3}$)	PWP ($\text{m}^3 \cdot \text{m}^{-3}$)	PAW ($\text{m}^3 \cdot \text{m}^{-3}$)
Clay	0.333	0.190	0.143
Sand	0.055	0.053	0.002
Silt	0.285	0.069	0.216

* The field capacity and permanent wilting point soil moisture contents were determined at -3.3 and -150 m , respectively. The negative sign indicates negative pressure or soil particles suction (attraction) pressure. The equation $FC - PWP$ soil water contents give the estimate for PAW

The PAW is a good indication of soil water content must be present in the soil necessary to maintain readily available water for plant growth. However, it does not indicate the rate at which soil water must be supplied into the soil or the rate of water infiltration into the soil by an irrigation system to sustain the determined PAW. For this reason, Richards' equation was used to estimate the water infiltration [36-39] into the soil at field capacity. Figure 2 shows the water infiltration profile into the clayey soil at different times. The observation was similar to those observed in Goh and Noborio [42]. Until 0.12 days of water infiltration, the entire soil depth remained relatively dry. At

231.48 days, the water has infiltrated into 0.6 m depth of soil. The longer the time allowed for water infiltration, the deeper the water infiltrates into the soil. There was a lag time between the initiation of water infiltration and soil water content rise at a deeper soil depth [27]. A similar observation was also observed for silty and sandy soils.

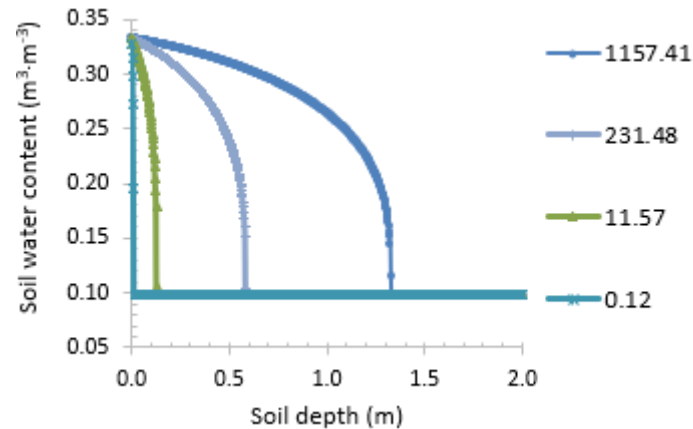


Fig. 2. The variation of soil water contents with soil depths. The curves indicate water infiltration front at 0.12, 11.57, 231.48, and 1157.41 days

Figure 3(a) and 3(b) show the relation between soil depth of interest with the water infiltration time and the infiltrated water. The infiltrated water was referring to the depth of water that has infiltrated into the soil. Different plant roots have different lengths. For example, onions, radish, and spinach were collectively roots depth of 0.15 m, whereas 0.3 m for celery, shallots, swiss chard, and 0.45 m for broccoli, cabbage, carrots, cauliflower, cucumbers, eggplants, kale [43]. Hence, different soil depths were selected in this study. Figure 3(a) showed the time for water to infiltrate into silty soil at 0.15 m depth was 6.1 times more than the time required for sand, whereas only 0.4 times that was faster than the clay. At 0.3 m depth, silty soil was found to have 5.2 times that of sandy soil and again 0.4 times that of clayey soil. A similar trend was observed for 0.45 m depth.

Figure 3(b) showed the silty soil has 334.1 times greater amount of water infiltrated into the soil than sand, while only 0.9 times when compared to clay. In water irrigation management, it is desirable to irrigate the soil and supply the water to the desired depth within the short time possible, that is, the minimum time lag between irrigation initiation and water increment at the desired soil depth. Sandy soil seemed to have met this requirement with the most minimum time required to irrigate the desire soil depth, but the amount of water it could contain was 0.003 times that of silt and clay for all depths. Hence, silt appeared in a better tradeoff in water infiltration time and infiltrated water than sand and clay.

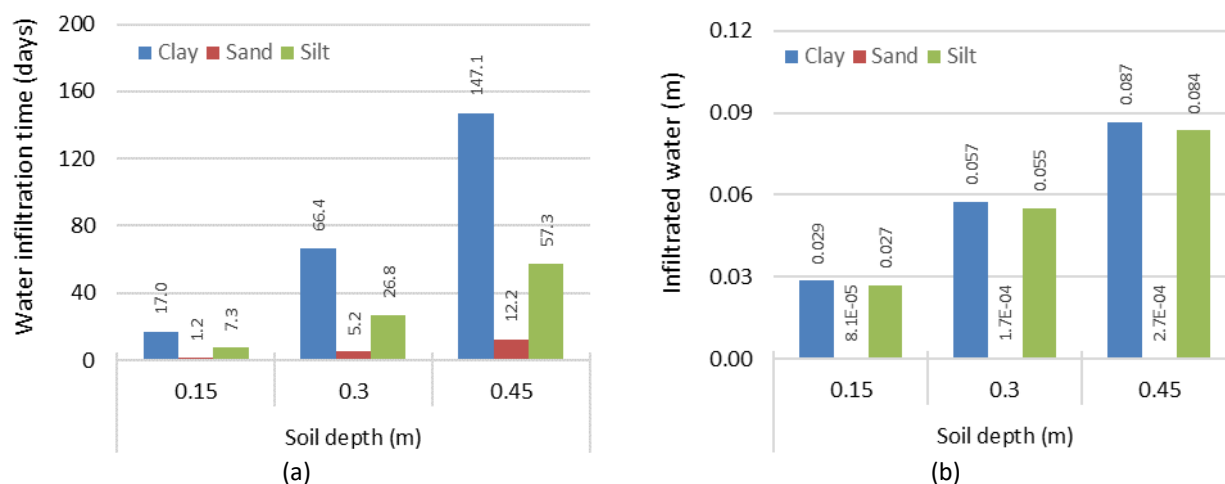


Fig. 3. (a) Water infiltration time to different soil depths, and (b) infiltrated water (m^3 water in m^2 land area) to different soil depths. The soil depths were 0.15, 0.3, and 0.45 m, and the soil textures were sand, clay, and silt

4. Conclusions

Field capacity (FC), permanent wilting (PWP), and plant available water (PAW) are essential parameters in water irrigation management. The FC was found greater in clay than silt and sand. A similar observation was found in PWP. However, silt was found to have the greatest PAW compared to sand and clay. PAW is an essential parameter to indicate water volume must be supplied to the soil depth, but it does not indicate the speed at which water rises in the soil pore space. The Richards' equation coupled with the field capacity value for water infiltration was used to solve this limitation. The results showed that sand has the shortest infiltration time compared to silt and clay. Similarly, sand also has the lowest amount of water infiltrated into the soil. Since the best choice was to have the shortest infiltration time and considerable water amount infiltration into the soil at field capacity, silt soil in the current study turnout to be the best among the three soils. This study revealed the usefulness of coupling Richards' equation and field capacity's soil moisture content. The results will be useful for farmers and field practitioners as early site assessment on crop water management.

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